

ACML 2009 Tutorial
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Nanjing

Learning to Rank

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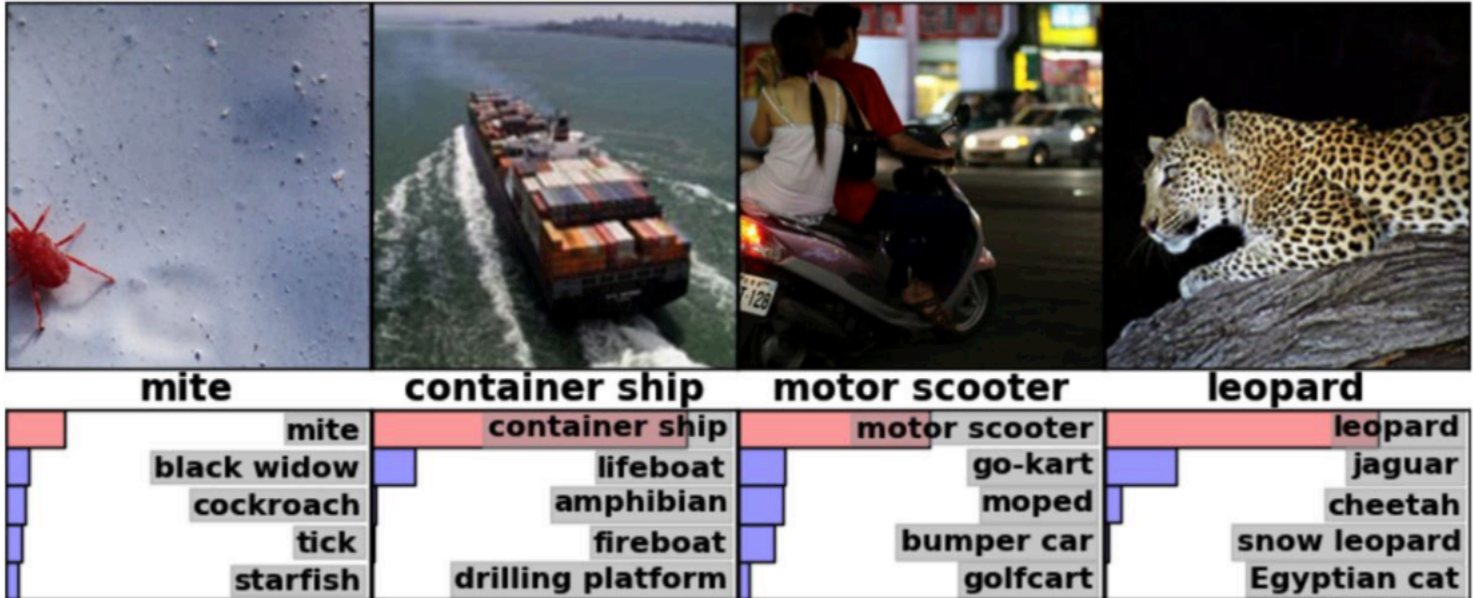
Outline of Tutorial

1. Introduction
2. Learning to Rank Problem
3. Learning to Rank Methods
4. Learning to Rank Theory
5. Learning to Rank Applications
6. Future Directions of Learning to Rank Research
7. Summary

