



# Data Mining for Business Analytics

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## Lecture 10: Similarity and Nearest Neighbors

**Stern School of Business  
New York University  
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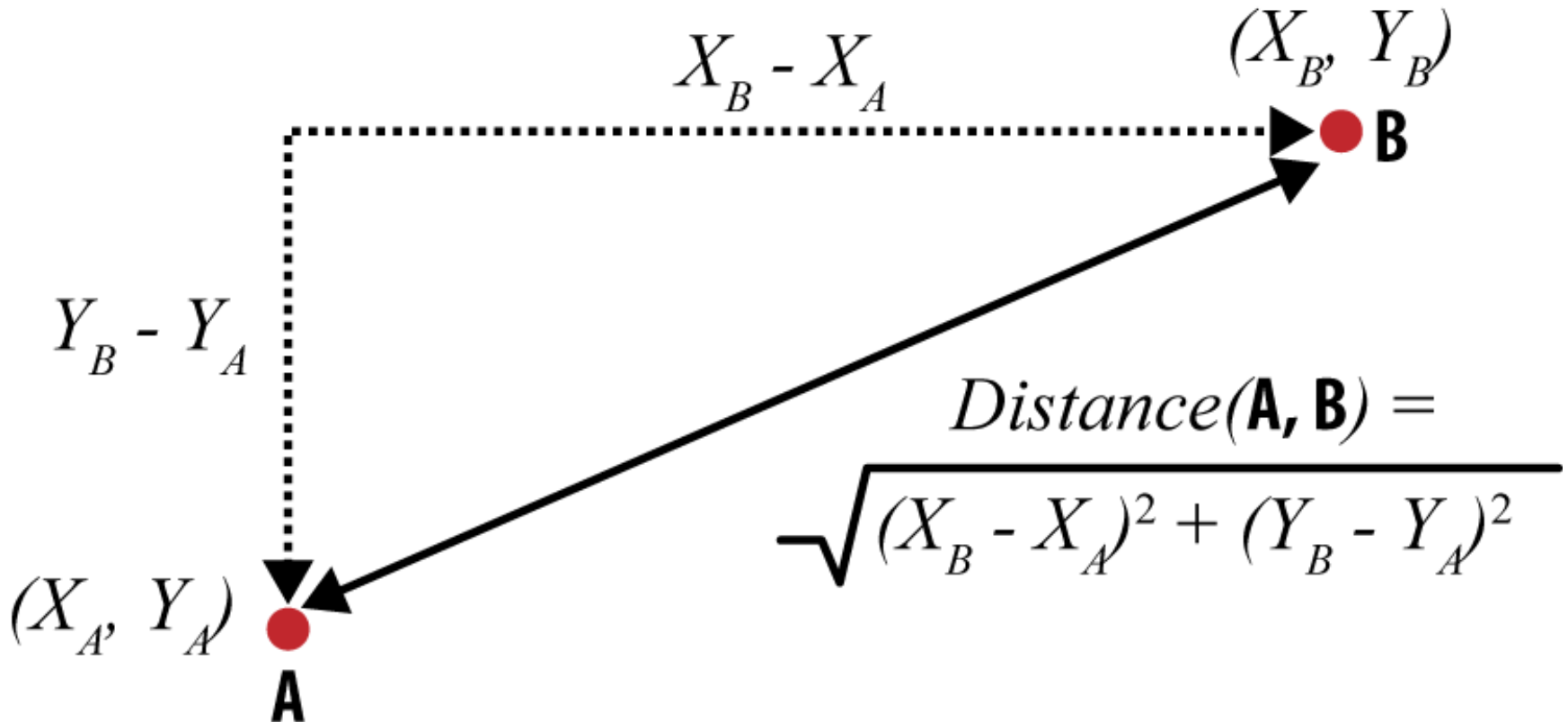
# Similarity and Distance

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- If two objects can be represented as feature vectors, then we can compute the distance between them

