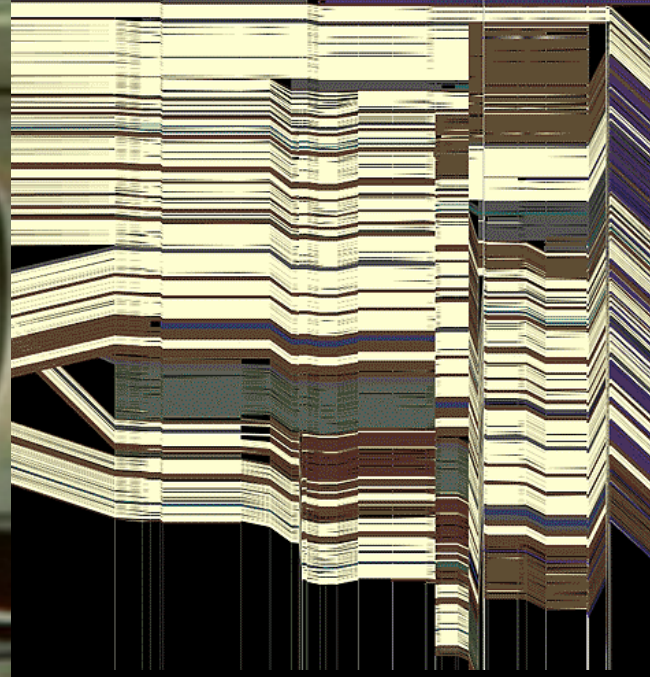
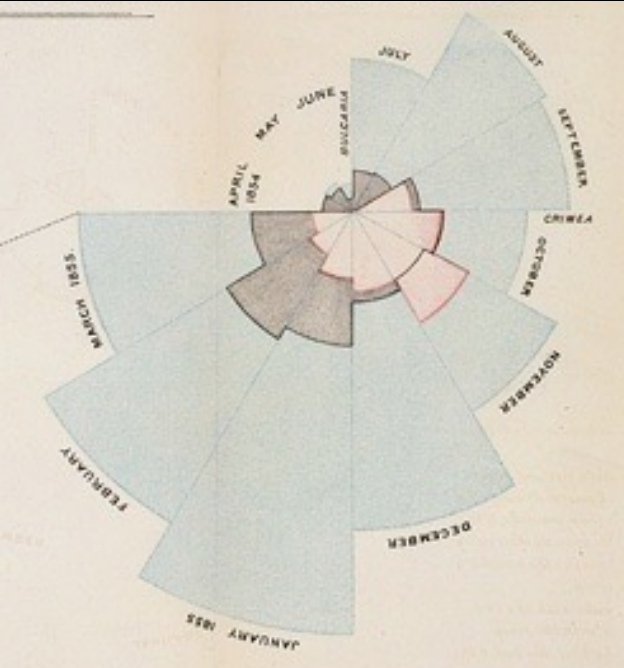


CSE 512 - Data Visualization

# Data and Image Models



Jeffrey Heer University of Washington

# Last Time: Value of Visualization

# The Value of Visualization

## **Record** information

Blueprints, photographs, seismographs, ...