Deep Learning Success: Vision

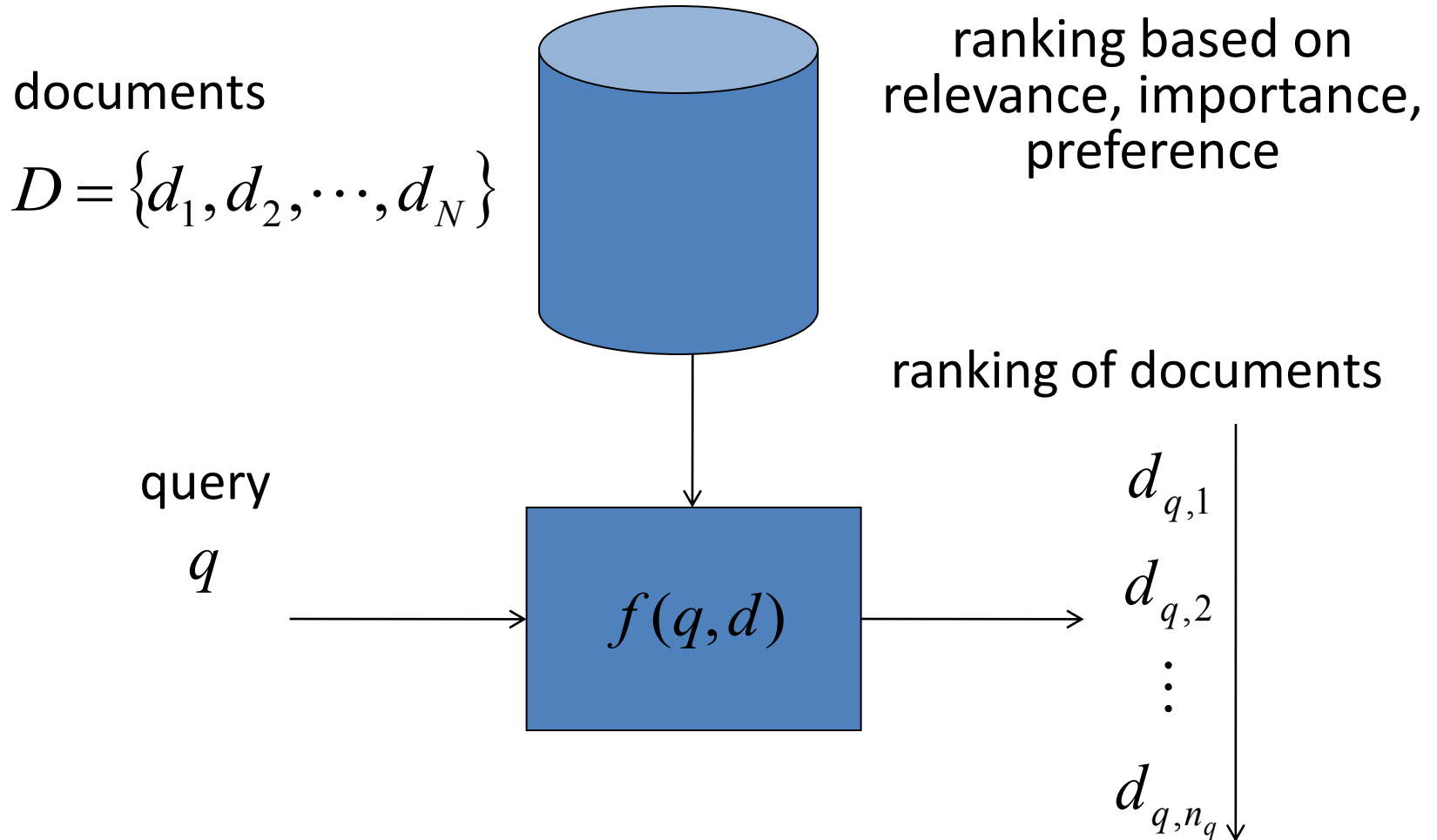
Image Recognition

IMAGENET



1. Introduction

Ranking Problem: Example = Document Search



Ranking Problem

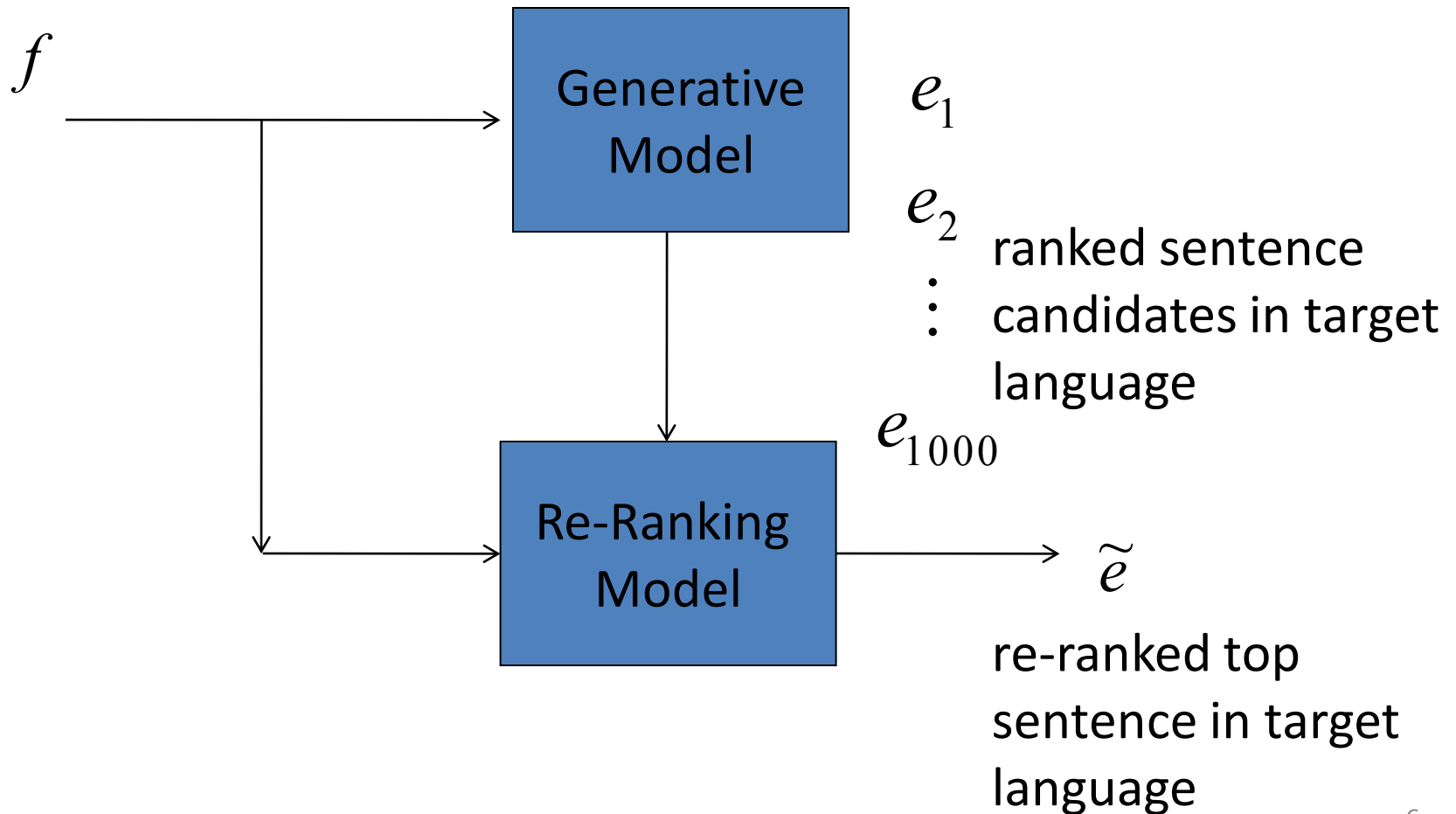
Example = Recommender System

	Item1	Item2	Item3	...	
User1	5	4			
User2	1		2		2
...		?	?	?	
UserM	4	3			

Ranking Problem

Example = Machine Translation

sentence source language



Ranking Problem

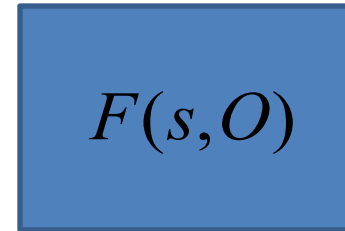
subjects

$$S = \{s_1, s_2, \dots, s_i, \dots\}$$

ranking of objects

$$O = \{o_1, o_2, \dots, o_j, \dots\}$$

$$O_i = \{o_{i,1}, o_{i,2}, \dots, o_{i,n_i}\}$$



$o_{i,1}$

$o_{i,2}$

\vdots

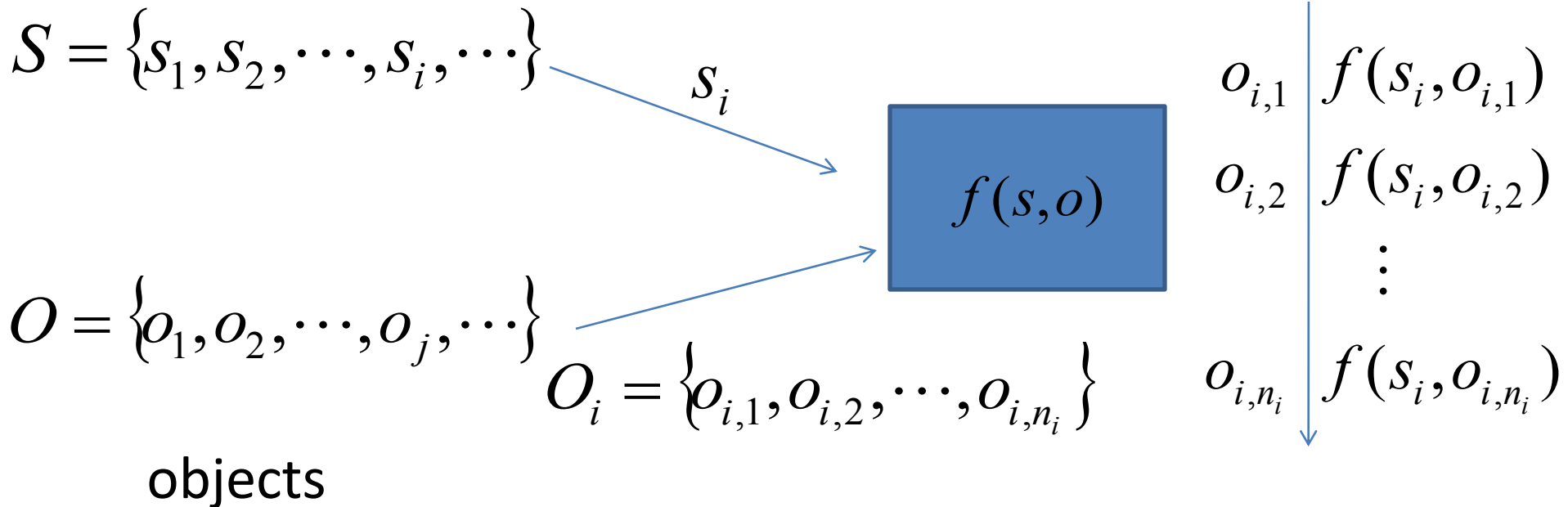
o_{i,n_i}

objects

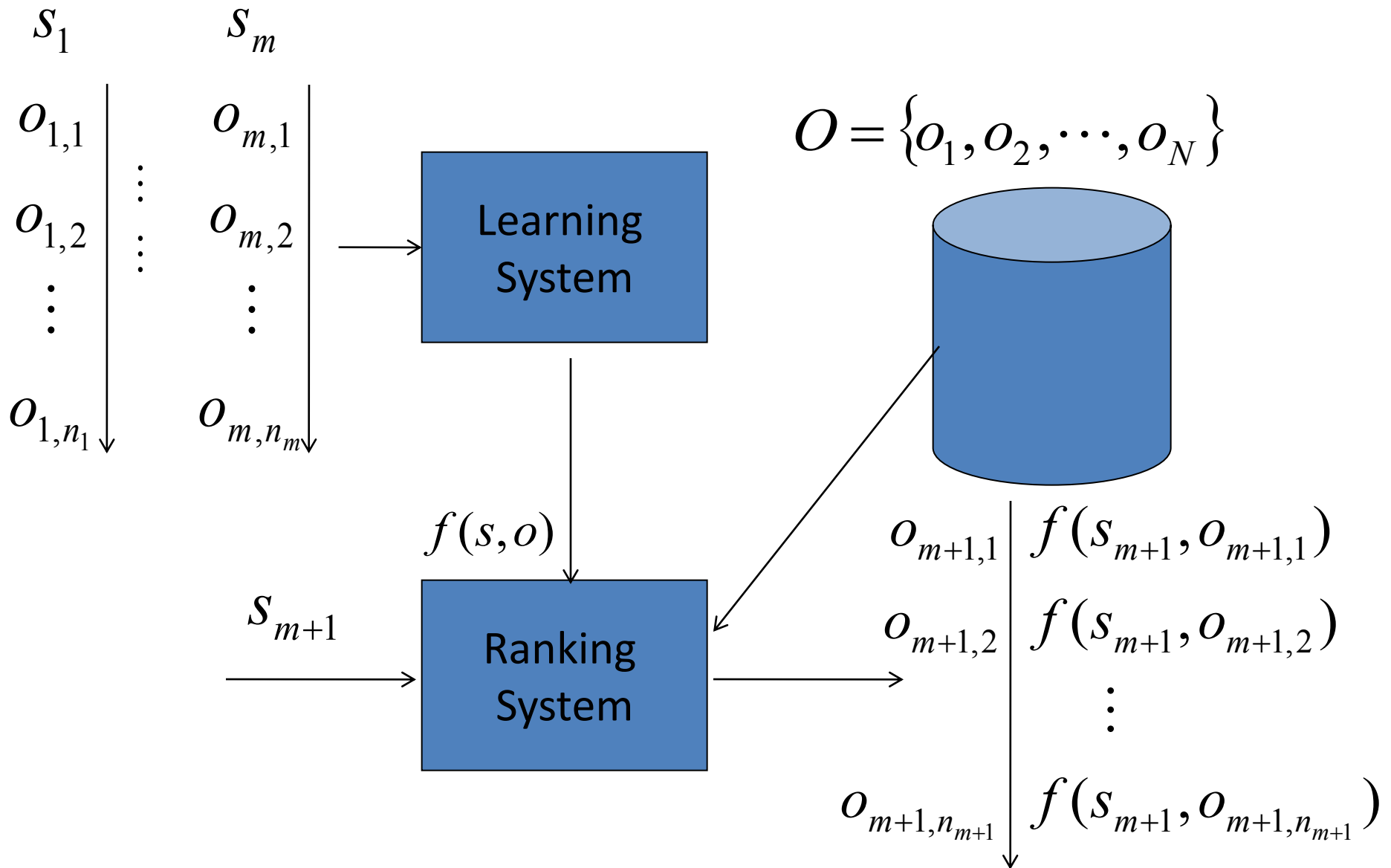
By Ranking Function

subjects

ranking of objects



Learning to Rank



What is Learning to Rank?

- Definition 1 (in broad sense)
Learning to Rank = any machine learning technology for ranking problem
- Definition 2 (in narrow sense)
Learning to Rank = machine learning technology for the above ranking problem (ranking of objects given subject)
- This tutorial takes Definition 2

Ranking Plays Key Role in Many Applications



Applications of Learning to Rank

- Search (Document Search, Entity Search, etc)
- Recommender System (Collaborative Filtering)
- Key Phrase Extraction
- Question Answering
- Document Summarization
- Opinion Mining
- Sentiment Analysis
- Machine Translation

Technologies on Learning to Rank

- Methods
 - Pointwise Methods
 - Pairwise Methods
 - Listwise Methods
- Theory
 - Generalization
 - Consistency
- Applications
 - Search
 - Collaborative Filtering
 - Key Phrase Extraction

Recent Trends on Learning to Rank

- Successfully applied to search
- Over 100 publications at SIGIR, ICML, NIPS, etc
- One book on learning to rank for information retrieval
- 2 sessions at SIGIR every year
- 3 SIGIR workshops
- Special issue at Information Retrieval Journal
- LETOR benchmark dataset, over 400 downloads

<http://research.microsoft.com/en-us/um/beijing/projects/letor/index.html>

Scope of This Tutorial

- Overview of Learning to Rank technologies
- Focusing on Learning to Rank methods
- Touching theoretical issues
- Showing future directions
- Knowledge necessary for this tutorial:
Machine Learning

Other 'Learning to Rank' Methods *Not Covered* in This Tutorial

- Rank Aggregation
- Ranking of Objects on Graph
 - Link Analysis (e.g, Page Rank)
- Unsupervised Learning of Ranking
 - Probabilistic Model in Information Retrieval (e.g., BM25, Language Model for IR)

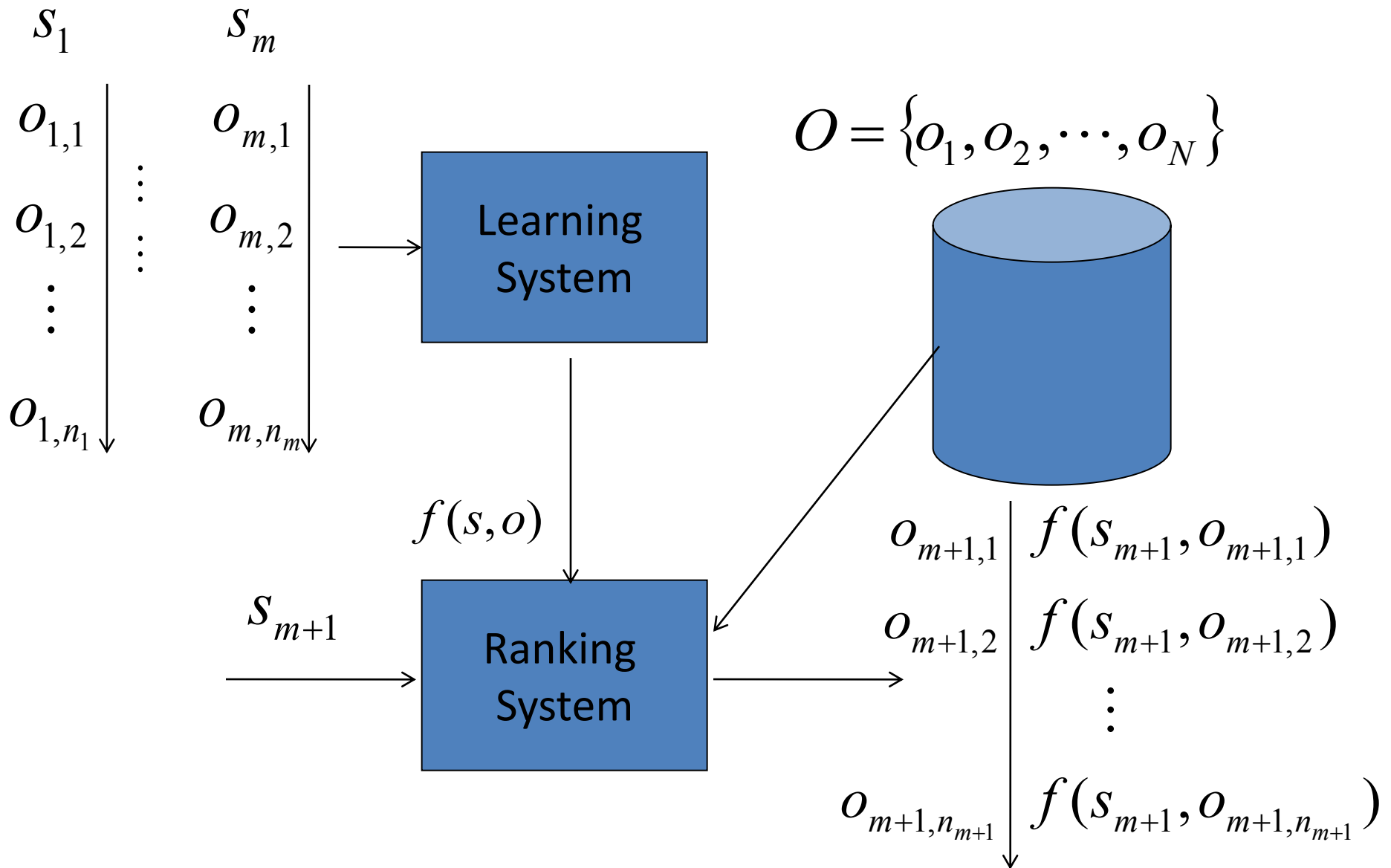
2. Learning to Rank Problem

Learning to Rank Problem

- 2.1 Problem Formulation
- 2.2 Example: Learning to Rank for Search
- 2.3 Issues in Learning to Rank
- 2.4 Relations with Other Learning Tasks

2.1 Problem Formulation

Learning to Rank

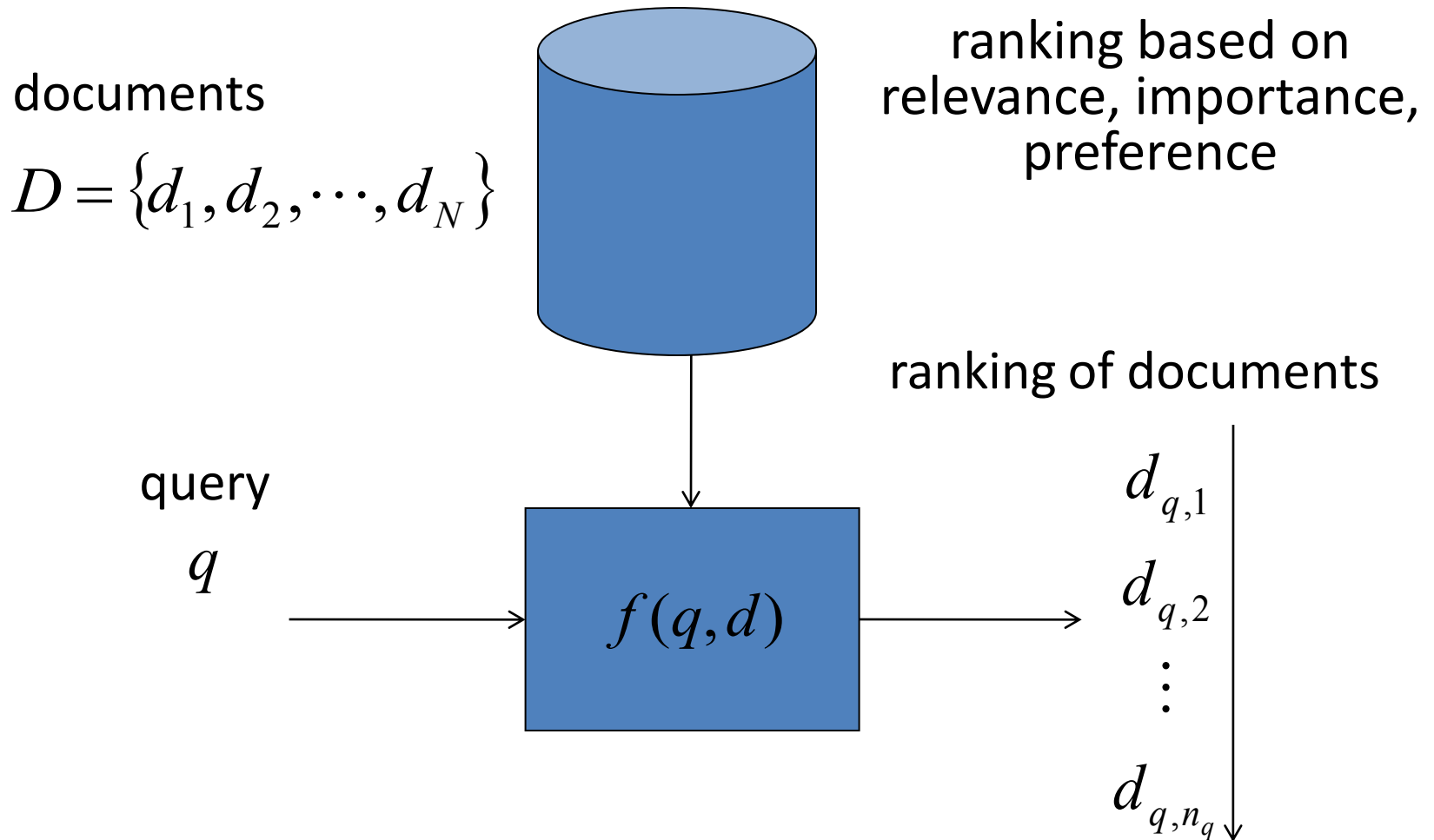


Characteristics of Learning to Rank

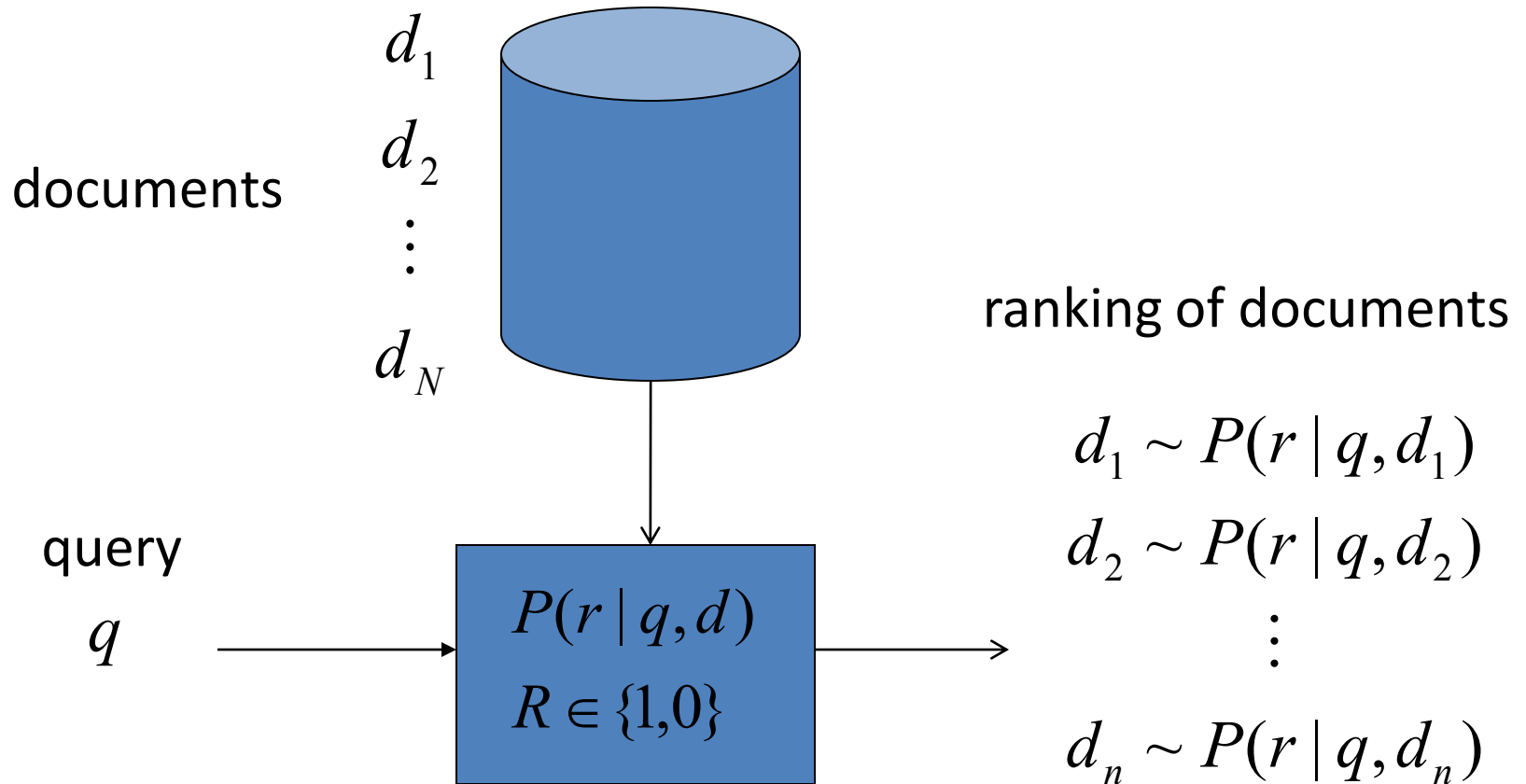
- Machine learning technologies
- Ranking of objects by subject
- Learning ranking function $f(s, o)$
- Using labeled data (supervised learning)
- Ranking function is feature based
- This tutorial mainly takes *document search* as example