Attribute	Person A	Person B
Age	23	40
Years at current address	2	10
Residential status (1=Owner, 2=Renter, 3=Other)	2	1

# Euclidean Distance



# Euclidean Distance

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$$\sqrt{(d_{1,A} - d_{1,B})^2 + (d_{2,A} - d_{2,B})^2 + \dots + (d_{n,A} - d_{n,B})^2}$$

$$d(A, B) = \sqrt{(23 - 40)^2 + (2 - 10)^2 + (2 - 1)^2} = 18.8$$

## Other Distance Functions

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$$d_{\text{Manhattan}}(\mathbf{X}, \mathbf{Y}) = \|\mathbf{X} - \mathbf{Y}\|_1 = |x_1 - y_1| + |x_2 - y_2| + \dots$$

(L1-norm, taxicab-distance)

$$d_{\text{Jaccard}}(X, Y) = 1 - \frac{|X \cap Y|}{|X \cup Y|}$$

$$d_{\text{Cosine}}(\mathbf{X}, \mathbf{Y}) = 1 - \frac{\mathbf{X} \cdot \mathbf{Y}}{\|\mathbf{X}\|_2 \cdot \|\mathbf{Y}\|_2}$$

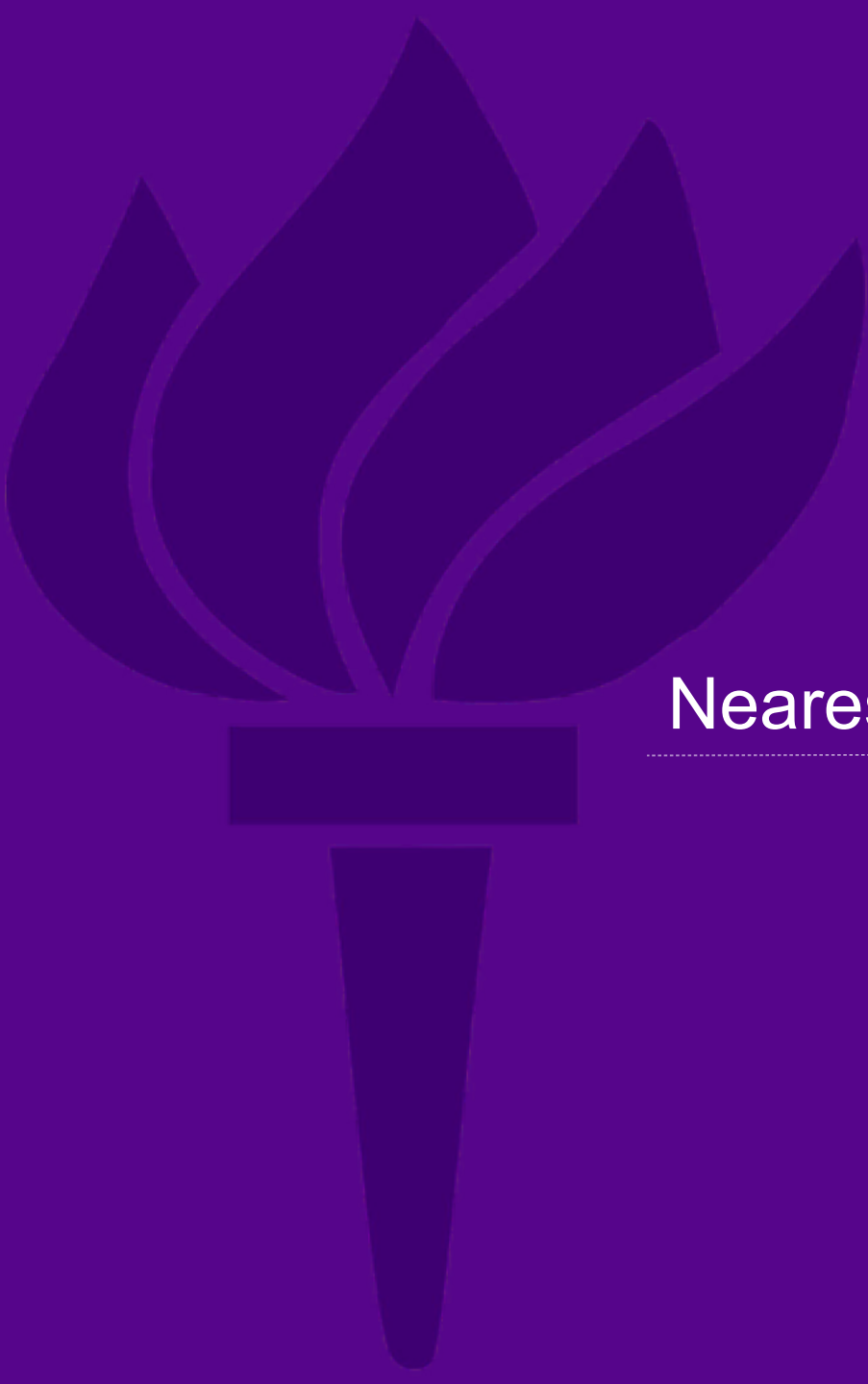
where  $\|\cdot\|_2$  represents the L2 norm, or Euclidean length, of each feature vector (for a vector this is simply the distance from the origin).