## **Analyze** data to support reasoning

Develop and assess hypotheses

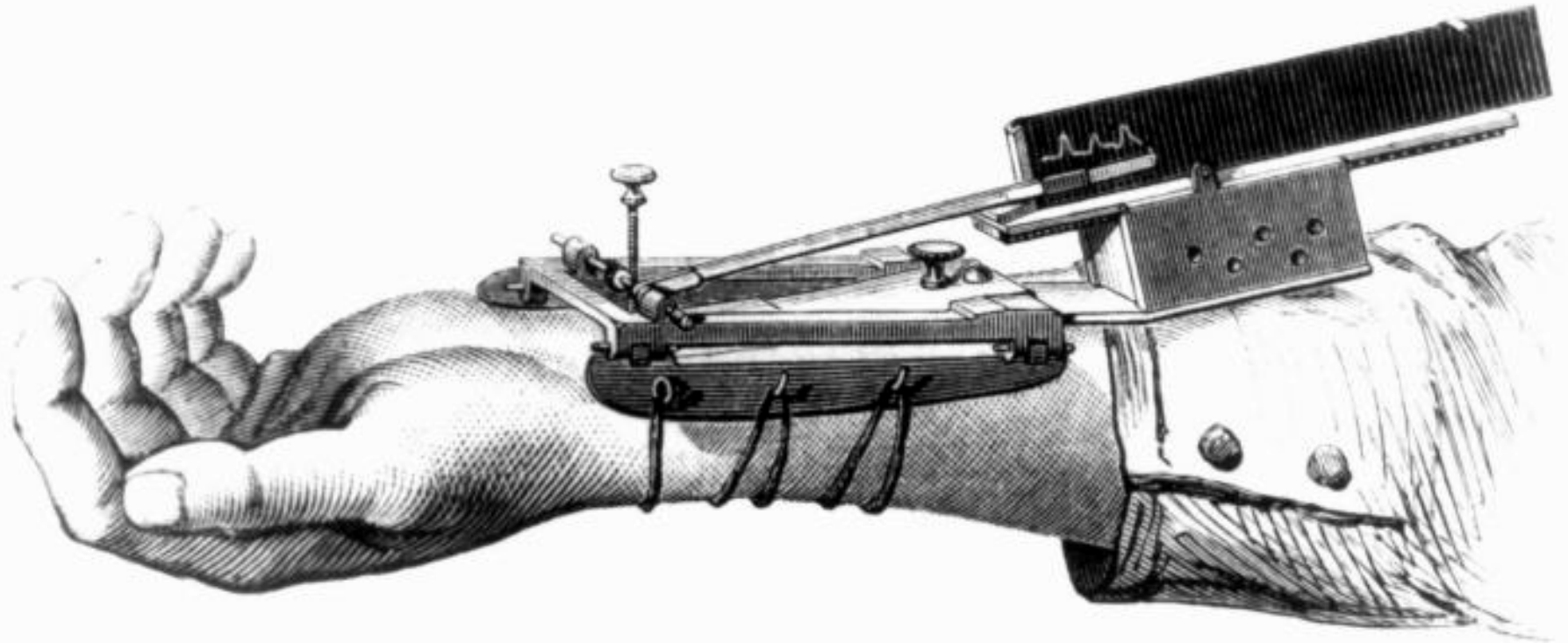
Find patterns / Discover errors in data

Expand memory

## **Communicate** information to others

Share and persuade

Collaborate and revise



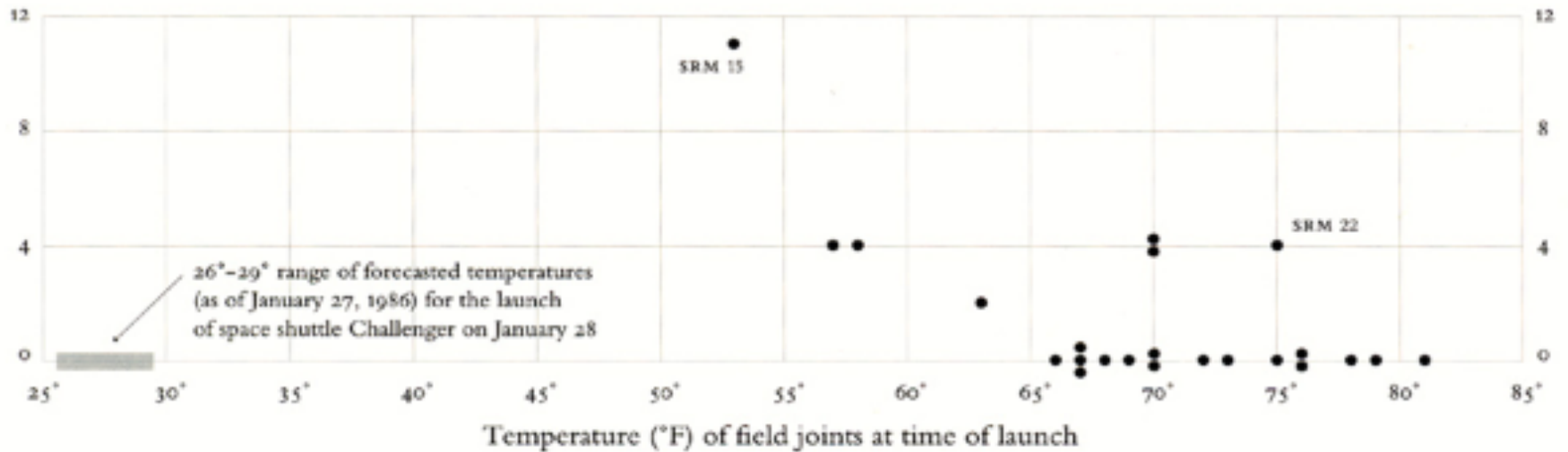
1.