2.2 Example: Learning to Rank for Search

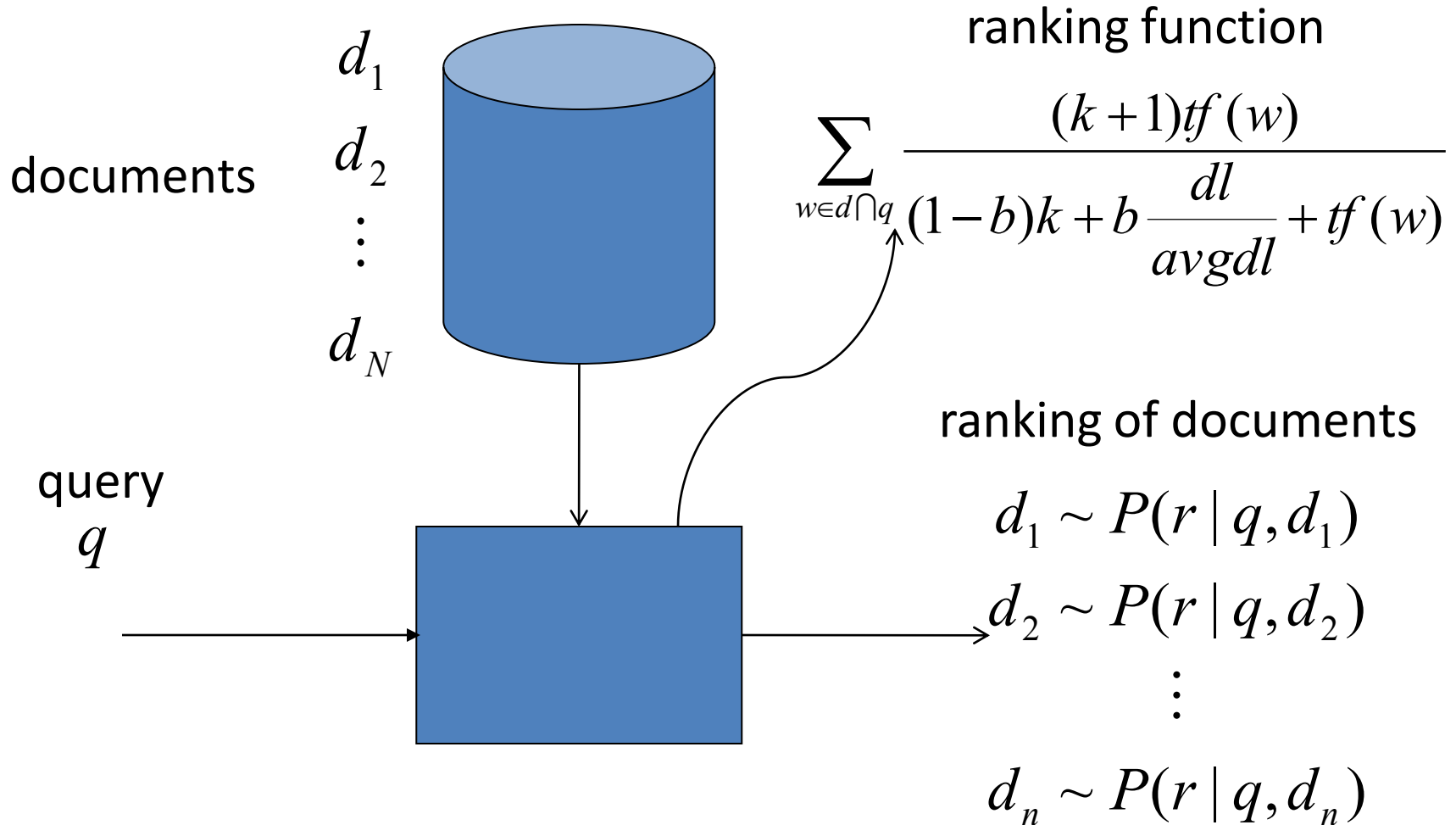
Ranking Problem: Example = Document Search



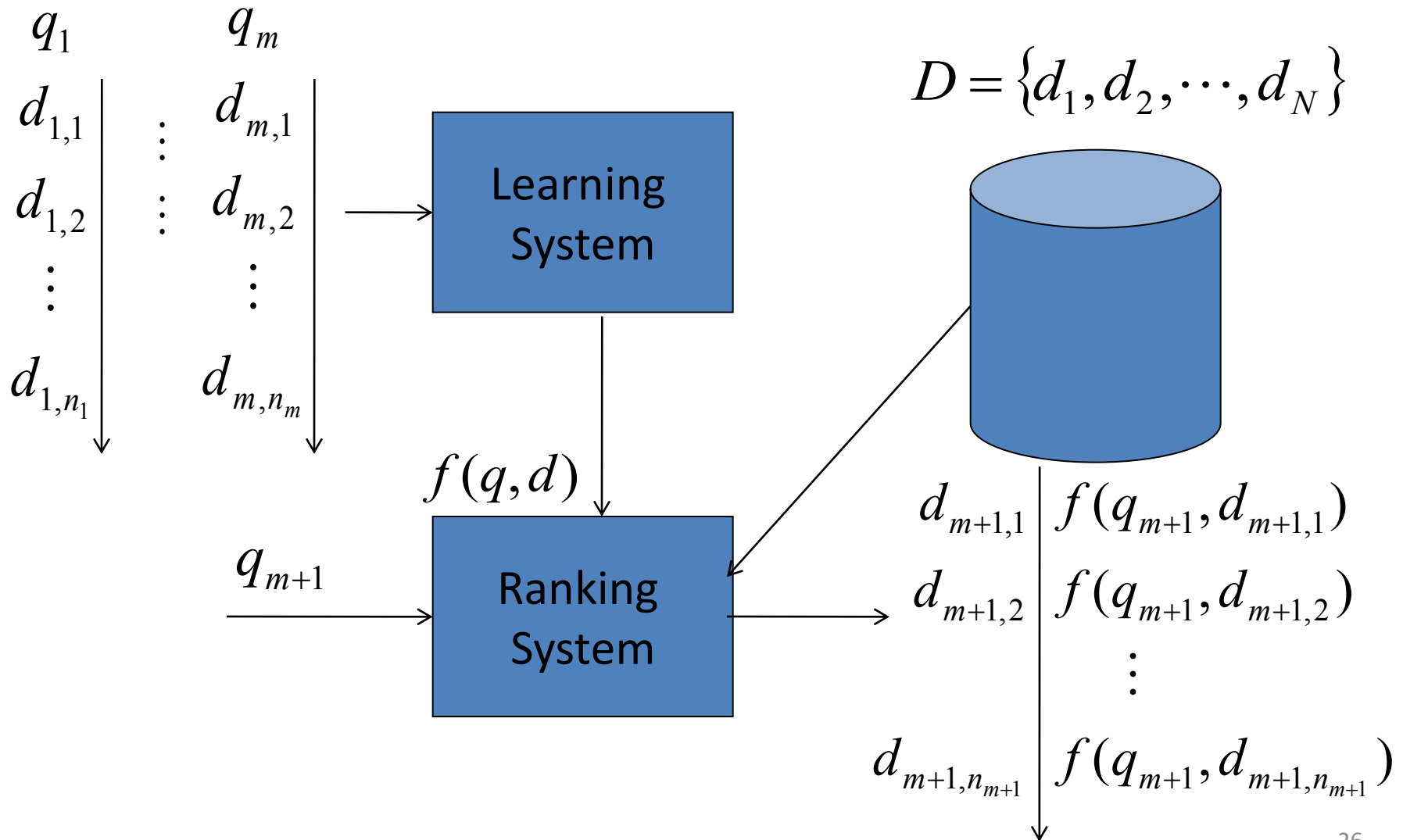
Traditional Approach = Probabilistic Model



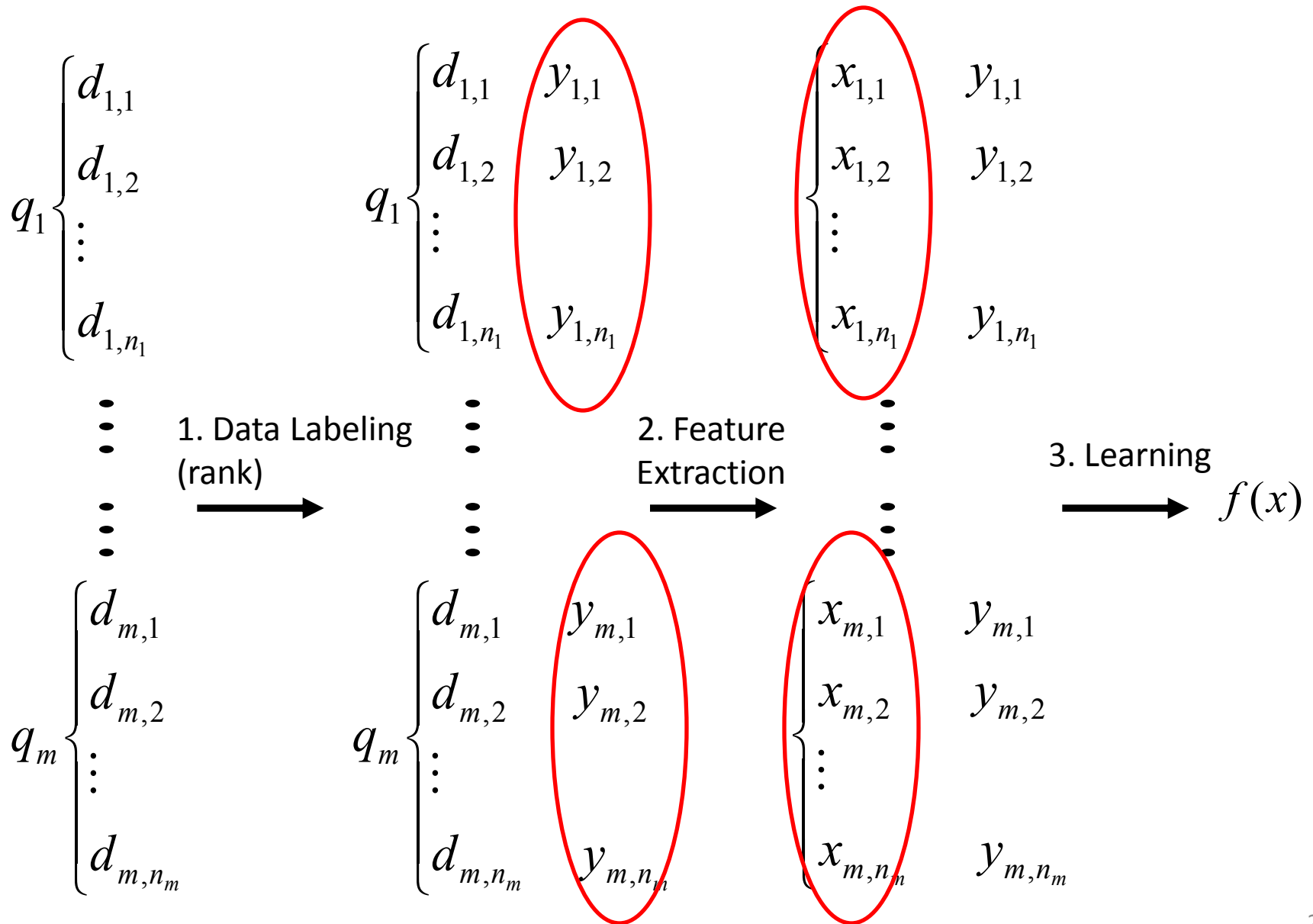
BM25



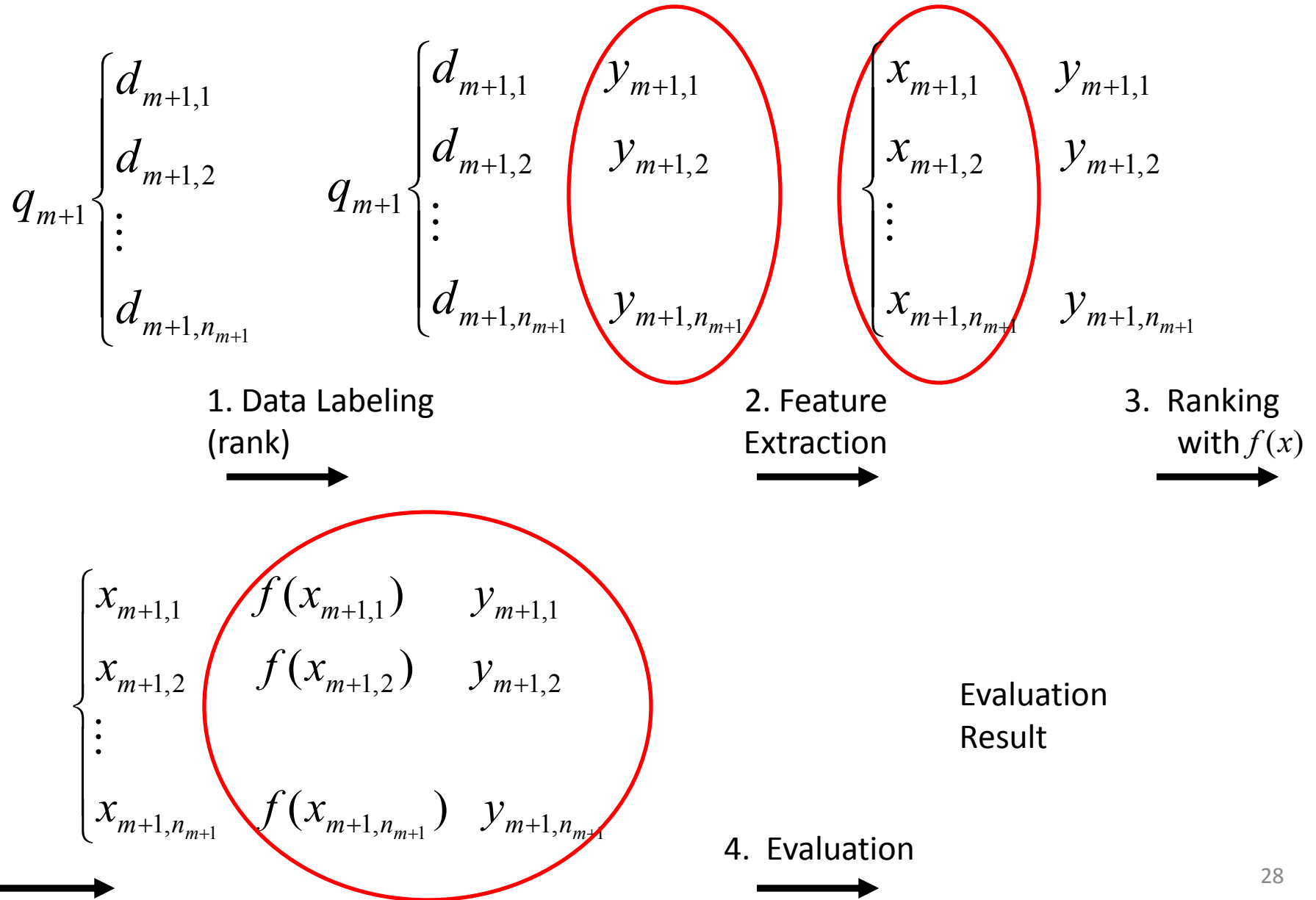
New Approach = Learning to Rank



Training Process



Testing Process



Notes

- Features are functions of query and document
- Query and associated documents form a group
- Groups are i.i.d. data
- Feature vectors within group are not i.i.d. data
- Ranking model is function of features
- Several data labeling methods (here labeling of rank as example)