## Example: “Whiskey Analytics”

1. **Color:** *yellow, very pale, pale, pale gold, gold, old gold, full gold, amber, etc.* (14 values)
2. **Nose:** *aromatic, peaty, sweet, light, fresh, dry, grassy, etc.* (12 values)
3. **Body:** *soft, medium, full, round, smooth, light, firm, oily.* (8 values)
4. **Palate:** *full, dry, sherry, big, fruity, grassy, smoky, salty, etc.* (15 values)
5. **Finish:** *full, dry, warm, light, smooth, clean, fruity, grassy, smoky, etc.* (19 values)

Consequently there are 68 binary features of each whiskey.

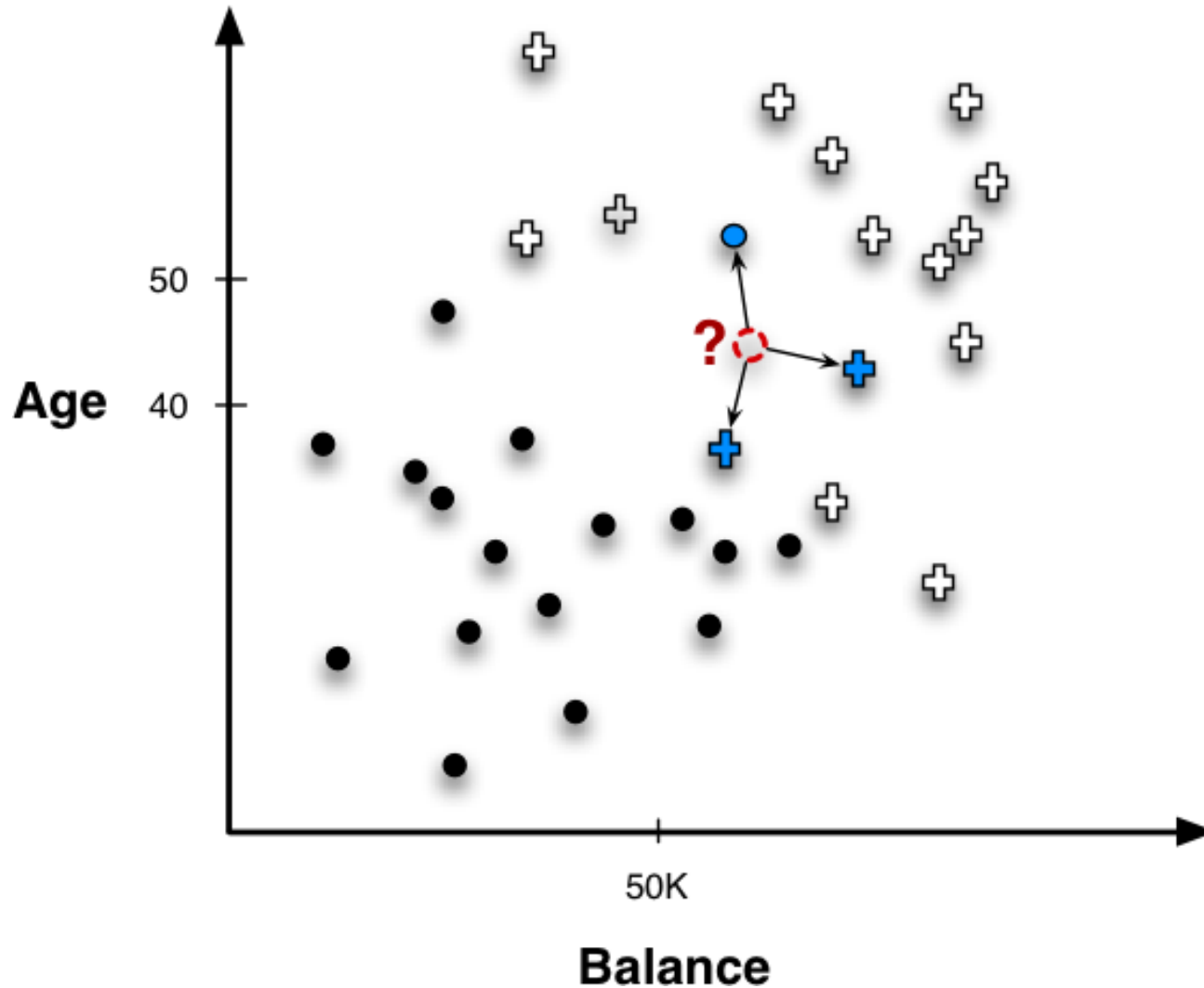
Whiskey	Distance	Descriptors
<i>Bunnahabhain</i>	—	<i>gold; firm,med,light; sweet,fruit,clean; fresh,sea; full</i>
Glenglassaugh	0.643	gold; firm,light,smooth; sweet,grass; fresh,grass
Tullibardine	0.647	gold; firm,med,smooth; sweet,fruit,full,grass,clean; sweet; big,arome,sweet