Marey's **sphygmograph** in use,  
1860. *La méthode graphique dans  
les sciences expérimentales et  
principalement en physiologie et en  
médecine.*

E.J. Marey's sphygmograph [from Braun 83]

# Make a Decision: Challenger

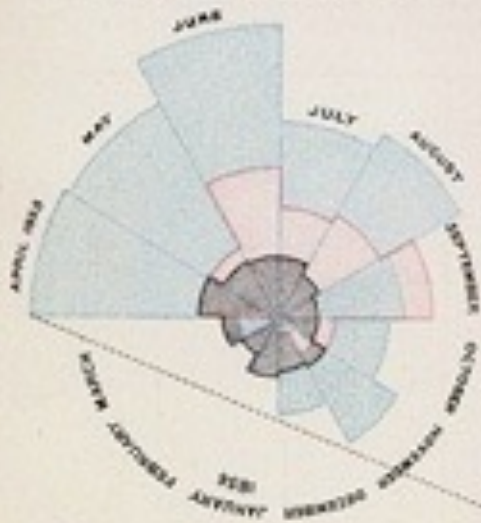
O-ring damage index, each launch



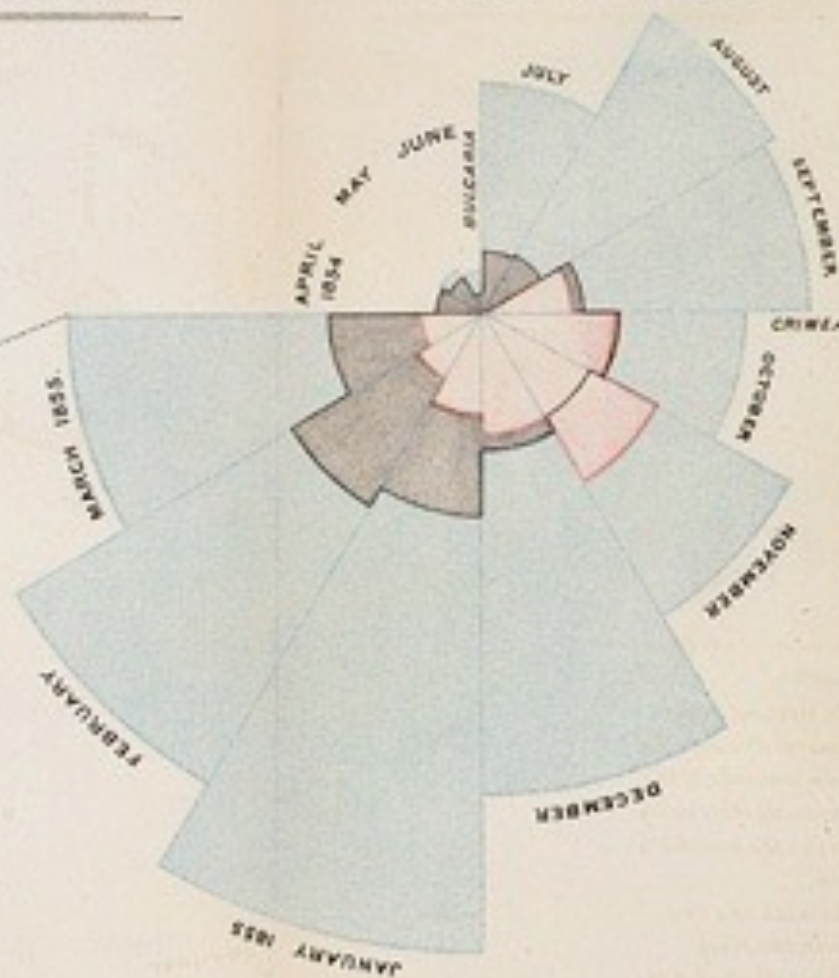
Visualizations drawn by Tufte show how low temperatures damage O-rings [Tufte 97]