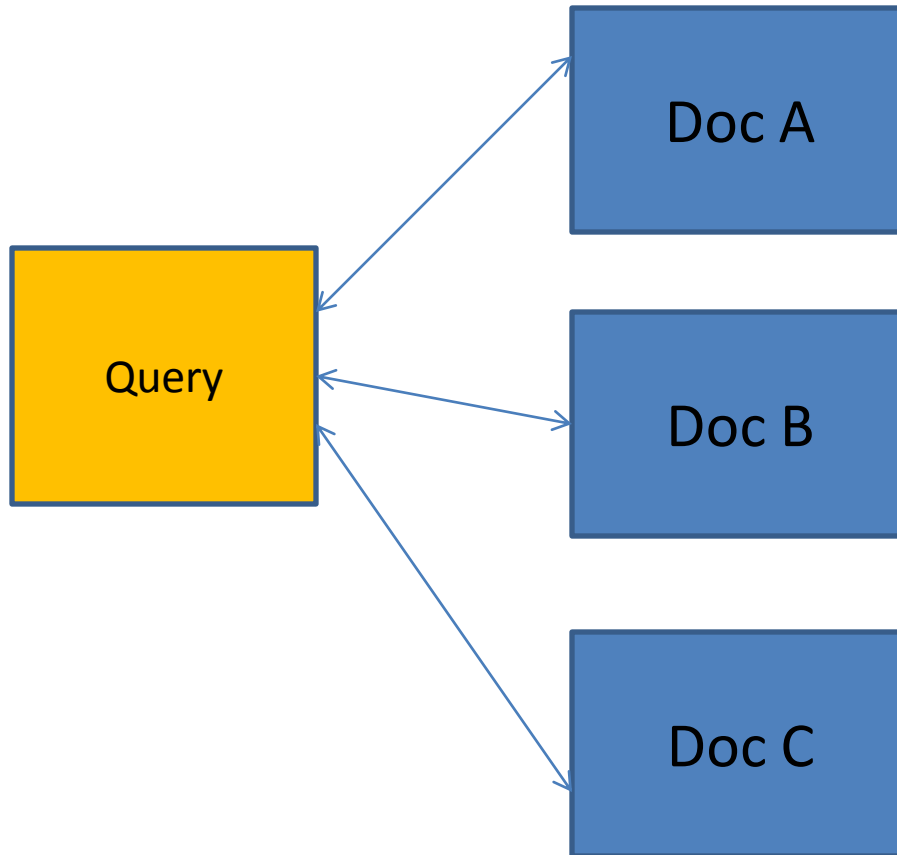
2.3 Issues in Learning to Rank

Issues in Learning to Rank

- Data Labeling
- Feature Extraction
- Evaluation Measure
- Learning Method (Model, Loss Function, Algorithm)

Data Labeling Problem

- E.g., relevance of documents w.r.t. query

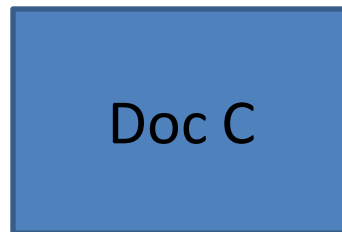
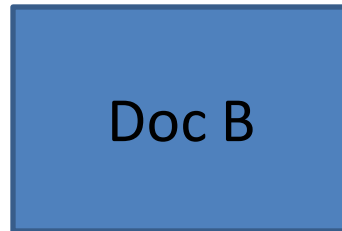
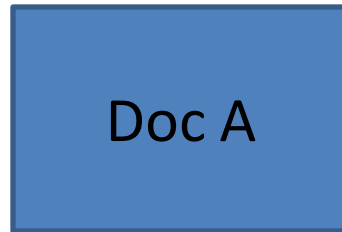


Data Labeling Methods

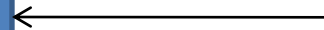
- Labeling of Ranks
 - Multiple levels (e.g., relevant, partially relevant, irrelevant)
 - Widely used in IR
- Labeling of Ordered Pairs
 - Ordered pairs between documents (e.g. $A > B$, $B > C$)
 - Implicit relevance judgment: derived from click-through data
- Creation of List
 - List (or permutation) of documents is given
 - Ideal but difficult to implement

Implicit Relevance Judgment

ranking of documents at search system



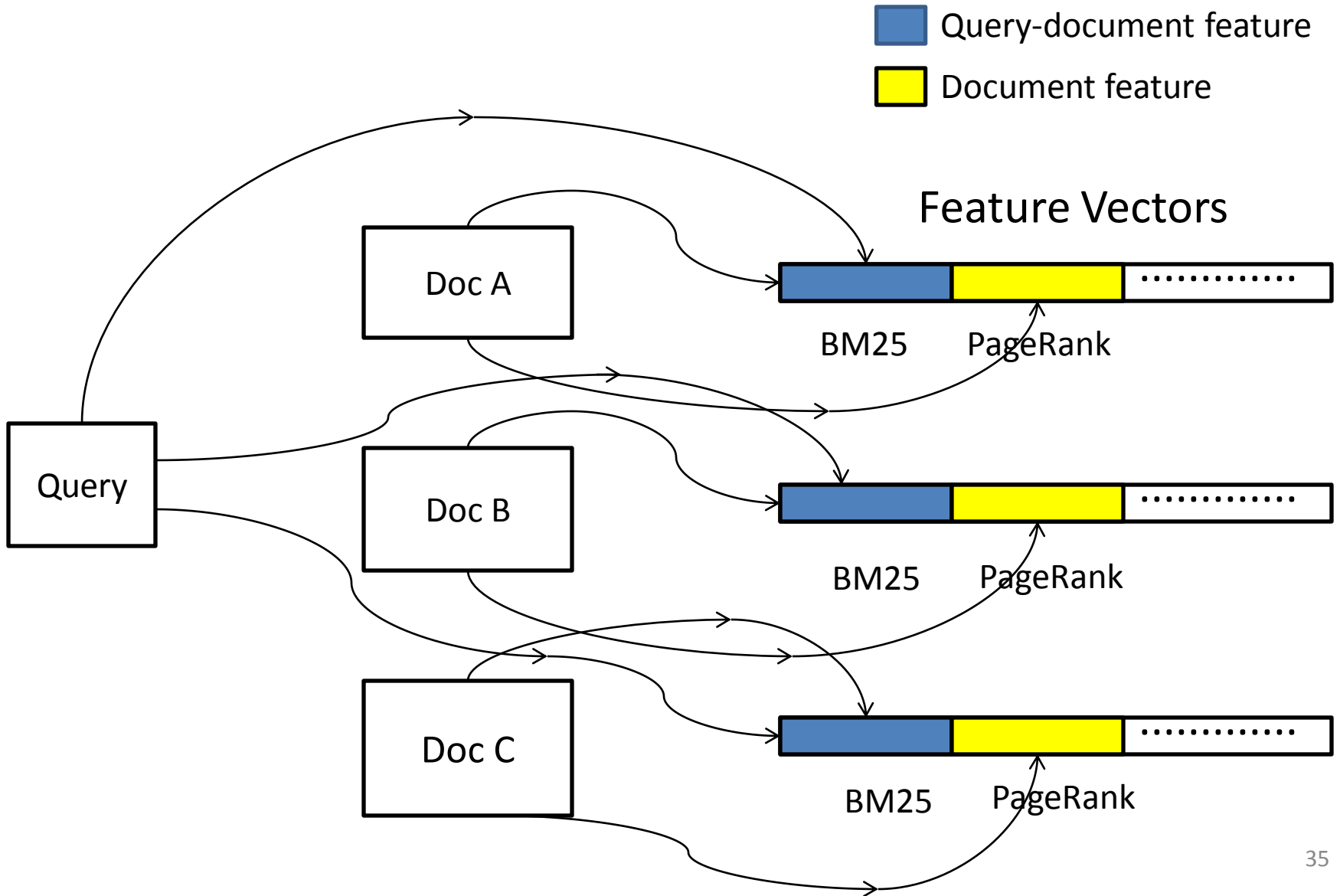
users often clicked on Doc B



ordered pair

$B > A$

Feature Extraction



Example Features

- Relevance: BM25
- Relevance: proximity
- Relevance: query exactly occurs in document
- Importance: PageRank

Evaluation Measures

- Important to rank top results correctly
- Measures
 - NDCG (Normalized Discounted Cumulative Gain)
 - MAP (Mean Average Precision)
 - MRR (Mean Reciprocal Rank)
 - WTA (Winners Take All)
 - Kendall's Tau

NDCG

- Evaluating ranking using labeled ranks
- NDCG at position j

$$\frac{1}{n_j} \sum_{i=1}^j (2^{r(i)} - 1) / \log(1 + i)$$

NDCG (cont')

- Example: perfect ranking
 - (3, 3, 2, 2, 1, 1, 1) rank $r=3,2,1$
 - (7, 7, 3, 3, 1, 1, 1) gain $2^{r(j)} - 1$
 - (1, 0.63, 0.5, 0.43, 0.39, 0.36, 0.33) position discount
 - (7, 18.11, 24.11, ...) DCG $1/\log(1+j)$
$$\sum_{i=1}^j (2^{r(i)} - 1) / \log(1+i)$$
 - (1/7, 1/18.11, 1/24.11, ...) normalizing factor n_j
 - (1, 1,1,1,1,1,1) NDCG for perfect ranking

NDCG (cont')

- Example: imperfect ranking
 - (2, 3, 2, 3, 1, 1, 1)
 - (3, 7, 3, 7, 1, 1, 1) Gain
 - (1, 0.63, 0.5, 0.43, 0.39, 0.36, 0.33) Position discount
 - (3, 14.11, 20.11, ...) DCG
 - (0.43, 0.78, 0.83,) NDCG
- Imperfect ranking decreases NDCG

2.4 Relations with Other Learning Tasks

Relations with Other Learning Tasks

- No need to predict category
vs Classification
- No need to predict value of $f(q, d)$
vs Regression
- Relative ranking order is more important
vs Ordinal regression
- *Learning to rank can be approximated by classification, regression, ordinal regression*

Ordinal Regression (Ordinal Classification)

- Categories are ordered
 - 5, 4, 3, 2, 1
 - e.g., rating restaurants
- Prediction
 - Map to ordered categories

3. Learning to Rank Methods

Learning to Rank Methods

- 3.1 Overview of Learning to Rank Methods
- 3.2 Pairwise Classification
- 3.3 Cost-sensitive Pairwise Classification
- 3.4 Probabilistic Model for Ranking
- 3.5 Direct Optimization of Evaluation Measure
- 3.6 Approximation of Evaluation Measure
- 3.7 Evaluation Results

3.1 Overview of Learning to Rank Methods

Three Major Approaches

- Pointwise approach
- Pairwise approach
- Listwise approach

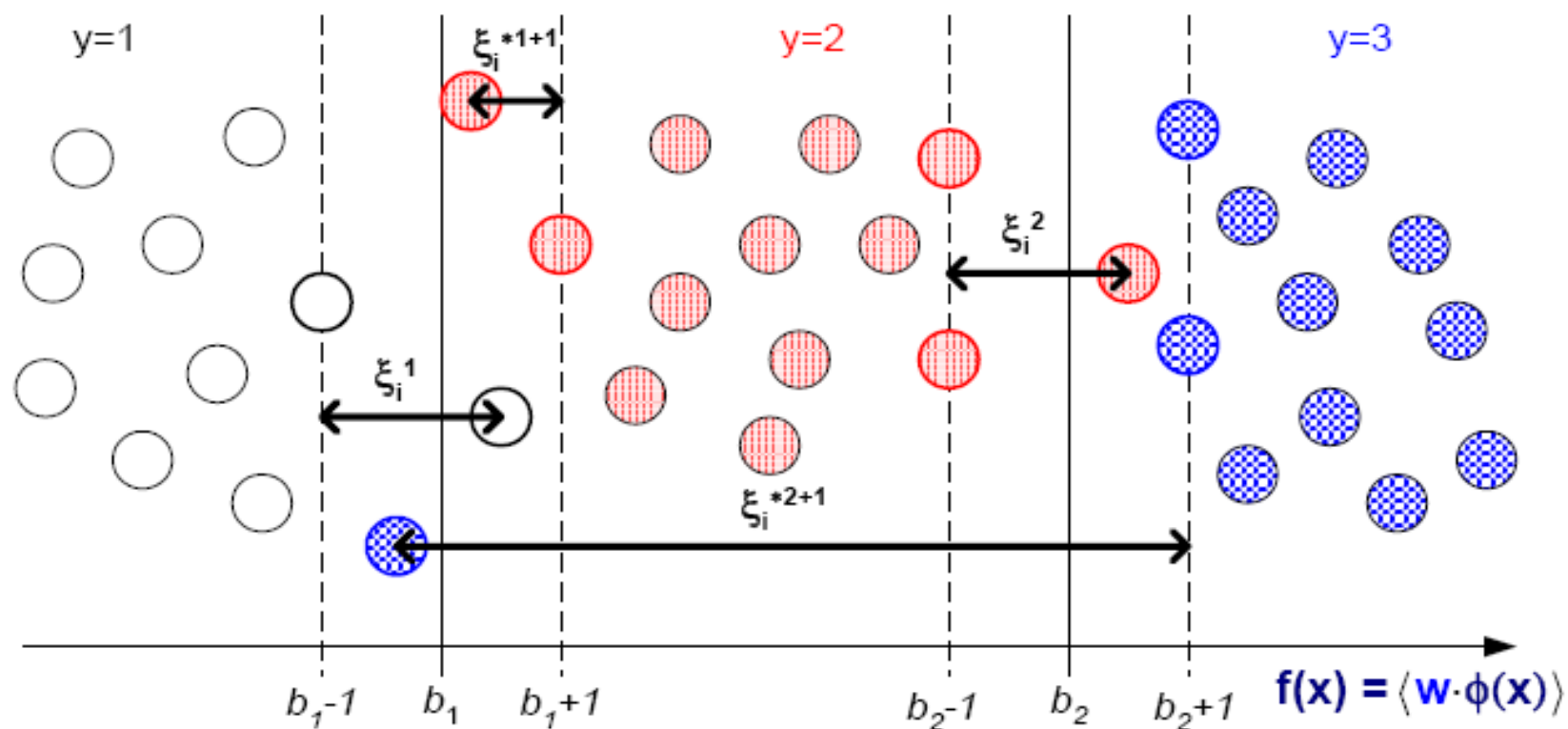
- First is suitable to ordinal regression
- Latter two are more suitable to learning to rank (e.g., ranking in search)