Ardbeg	0.667	sherry; firm,med,full,light; sweet; dry,peat,sea;salt
Bruichladdich	0.667	pale; firm,light,smooth; dry,sweet,smoke,clean; light; full
Glenmorangie	0.667	p.gold; med,oily,light; sweet,grass,spice; sweet,spicy,grass,sea,fresh; full,long



## Nearest Neighbors

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# Nearest Neighbors for Predictive Modeling





# Nearest Neighbors for Predictive Modeling

Customer	Age	Income (1000s)	Cards	Response (target)	Distance from David
David	37	50	2	?	0
John	35	35	3	Yes	$\sqrt{(35 - 37)^2 + (35 - 50)^2 + (3 - 2)^2} = 15.16$
Rachael	22	50	2	No	$\sqrt{(22 - 37)^2 + (50 - 50)^2 + (2 - 2)^2} = 15$
Ruth	63	200	1	No	$\sqrt{(63 - 37)^2 + (200 - 50)^2 + (1 - 2)^2} = 152.23$
Jefferson	59	170	1	No	$\sqrt{(59 - 37)^2 + (170 - 50)^2 + (1 - 2)^2} = 122$
Norah	25	40	4	Yes	$\sqrt{(25 - 37)^2 + (40 - 50)^2 + (4 - 2)^2} = 15.74$