DIAGRAM OF THE CAUSES OF MORTALITY  
IN THE ARMY IN THE EAST.

2.  
APRIL 1855 TO MARCH 1856.



1.  
APRIL 1854 TO MARCH 1855.

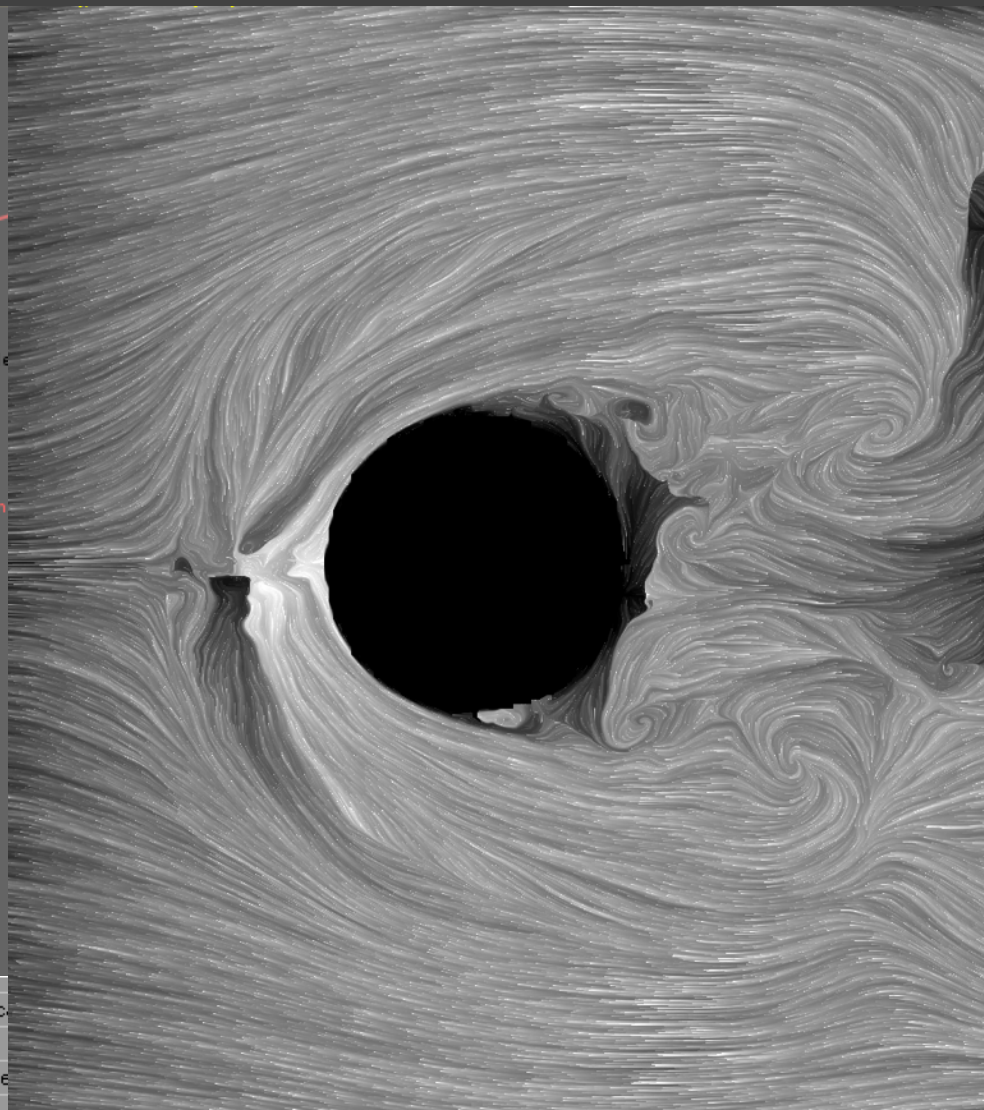