Pointwise Approach

- Transforming ranking to regression, classification, or ordinal regression
- Query-document group structure is ignored

Point-wise learning

- Goal is to learn a threshold to separate each rank



Pointwise Approach

	Learning		
	Regression	Classification	Ordinal Regression
Input	Feature vector x		
Output	Real number $y = f(x)$	Category $y = \text{classifier}(x)$	Ordered category $y = \text{thresold}(f(x))$
Model	Ranking function $f(x)$		
Loss Function	Regression loss	Classification loss	Ordinal regression loss

Pointwise Approach

	Ranking
Input	$\mathbf{x} = \{x_i\}_{i=1}^n$
Output	Permutation on vectors $\boldsymbol{\pi} = \text{sort}(\{f(x_i)\}_{i=1}^n)$
Model	Ranking function $f(x)$
Loss Function	Ranking evaluation measure

Pairwise Approach

- Transforming ranking to pairwise classification
- Query-document group structure is ignored

Pairwise Approach

	Learning	Ranking
Input	Ordered feature vector pair $(x_i, x_j), x_i > x_j$	Feature vectors $\mathbf{X} = \{x_i\}_{i=1}^n$
Output	Classification on order of vector pair $y_{i,j} = \text{classifier}(x_i - x_j)$	Permutation on vectors $\boldsymbol{\pi} = \text{sort}(\{f(x_i)\}_{i=1}^n)$
Model	Ranking function $f(x)$	
Loss Function	Pairwise classification loss	Ranking evaluation measure

Listwise Approach

- List as instance
- Query-document group structure is used
- Straightforwardly represents learning to rank problem

Listwise Approach

	Learning & Ranking
Input	Feature vectors $\mathbf{X} = \{x_i\}_{i=1}^n$
Output	Permutation on feature vectors $\boldsymbol{\pi} = \text{sort}(\{f(x_i)\}_{i=1}^n)$
Model	Ranking function $f(x)$
Loss Function	Listwise loss function (ranking evaluation measure)

Learning to Rank Methods

- Pointwise Approach
 - Subset Ranking [Cossock and Zhang, 2006]: Regression
 - SVM [Nallapati, 2004]: Binary Classification Using SVM
 - McRank [Li et al 2007]: Multi-Class Classification Using Boosting Tree
 - Prank [Crammer and Singer 2002]: Ordinal Regression Using Perceptron
 - Large Margin [Shashua & Levin 2002]: Ordinal Regression Using SVM

Learning to Rank Methods

- Pairwise Approach
 - Ranking SVM: Pairwise Classification Using SVM
 - RankBoost [Freund et al 2003]: Pairwise Classification Using Boosting
 - RankNet [Burges et al 2005]: Pairwise Classification Using Neural Net
 - Frank [Tsai et al 2007]: Pairwise Classification Using Fidelity Loss and Neural Net
 - GBRank [Zheng et al 2007]: Pairwise Regression Using Boosting Tree
 - IR SVM [Cao et al 2006]: Cost-sensitive Pairwise Classification Using SVM
 - Multiple SVMs [Qin et al 2007]: Multiple SVMs

Learning to Rank Methods

- Listwise Approach
 - ListNet [Cao et al 2007]: Probabilistic Ranking Model
 - ListMLE [Xia et al 2008]: Probabilistic Ranking Model
 - AdaRank [Xu and Li 2007]: Direct Optimization of Evaluation Measure
 - SVM Map [Yue et al 2007]: Direct Optimization of Evaluation Measure
 - PermuRank [Xu et al 2008]: Direct Optimization of Evaluation Measure
 - Soft Rank [Taylor et al 2008]: Approximation of Evaluation Measure
 - Lambda Rank [Burges et al 2007]: Using Implicit Loss Function

Learning to Rank Methods

- Other Methods
 - K-Nearest Neighbor Ranker [Geng et al 2008]
 - Semi-Supervised Learning [Jin et al 2008]