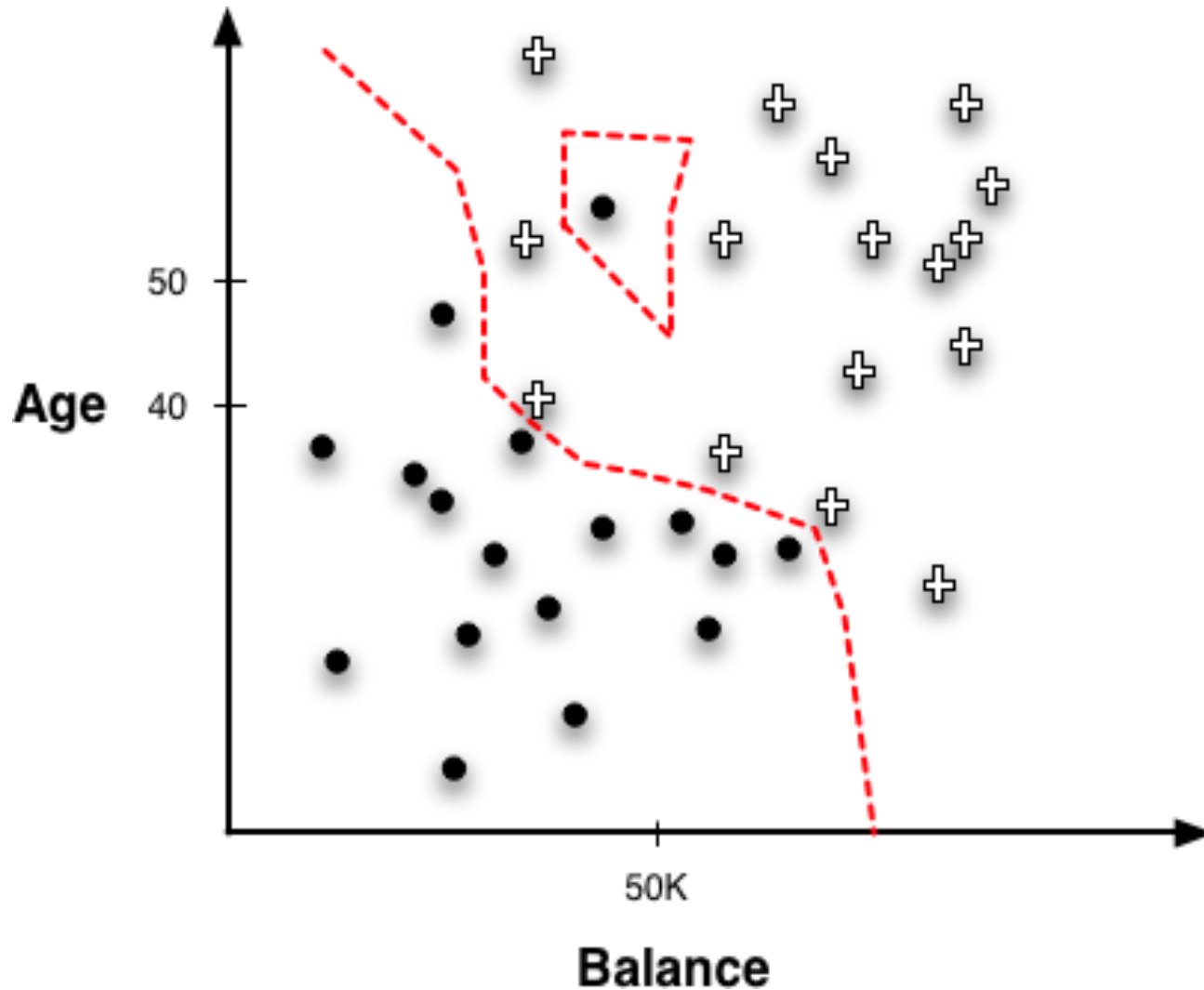
# How Many Neighbors and How Much Influence?