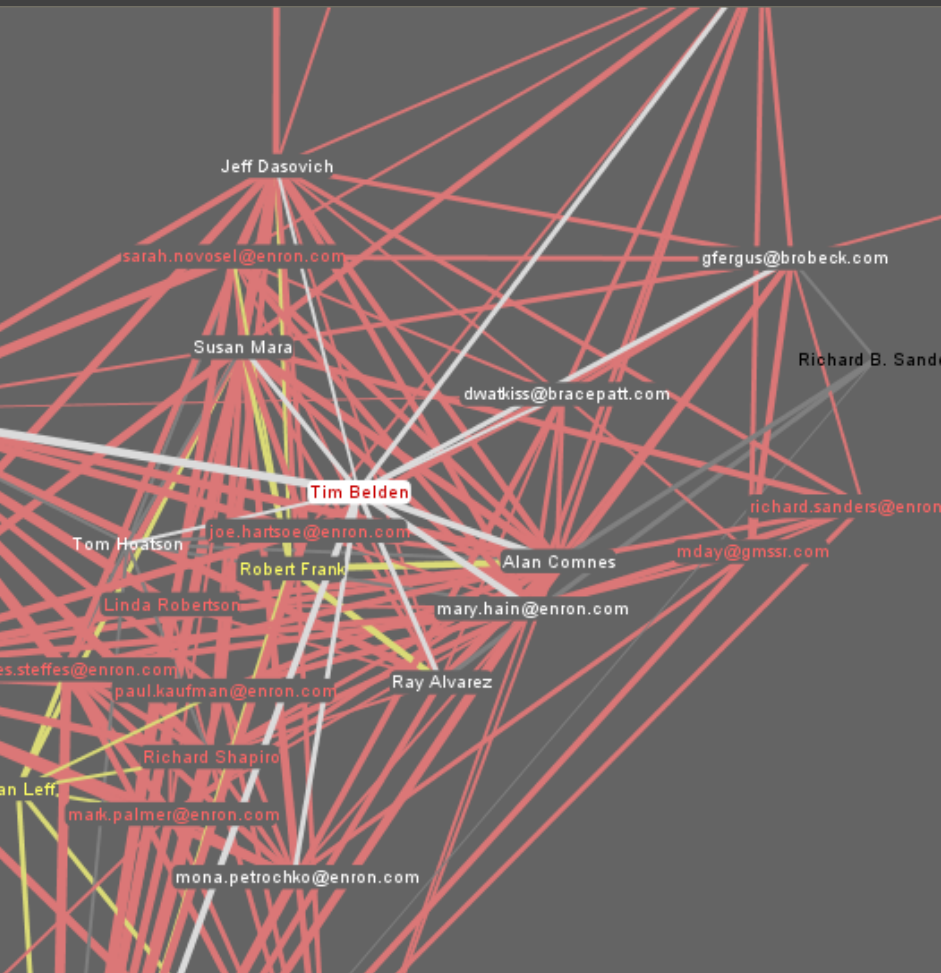


“to affect thro’ the Eyes  
what we fail to convey to  
the public through their  
word-proof ears”