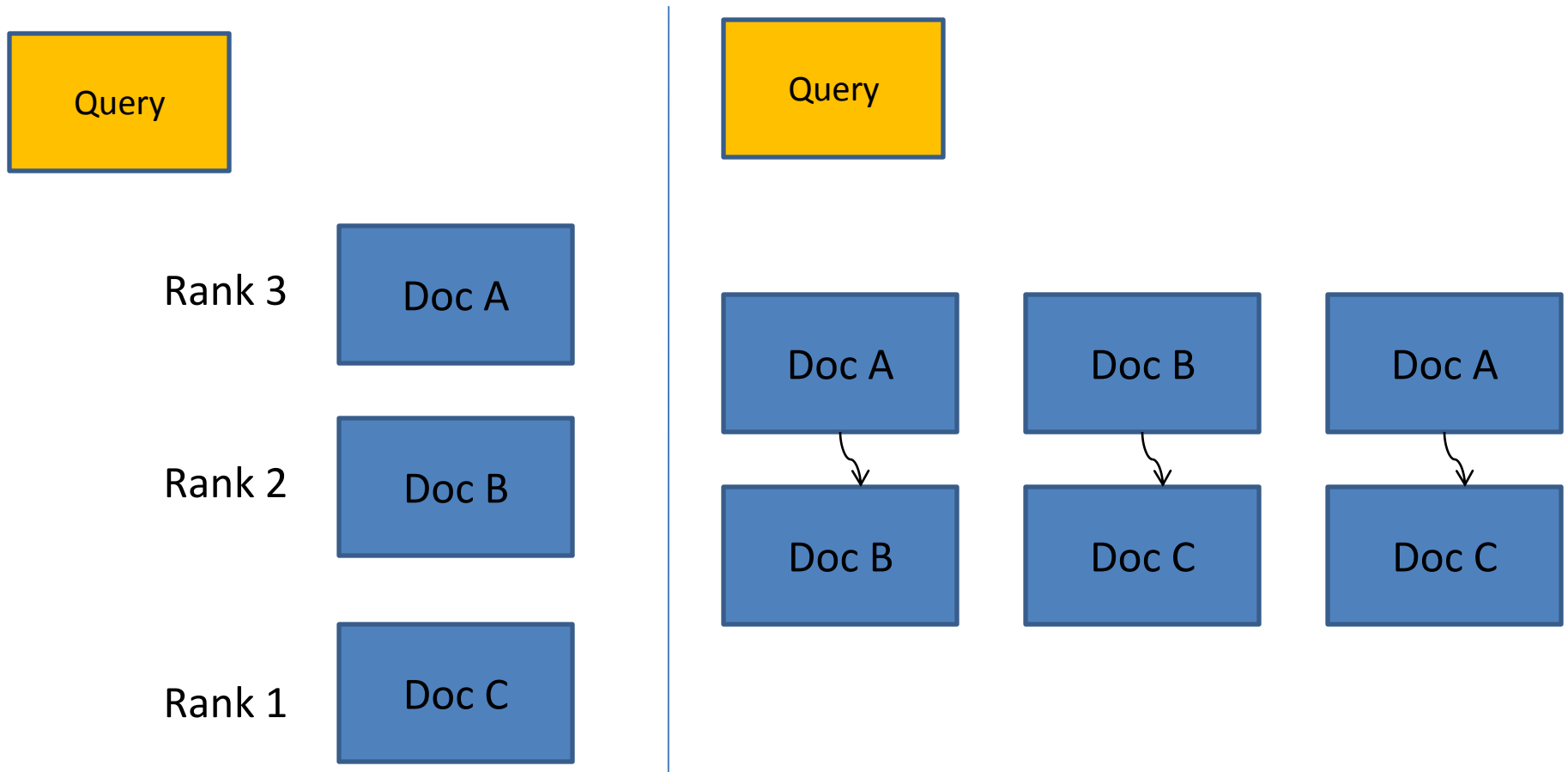
3.2 Pairwise Classification

Pairwise Classification Methods

- Ranking SVM
- RankBoost
- RankNet

Pairwise Classification

- Converting document list to document pairs



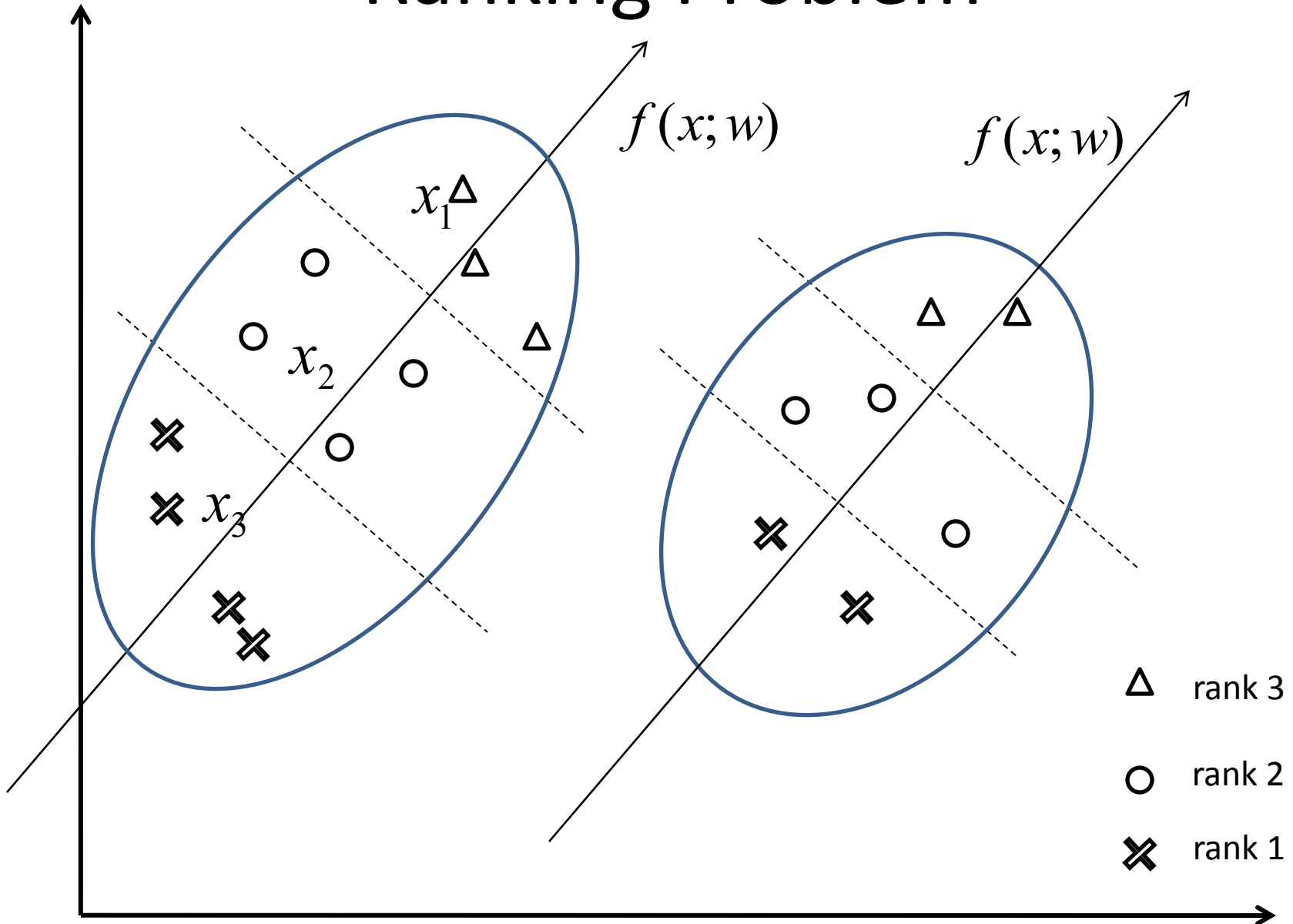
Ranking SVM

Transforming Ranking to Pairwise Classification

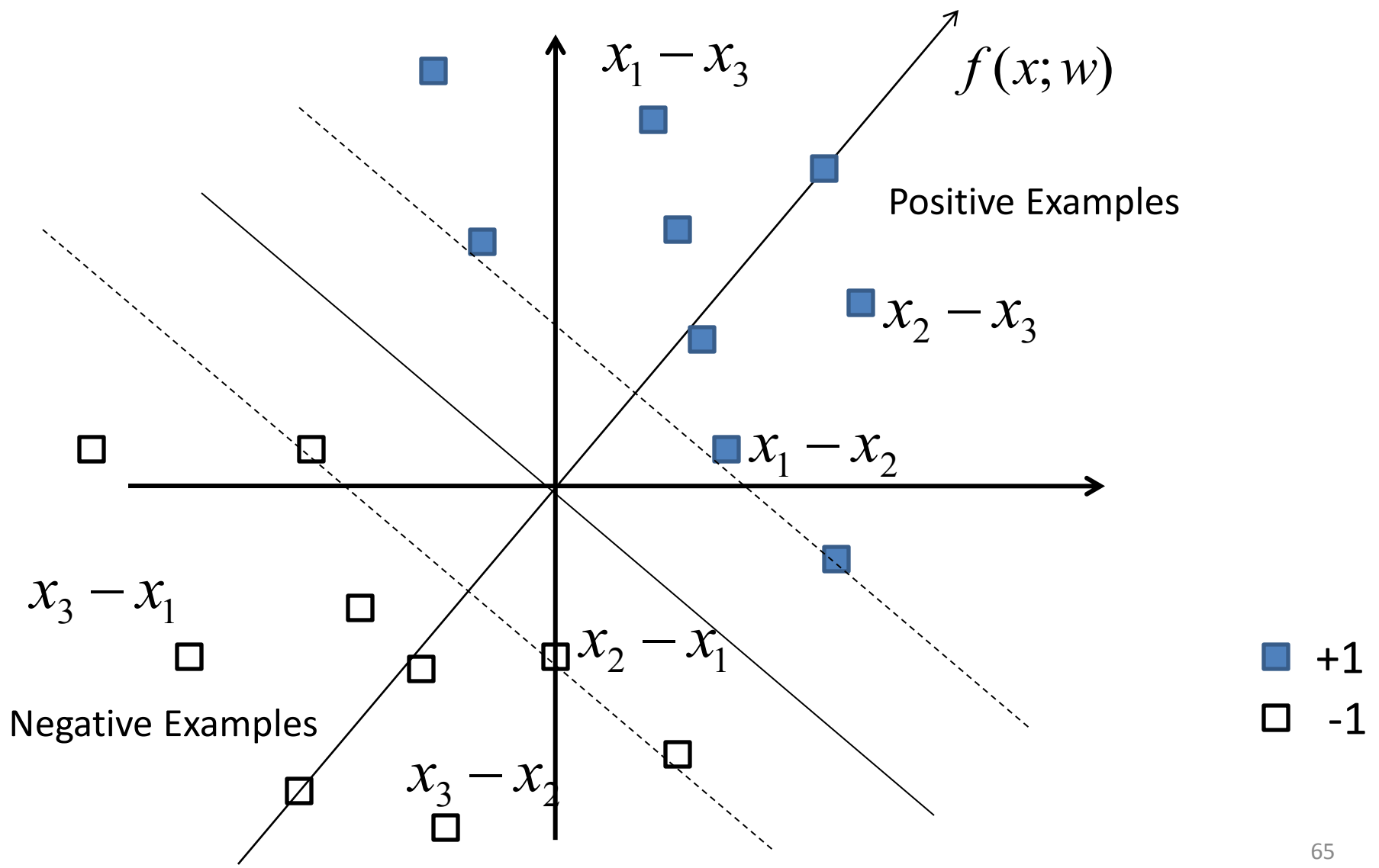
- Input space: X
- Ranking function $f : X \rightarrow R$
- Ranking: $x_i \succ x_j \Leftrightarrow f(x_i; w) > f(x_j; w)$
- Linear ranking function: $f(x; w) = \langle w, x \rangle$
 $\langle w, x_i - x_j \rangle > 0 \Leftrightarrow f(x_i; w) > f(x_j; w)$
- Transforming to pairwise classification:

$$(x_i - x_j, z), \quad z = \begin{cases} +1 & x_i \succ x_j \\ -1 & x_j \succ x_i \end{cases}$$

Ranking Problem



Transformed Pairwise Classification Problem



Ranking SVM

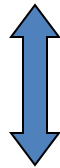
- Pairwise classification on differences of feature vectors
- Corresponding positive and negative examples
- Negative examples are redundant and can be discarded
- Hyper plane passes the origin
- Soft Margin and Kernel can be used
- *Ranking SVM* = pairwise classification SVM

Learning of Ranking SVM

$$\min_{w, \xi} \frac{1}{2} \|w\|^2 + C \sum_{i=1}^l \xi_i$$

$$z_i \langle w, x_i^{(1)} - x_i^{(2)} \rangle \geq 1 - \xi_i \quad i = 1, \dots, l$$

$$\xi_i \geq 0$$



$$\min_w \sum_{i=1}^l \left[1 - z_i \langle w, x_i^{(1)} - x_i^{(2)} \rangle \right]_+ + \lambda \|w\|^2$$

$$[s]_+ = \max(0, s) \quad \lambda = \frac{1}{2C}$$

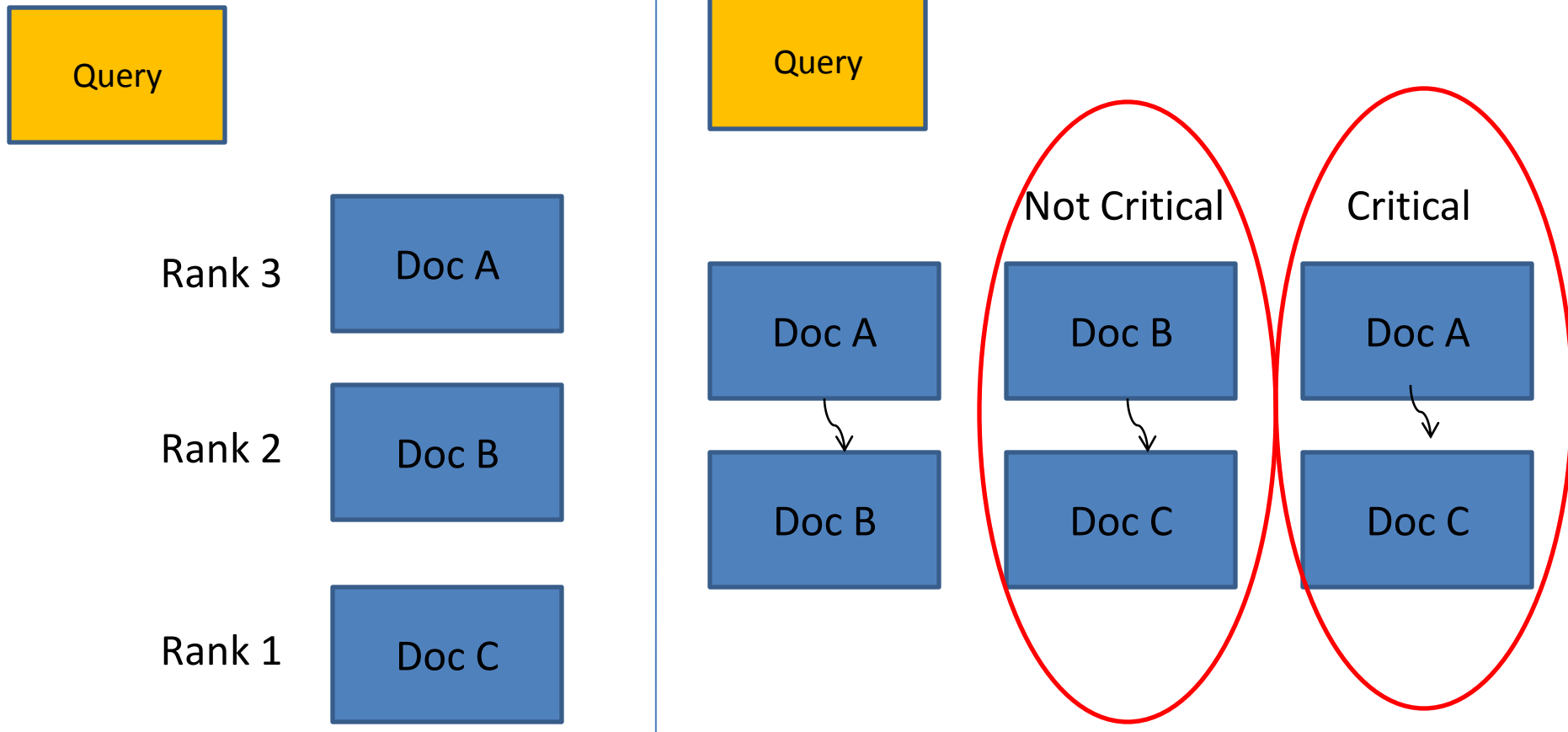
3.3 Cost-sensitive Pairwise Classification

Cost-Sensitive Pairwise Classification Methods

- IR SVM
- Multiple SVMs

Cost-sensitive Pairwise Classification

- Converting to document pairs



IR SVM

Problems with Ranking SVM

- Not sufficient emphasis on correct ranking on top

Ranks: 3, 2, 1

ranking 1: 2 3 2 1 1 1 1

ranking 2: 3 2 1 2 1 1 1

ranking 2 should be better than ranking 1

Ranking SVM views them as the same

- Numbers of pairs vary according to queries

q1: 3 2 2 1 1 1 1

q2: 3 3 2 2 2 1 1 1 1 1

number of pairs for q1 : $2*(2-2) + 4*(3-1) + 8*(2-1) = 14$

number of pairs for q2: $6*(3-2) + 10*(3-1) + 15*(2-1) = 31$

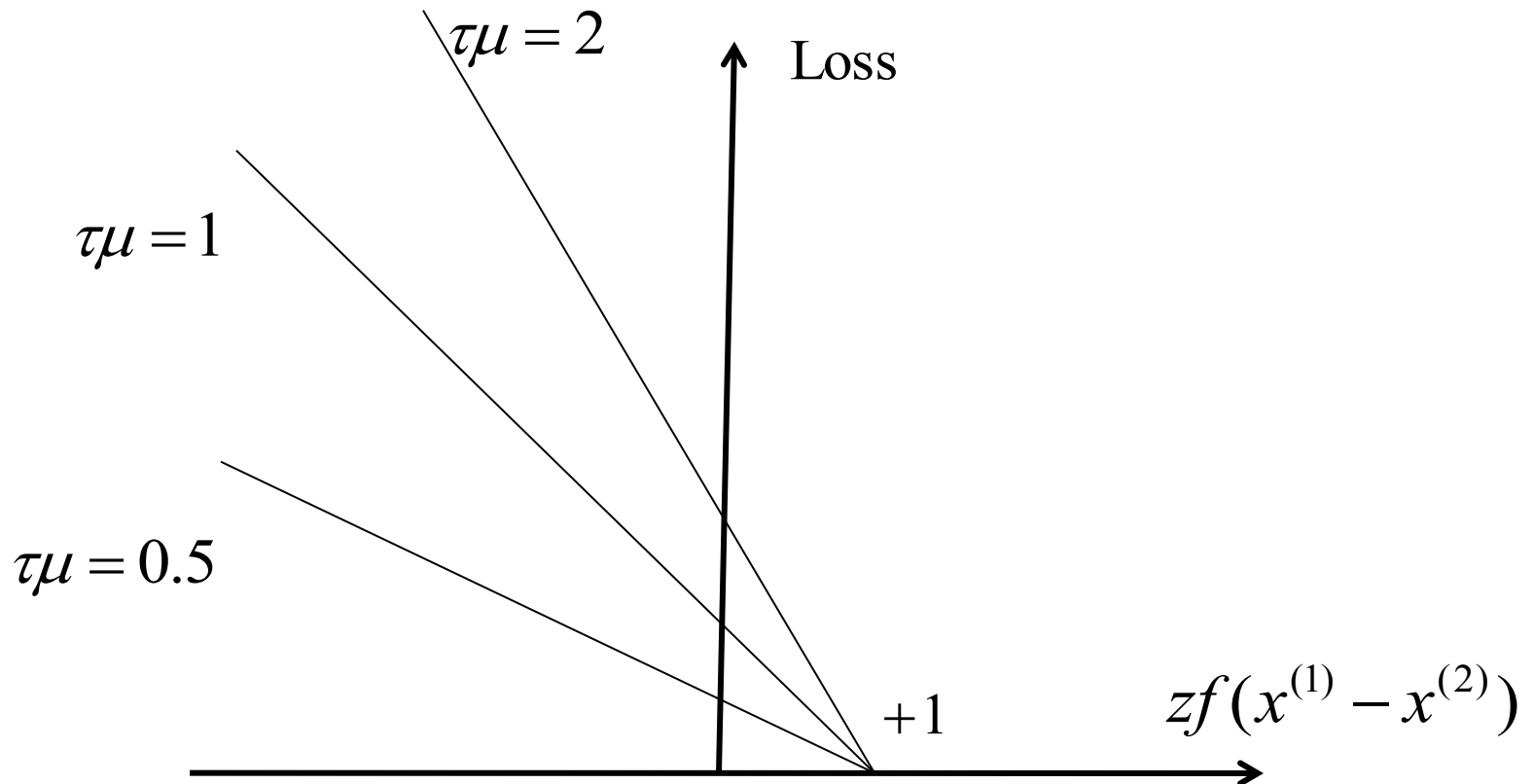
Ranking SVM is biased toward q2

IR SVM

- Solving the two problems of Ranking SVM
- Higher weight on important rank pairs $\tau_{k(i)}$
- Normalization weight on pairs in query $\mu_{q(i)}$
- IR SVM = Ranking SVM using modified hinge loss

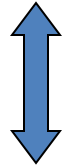
Modified Hinge Loss function

$$\min_w \sum_{i=1}^l \tau_{k(i)} \mu_{q(i)} \left[1 - z_i \langle w, x_i^{(1)} - x_i^{(2)} \rangle \right]_+ + \lambda \|w\|^2$$



Learning of IR SVM

$$\min_w \sum_{i=1}^l \tau_{k(i)} \mu_{q(i)} \left[1 - z_i \langle w, x_i^{(1)} - x_i^{(2)} \rangle \right]_+ + \lambda \|w\|^2$$



$$\min_{w, \xi} \frac{1}{2} \|w\|^2 + \sum_{i=1}^l C_i \xi_i$$

$$z_i \langle w, x_i^{(1)} - x_i^{(2)} \rangle \geq 1 - \xi_i \quad i = 1, \dots, l$$

$$\xi_i \geq 0$$

$$C_i = \frac{\tau_{k(i)} \mu_{q(i)}}{2\lambda}$$

3.4 Probabilistic Model for Ranking

Methods of Using Probabilistic Models

- ListNet
- ListMLE

ListNet and ListMLE

Plackett-Luce Model (Permutation Probability)

- Probability of permutation π is defined as

$$P(\pi) = \prod_{i=1}^n \frac{S_{\pi(i)}}{\sum_{j=i}^n S_{\pi(j)}}$$

- Example:

$$P(ABC) = \frac{S_A}{S_A + S_B + S_C} \cdot \frac{S_B}{S_B + S_C} \cdot \frac{S_C}{S_C}$$

P(A ranked No.1)

P(B ranked No.2 | A ranked No.1)

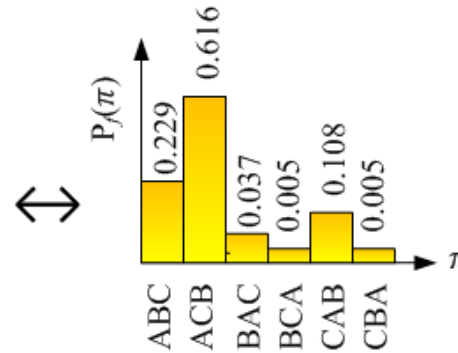
P(C ranked No.3 | A ranked No.1, B ranked No.2)

Properties of Plackett-Luce Model

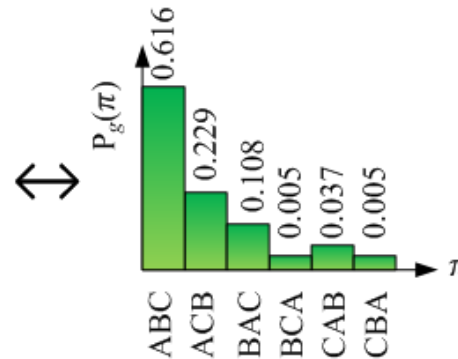
- Objects: ABC
- Scores: $s_A = 5, s_B = 3, s_C = 1$
- Property 1: $P(ABC)$ is largest, $P(CBA)$ is smallest
- Property 2: swap B and C in ABC, $P(ABC) > P(ACB)$