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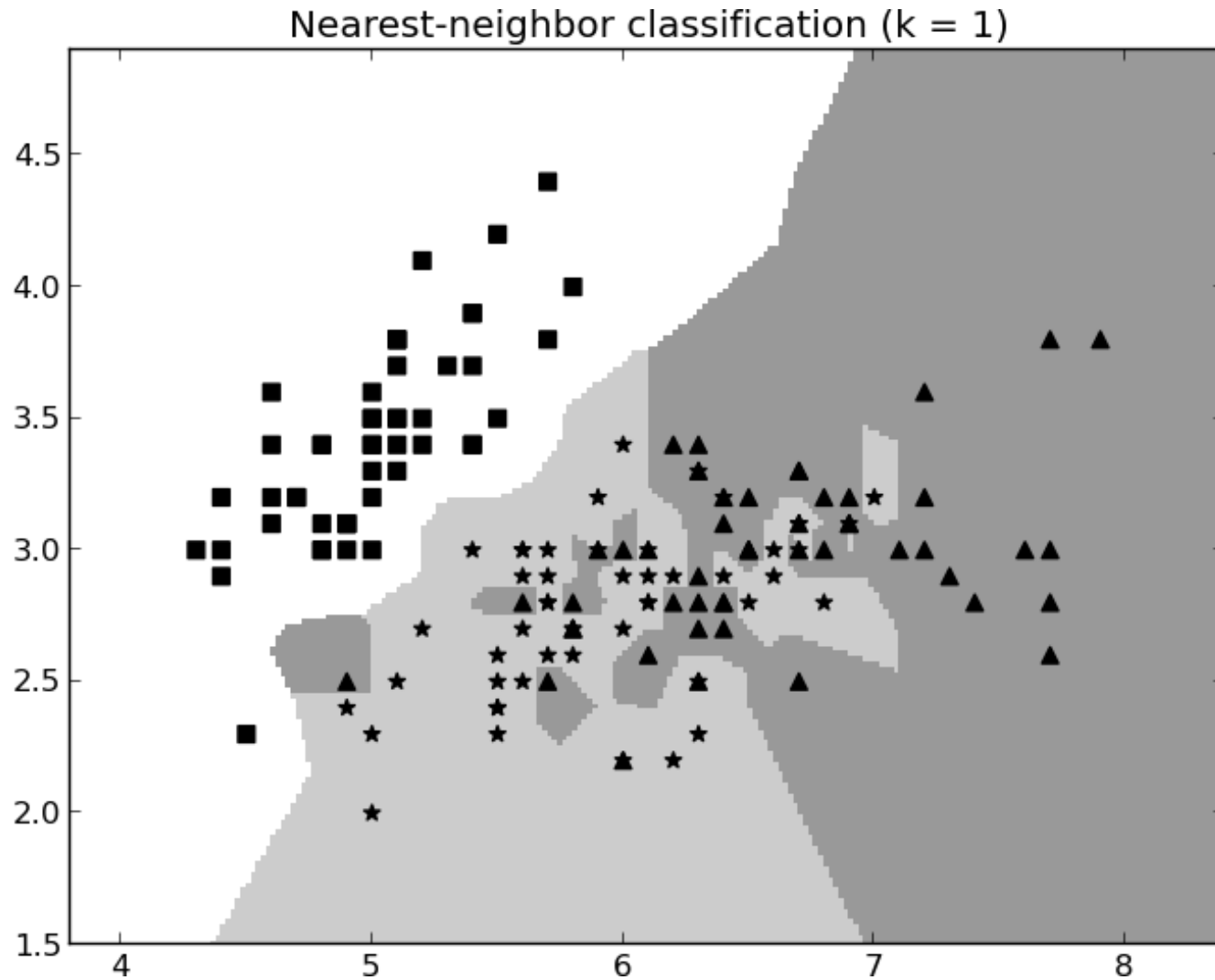
## $k$ Nearest Neighbors