KL Divergence between Permutation Probability Distributions

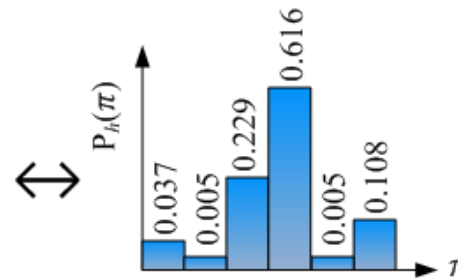
$f: f(A) = 3, f(B)=0, f(C)=1;$
 Ranking by f : ABC



$g: g(A) = 6, g(B)=4, g(C)=3;$
 Ranking by g : ABC



$h: h(A) = 4, h(B)=6, h(C)=3;$
 Ranking by h : ACB



ListNet

- Parameterized Plackett-Luce Model

$$s = \exp(f(x; w))$$

$$P(G(x_1 \cdots x_k)) = \prod_{i=1}^k \frac{s_{x_i}}{\sum_{j=i}^n s_{x_j}}$$

- Ranking Model: $f(x; w) = \text{Neural Net}$

ListNet (cont')

- Loss function = KL-divergence between two Top- k probability distributions from ground truth and ranking model

$$L(w) = -\sum_{q \in Q} \sum_{\pi \in \Omega^k} \left(\prod_{i=1}^k \frac{\exp(y_i)}{\sum_{j=i}^n \exp(y_j)} \right) \log \left(\prod_{i=1}^k \frac{\exp(f(x_i; w))}{\sum_{j=i}^n \exp(f(x_j; w))} \right)$$

- Algorithm = Gradient Descent

ListMLE

- Parameterized Plackett-Luce Model

$$s = \exp(f(x; w))$$

$$P(G(x_1 \cdots x_k)) = \prod_{i=1}^k \frac{S_{x_i}}{\sum_{j=i}^n S_{x_j}}$$

- Maximum Likelihood Estimation

$$L(w) = -\sum_{q \in Q} \log \left(\prod_{i=1}^k \frac{\exp(f(x_i; w))}{\sum_{j=i}^n \exp(f(x_j; w))} \right)$$

Plackett-Luce Model (Top-k Probability)

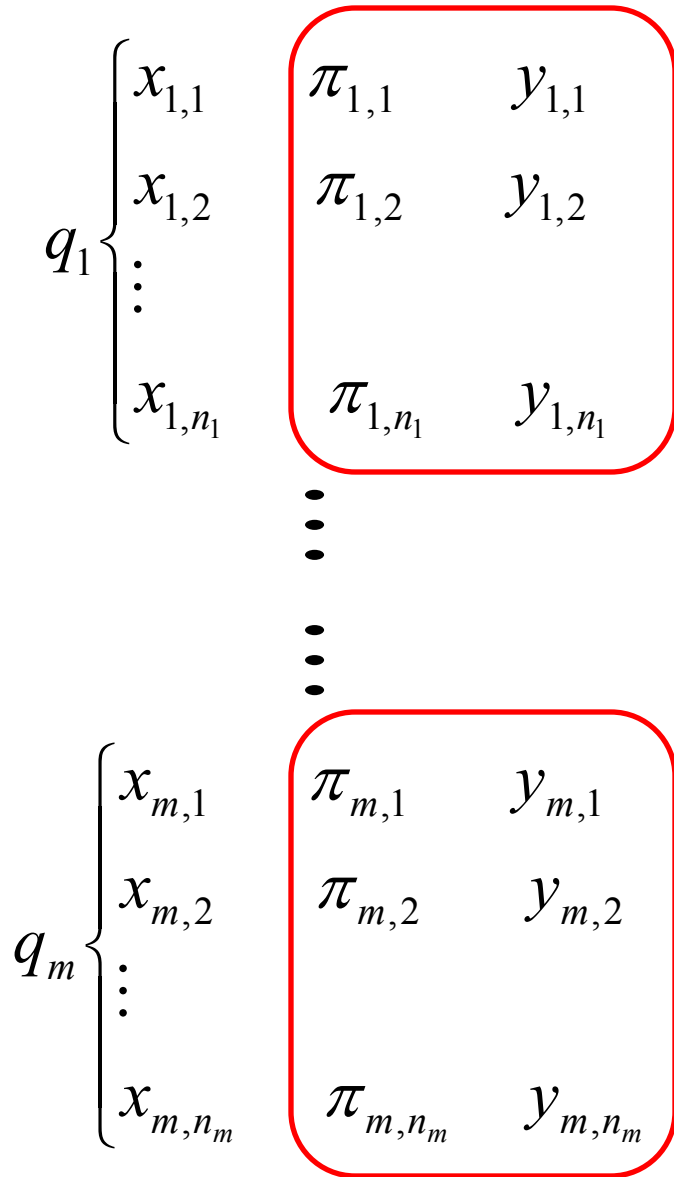
- Computation of permutation probabilities is intractable
- Top- k probability
 - Defining Top- k subgroup $G(o_1 \dots o_k)$ containing all permutations whose top- k objects are o_1, \dots, o_k
 - $$P(G(o_1 \dots o_k)) = \prod_{i=1}^k \frac{S_{o_i}}{\sum_{j=i}^n S_{o_j}}$$
 - Time complexity of computation : from $n!$ to $n!/(n-k)!$
- Example:
$$P(G(A)) = \frac{S_A}{S_A + S_B + S_C}$$

3.5 Direct Optimization of Evaluation Measures

Direction Optimization Methods

- AdaRank
- PermuRank
- SVM MAP

Listwise Loss



$$\max_{f \in \mathcal{F}} \sum_{i=1}^m E(\pi(q_i, \mathbf{d}_i, f), \mathbf{y}_i)$$



$$\min_{f \in \mathcal{F}} \sum_{i=1}^m (1 - E(\pi(q_i, \mathbf{d}_i, f), \mathbf{y}_i))$$

AdaRank, SVM-MAP, PermuRank

- Optimizing different upper bounds (surrogate loss functions)

$$\sum_{i=1}^m (1 - E(\pi(q_i, \mathbf{d}_i, f), \mathbf{y}_i))$$

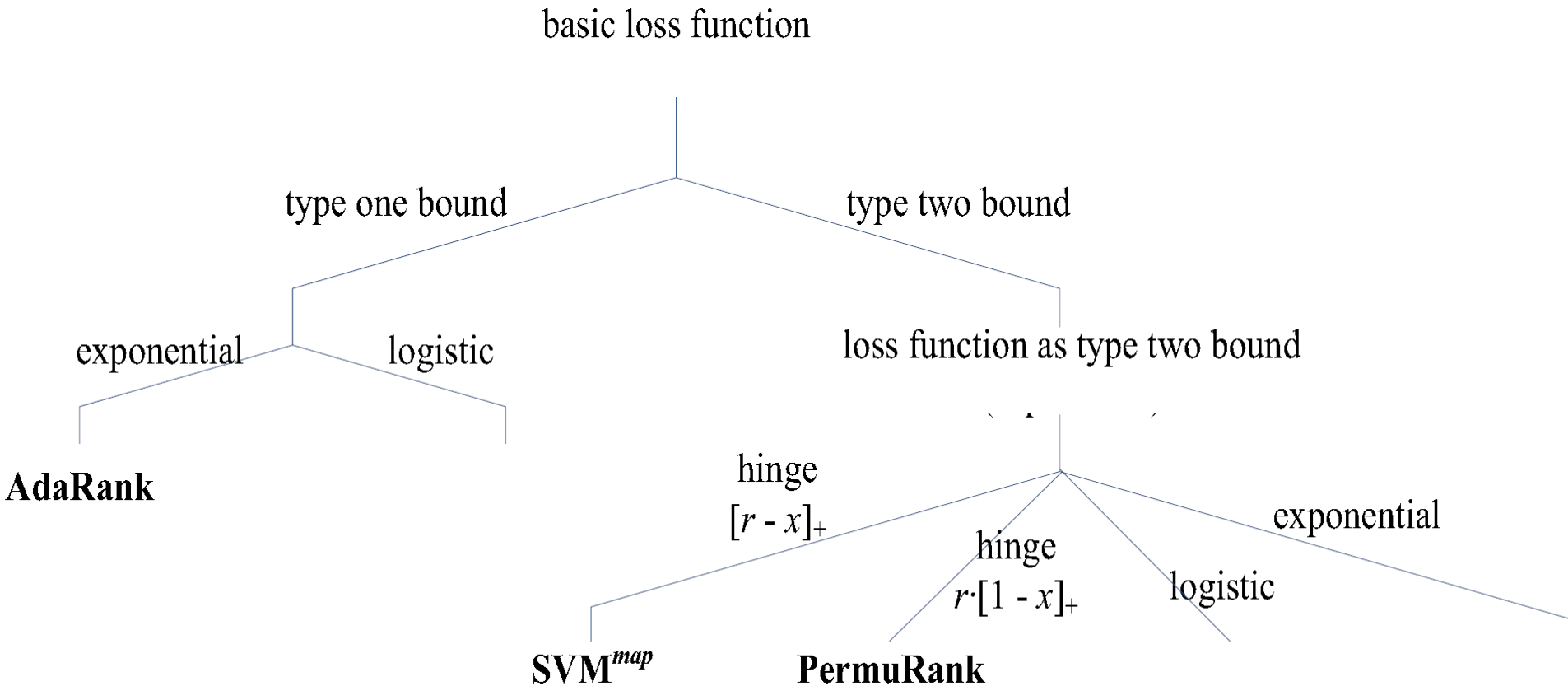
- Type One Upper Bound

$$\sum_{i=1}^m \exp\{-E(\pi_i, \mathbf{y}_i)\} \quad \sum_{i=1}^m \log_2(1 + e^{-E(\pi_i, \mathbf{y}_i)})$$

- Type Two Upper Bound

$$\sum_{i=1}^m \max_{\pi_i^* \in \Pi_i^*; \pi_i \in \Pi_i \setminus \Pi_i^*} ((E(\pi_i^*, \mathbf{y}_i) - E(\pi_i, \mathbf{y}_i)) \cdot \mathbb{I}[(F(q_i, \mathbf{d}_i, \pi_i^*) \leq F(q_i, \mathbf{d}_i, \pi_i))])$$

Relations between Upper Bounds



AdaRank

AdaRank

- Optimizing exponential loss function
- Algorithm: AdaBoost-like algorithm for ranking

Loss Function of AdaRank

$$\max_{f \in \mathcal{F}} \sum_{i=1}^m E(\pi(q_i, \mathbf{d}_i, f), \mathbf{y}_i)$$

Any evaluation measure taking value between $[-1, +1]$

$$\min_{f \in \mathcal{F}} \sum_{i=1}^m (1 - E(\pi(q_i, \mathbf{d}_i, f), \mathbf{y}_i))$$

$$\longleftarrow e^{-x} \geq 1 - x$$

$$\min_{f \in \mathcal{F}} \sum_{i=1}^m \exp\{-E(\pi(q_i, \mathbf{d}_i, f), \mathbf{y}_i)\}$$

$$\longleftarrow f(\vec{x}) = \sum_{t=1}^T \alpha_t h_t(\vec{x})$$

$$\min_{h_t \in \mathcal{H}, \alpha_t \in \mathbb{R}^+} L(h_t, \alpha_t) = \sum_{i=1}^m \exp\{-E(\pi(q_i, \mathbf{d}_i, f_{t-1} + \alpha_t h_t), \mathbf{y}_i)\}$$

AdaRank Algorithm

Input: $S = \{(q_i, \mathbf{d}_i, \mathbf{y}_i)\}_{i=1}^m$, and parameters E and T

Initialize $P_1(i) = 1/m$.

For $t = 1, \dots, T$

- Create weak ranker h_t with weighted distribution P_t on training data S .
- Choose α_t

$$\alpha_t = \frac{1}{2} \cdot \ln \frac{\sum_{i=1}^m P_t(i) \{1 + E(\pi(q_i, \mathbf{d}_i, h_t), \mathbf{y}_i)\}}{\sum_{i=1}^m P_t(i) \{1 - E(\pi(q_i, \mathbf{d}_i, h_t), \mathbf{y}_i)\}}.$$

- Create f_t

$$f_t(\vec{x}) = \sum_{k=1}^t \alpha_k h_k(\vec{x}).$$

- Update P_{t+1}

$$P_{t+1}(i) = \frac{\exp\{-E(\pi(q_i, \mathbf{d}_i, f_t), \mathbf{y}_i)\}}{\sum_{j=1}^m \exp\{-E(\pi(q_j, \mathbf{d}_j, f_t), \mathbf{y}_j)\}}.$$

End For

Output ranking model: $f(\vec{x}) = f_T(\vec{x})$.

Theoretical Results on AdaRank

- Training error will be continuously reduced during learning phase.

THEOREM 1. *The following bound holds on the ranking accuracy of the AdaRank algorithm on training data:*

$$\frac{1}{m} \sum_{i=1}^m E(\pi(q_i, \mathbf{d}_i, f_T), \mathbf{y}_i) \geq 1 - \prod_{t=1}^T e^{-\delta_{\min}^t} \sqrt{1 - \varphi(t)^2},$$

where $\varphi(t) = \sum_{i=1}^m P_t(i) E(\pi(q_i, \mathbf{d}_i, h_t), \mathbf{y}_i)$, $\delta_{\min}^t = \min_{i=1, \dots, m} \delta_i^t$, and

$$\delta_i^t = E(\pi(q_i, \mathbf{d}_i, f_{t-1} + \alpha_t h_t), \mathbf{y}_i) - E(\pi(q_i, \mathbf{d}_i, f_{t-1}), \mathbf{y}_i) - \alpha_t E(\pi(q_i, \mathbf{d}_i, h_t), \mathbf{y}_i),$$

for all $i = 1, 2, \dots, m$ and $t = 1, 2, \dots, T$.

SVM MAP

Global Ranking Function

$$\sigma_i = \arg \max_{\sigma \in \Pi_i} F(q_i, \mathbf{d}_i, \sigma).$$

$$F(q_i, \mathbf{d}_i, \pi_i) = \mathbf{w}^\top \Phi(q_i, \mathbf{d}_i, \pi_i),$$

$$\Phi(q_i, \mathbf{d}_i, \pi_i) = \frac{1}{n(q_i) \cdot (n(q_i) - 1)} \sum_{k, l, k < l} [z_{kl} (\phi(q_i, d_{ik}) - \phi(q_i, d_{il}))],$$

Equivalent to ranking with local ranking function (plus sorting)

$$f(q_i, d_{ij}) = \mathbf{w}^\top \phi(q_i, d_{ij})$$

Ranking with Global Function

$$f_A = w^T \phi_A, \quad f_B = w^T \phi_B, \quad f_C = w^T \phi_C$$

$$f_A > f_B > f_C$$

- **ABC** $F_{ABC} = \frac{1}{6}((f_A - f_B) + (f_B - f_C) + (f_A - f_C))$

- **ACB** $F_{ACB} = \frac{1}{6}((f_A - f_C) + (f_C - f_B) + (f_A - f_B))$

$$F_{ABC} > F_{ACB}$$

Type Two Bound

$$R(F) = \sum_{i=1}^m (E(\pi_i^*, y_i) - E(\pi_i, y_i)) = \sum_{i=1}^m (1 - E(\pi_i, y_i)),$$

$$\sum_{i=1}^m \max_{\pi_i^* \in \Pi_i^*; \pi_i \in \Pi_i \setminus \Pi_i^*} ((E(\pi_i^*, y_i) - E(\pi_i, y_i)) \cdot \mathbb{I}[(F(q_i, \mathbf{d}_i, \pi_i^*) \leq F(q_i, \mathbf{d}_i, \pi_i))]),$$

SVM MAP

$$\sum_{i=1}^m \left[\max_{\pi_i^* \in \Pi_i^*; \pi_i \in \Pi_i \setminus \Pi_i^*} ((E(\pi_i^*, y_i) - E(\pi_i, y_i)) - (F(q_i, \mathbf{d}_i, \pi_i^*) - F(q_i, \mathbf{d}_i, \pi_i))) \right]_+ + \lambda \|\vec{w}\|^2 .$$

$$\min_{\vec{w}; \xi \geq 0} \frac{1}{2} \|\vec{w}\|^2 + \frac{C}{m} \sum_{i=1}^m \xi_i$$

$$s.t. \quad \forall i, \forall \pi_i^* \in \Pi_i^*, \forall \pi_i \in \Pi_i \setminus \Pi_i^* :$$

$$F(q_i, \mathbf{d}_i, \pi_i^*) - F(q_i, \mathbf{d}_i, \pi_i) \geq E(\pi_i^*, y_i) - E(\pi_i, y_i) - \xi_i,$$

3.6 Approximation of Evaluation Measures

Method based on Approximation of Evaluation Measure

- SoftRank
- LambdaRank

SoftRank

SoftRank

- Evaluation measures are not smooth, due to use of sorting
- Probabilistically approximate evaluation measures (Soft NDCG)
- Model: Neural Net
- Algorithm: Gradient Descent

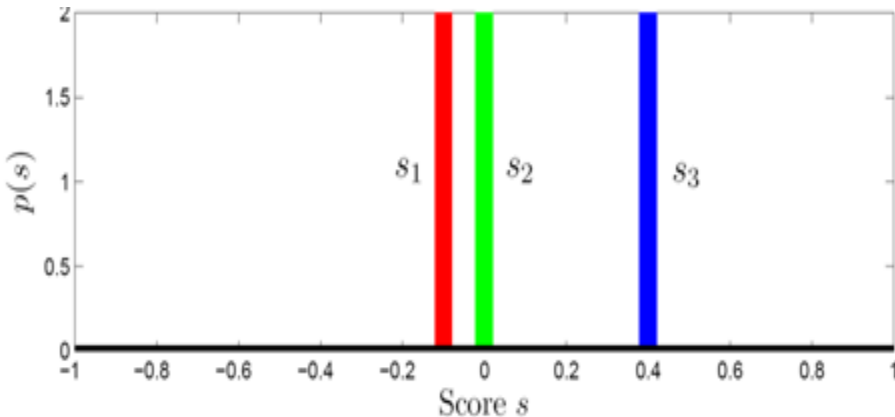
SoftRank Algorithm

- Calculate score distributions of documents
- Calculate position distributions of documents
- Compute SoftNDCG
- Optimize SoftNDCG by Gradient Descent

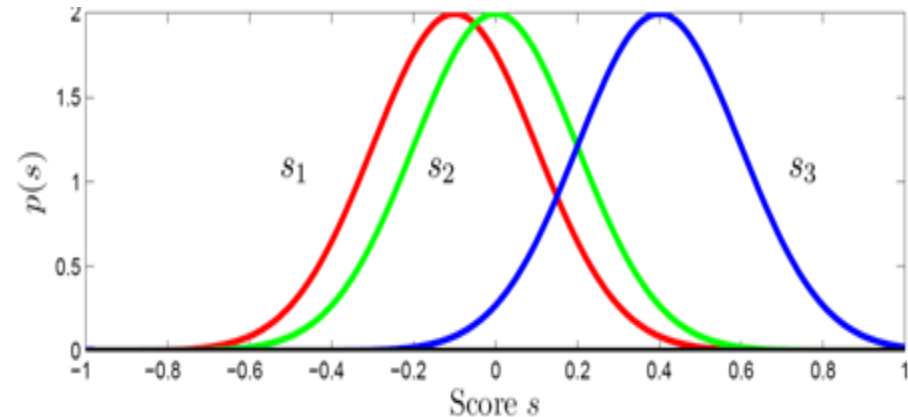
Score Distribution of Document

- Assuming that score of document s_j follows Gaussian distribution

$$p(s_j) = N(s_j | f(x_j), \sigma_s^2)$$



Deterministic Score



Probabilistic Score

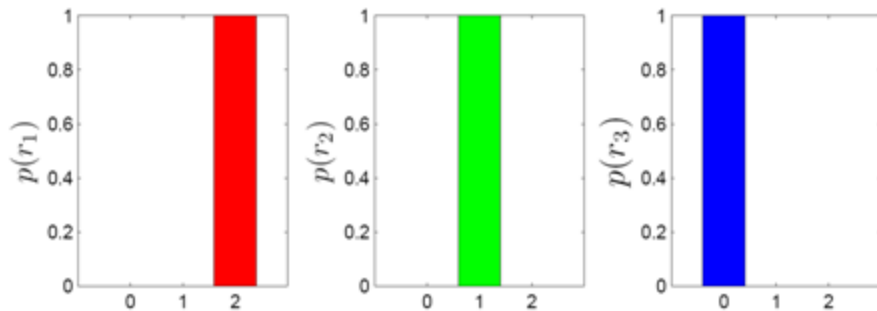
Position Distribution of Document

- Probability of document i being ranked before document j

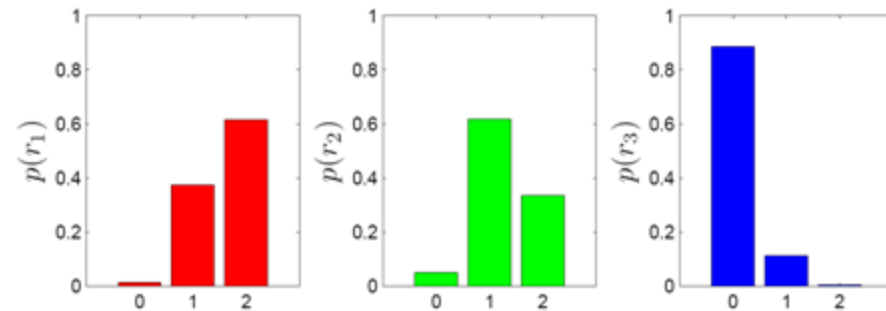
$$\pi_{ij} = \int_0^{\infty} N(s | f(x_i) - f(x_j), 2\sigma^2) ds$$

- Position distribution of document (recursive definition)

$$p_j^{(i)}(r) = p_j^{(i-1)}(r-1)\pi_{ij} + p_j^{(i-1)}(r)(1-\pi_{ij})$$



Deterministic Position Distribution



Probabilistic Position Distribution

Soft NDCG

- Re-writing NDCG as document (feature vector) indexed

$$G = G_{max}^{-1} \sum_{j=1}^N g(j) D(r_j).$$

- Only position discount is affected by ranking model
- Assume that positions of document are probabilistically determined by ranking model, rather than deterministically

Soft NDCG (cont')

- Soft NDCG

$$\mathcal{G} = G_{max}^{-1} \sum_{j=1}^N g(j) E[D(r_j)].$$

$$\mathcal{G} = G_{max}^{-1} \sum_{j=1}^N g(j) \sum_{r=0}^{N-1} D(r) p_j(r)$$

- Only need to calculate probabilities of positions of document $p_j(r)$

3.7 Evaluation Results

LETOR Data Set

- Available at
 - <http://research.microsoft.com/~letor/>
- Data Corpora: TREC, OHSUMED
- Training/Validation/Test split
- Standard IR Features

Evaluation Results

- Pairwise approach and listwise approach perform better than pointwise approach
- Listwise approach performs better than pairwise approach in most cases
- Listwise approach
 - ListMLE, ListNet, AdaRank, PermuRank, SVM-MAP
- Pairwise approach
 - Ranking SVM, RankNet, RankBoost
- Pointwise approach
 - Linear Regression

4. Learning to Rank Theory

Learning to Rank Theory

- 4.1 Generalization Analysis of Pairwise Methods
- 4.2 Generalization Analysis of Listwise Methods

Learning to Rank Theory

- Pairwise Approach
 - Generalization Analysis [Lan et al 2008]
- Listwise Approach
 - Generalization Analysis [Lan et al 2009]
 - Consistency Analysis [Xia et al 2008]

4.1 Generalization Analysis of Pairwise Methods

Pairwise Learning Framework (Query Level)

- Data is represented as $(z^{(q)}, y^{(q)})$, where $z^{(q)}$ is pair of feature vectors $(x_1^{(q)}, x_2^{(q)})$ and $y^{(q)}$ is ground-truth on their order, w.r.t. query q
- (z, y) are random variables according to distribution $P(\cdot, \cdot)$
- Training Data: $S = (q_1, S_1) \cdots (q_m, S_m)$
 $S_i = \{(z_1^{(i)}, y_1^{(i)}), \dots, (z_{n_i}^{(i)}, y_{n_i}^{(i)})\}, i = 1, \dots, m$

- Expected Risk:

$$R_l(f) = \int_Q L(f, q) P_Q(dq) \quad L(f, q) = \int_{X^2 \times Y} l(f; z^{(q)}, y^{(q)}) D_q(dz^{(q)}, dy^{(q)})$$

- Empirical Risk:

$$\hat{R}_l(f; S) = \frac{1}{m} \sum_{i=1}^m \hat{L}(f; q_i) \quad \hat{L}(f; q_i) = \frac{1}{n_i} \sum_{j=1}^{n_i} l(f; z_j^{(i)}, y_j^{(i)})$$

Generalization Analysis

- Goal = to minimize expected risk $R_l(f)$
- Distribution is unknown we instead minimize empirical risk $\hat{R}_l(f; S)$
- Generalization analysis is concerned with upper bound of difference between expected and empirical risks

Generalization Analysis Using Stability

- With probability at least $1 - \delta$

$$R_l(f) \leq \hat{R}_l(f; S) + 2\tau(m) + (4m\tau(m) + B) \sqrt{\frac{\ln 1/\delta}{2m}}$$

- The bound is related to number of training queries m , and stability of algorithm
- If $\tau(m)$ goes to 0 very fast when m approaches infinity, then the bound will be tight.

Stability of Ranking SVM and IRSVM

- Ranking SVM

$$\tau(m) = \frac{4\kappa^2}{\lambda m} \frac{1 + \frac{\sigma}{\mu\sqrt{\delta/m}}}{1 - \frac{\varepsilon}{\mu}} = O\left(\frac{1}{\sqrt{m}}\right)$$

- IR SVM

$$\tau(m) = \frac{4\kappa^2}{\lambda m} = O\left(\frac{1}{m}\right)$$

- IR SVM > Ranking SVM

4.2 Generalization Analysis of Listwise Methods

Listwise Learning Framework

- Data is represented as (z, y) , where z is feature vector set $z = (x_1, \dots, x_n)$ and y is ground-truth permutation
- (z, y) are random variables according to distribution $P(\cdot, \cdot)$
- Training Data: $(z_1, y_1), \dots, (z_m, y_m)$

- Expected Risk:

$$R_l(f) = \int_{Z \times Y} l(f; z, y) P(dz, dy)$$

- Empirical Risk:

$$R_l(f; S) = \frac{1}{m} \sum_{i=1}^m l(f; z_i, y_i)$$

Generalization Analysis

- Goal = to minimize expected risk $R_{l_A}(f)$
- Distribution is unknown we instead minimize empirical risk $\hat{R}_{l_A}(f; S)$
- Generalization analysis is concerned with upper bound of difference between expected and empirical risks

$$\sup(R_{l_A}(f) - \hat{R}_{l_A}(f; S))$$

Generalization Analysis Using Rademacher Complexity

- With probability at least $1 - \delta$

$$\sup(R_{l_A}(f) - \hat{R}_{l_A}(f; S)) \leq \frac{4BM}{\sqrt{m}} C_A(\phi) N(\phi) + \sqrt{\frac{2 \ln 2 / \delta}{m}}$$

- The bound is related to:
 - $C_A(\phi)$, algorithm-dependent factor, determined by loss function and transformation function ϕ
 - $N(\phi)$, algorithm-independent factor, only determined by transformation function ϕ
 - when n approaches infinity, generalization bound vanishes at rate of $O\left(\frac{1}{\sqrt{m}}\right)$.

Generalization Analysis Using Rademacher Complexity (cont')

- ListMLE

$$C_{ListMLE}(\phi) = \frac{2}{\phi(-BM)(\log n + \log \frac{\phi(BM)}{\phi(-BM)})}$$

- ListNet

$$C_{ListNet}(\phi) = \frac{2n!}{\phi(-BM)(\log n + \log \frac{\phi(BM)}{\phi(-BM)})}$$

- ListMLE > ListNet

5. Learning to Rank Applications

Learning to Rank Applications

- Search [Burgess et al 2005]
- Recommender System [Freund et al 2003]
- Key Phrase Extraction [Jiang et al 2009]

Recommender System (Collaborative Filtering)

- Problem formulation
 - Input: users' ratings on some items
 - Output: users' ratings on other items
 - Assumption: users sharing same ratings on input items tend to agree on new items
- Solutions
 - Classification
 - Ordinal Regression
 - Learning to Rank

Recommender System

	Item1	Item2	Item3	...	
User1	5	4			
User2	1		2		2
...		?	?	?	
UserM	4	3			

Recommender System Using RankBoost

- Ranking items according to users
- Justification: users tend to rate on different scales
- Method: RankBoost
- Result: RankBoost > Nearest Neighbor

Key Phrase Extraction

- Problem formulation
 - Input: document
 - Output: keyphrases of document
 - Two steps: phrase extraction and keyphrase identification
- Traditional approach
 - Classification: keyphrase vs non-keyphrase

Key Phrase Extraction Using Ranking SVM

- Ranking of phrases as keyphrases
- Justification: keyphrase or non-keyphrase is relative
- Method: Ranking SVM
- Result: Ranking SVM > SVM

6. Future Directions of Learning to Rank Research

New Issues to be Further Studied

- Learning from implicit data
 - Automatically generate labeled data from implicit feedback
- Model (feature) learning
 - Automatically learn features such as BM25
- Global ranking
 - Using features of current document as well as relations with other documents

New Issues to be Further Studied (cont')

- Query-dependent ranking
 - Creating different ranking models for different queries (in search)
- New applications
 - Machine Translation, etc

7. Summary

Content of Tutorial

- Introduction
- Learning to Rank Problem
- Learning to Rank Methods
- Learning to Rank Theory
- Learning to Rank Applications
- Future Directions of Learning to Rank Research

Takeaway Message

- Learning to Rank = branch of Machine Learning
- Learning to Rank = learning for ranking objects given subject
- Learning to Rank is different from ordinal regression
- Learning to Rank has been successfully applied to search
- Existing approaches: pointwise, pairwise, listwise

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