- $k = ?$
- $k = 1?$
- $k = n?$

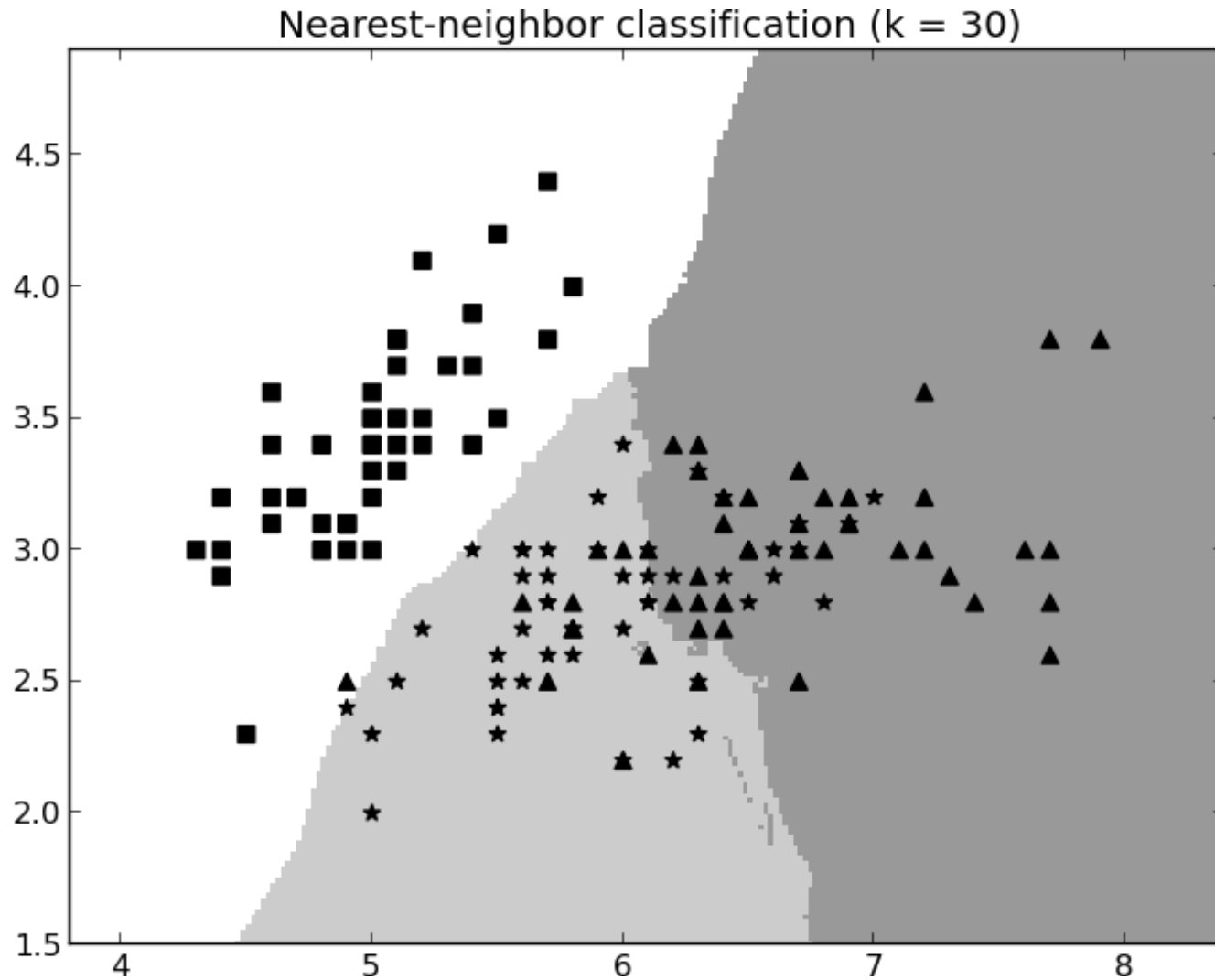
# Geometric Interpretation, Over-fitting, and Complexity



# 1-Nearest Neighbor



# 30-Nearest Neighbors



# Issues with Nearest-Neighbor Models

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- Dimensionality and domain knowledge
  - There might be too many features (and some are irrelevant)
  - The distance function need to consider the scale and importance of the features.
- Computational efficiency