1856 “Coxcomb” of Crimean War Deaths, Florence Nightingale



# InfoVis vs. SciVis?



# Informative vs. Aesthetic?

## wind map

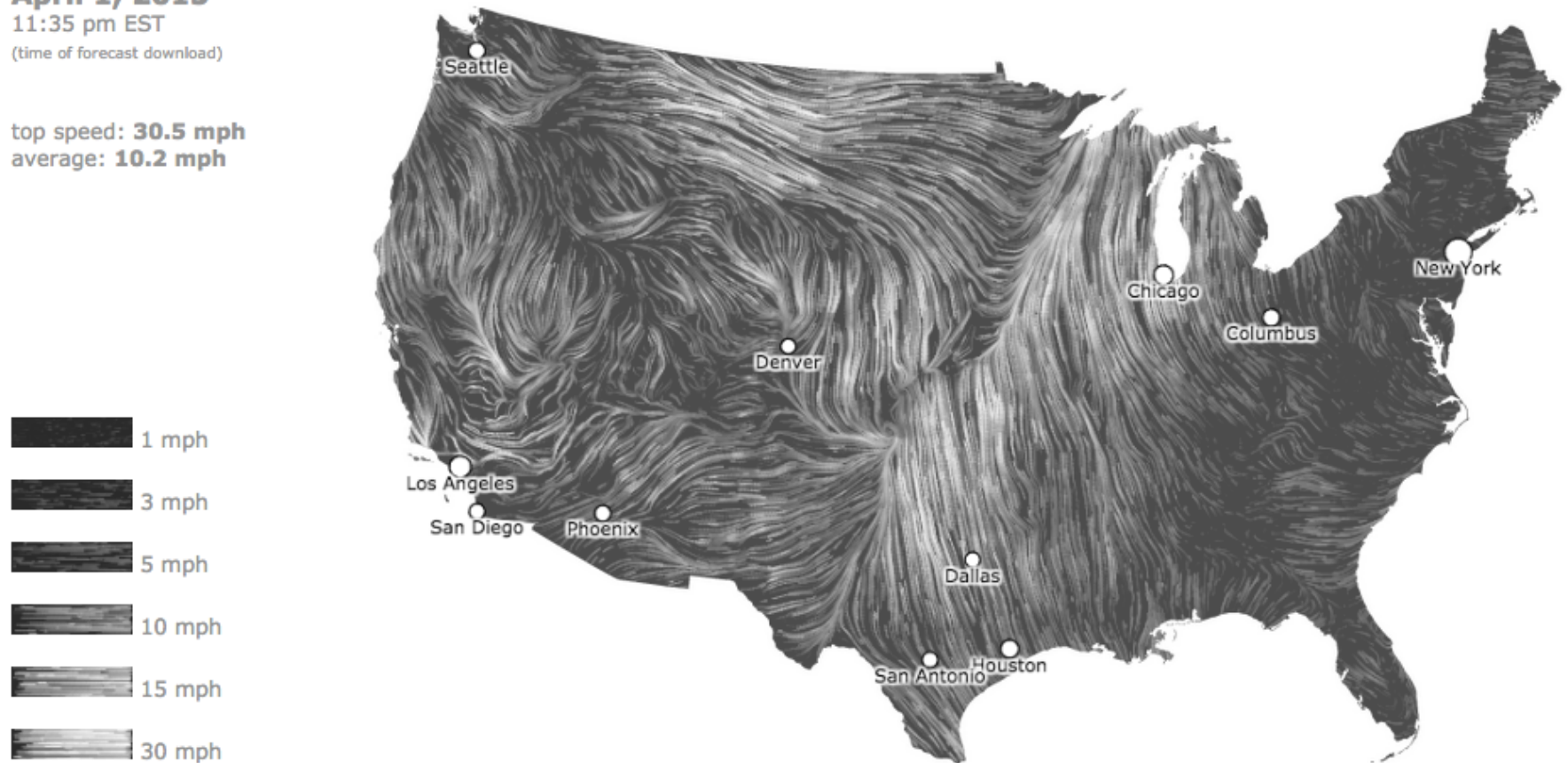
**April 1, 2015**

11:35 pm EST

(time of forecast download)

top speed: **30.5 mph**

average: **10.2 mph**





# Data & Image Models

# The Big Picture

## task

questions, goals  
assumptions

## data

physical data type  
conceptual data type

## domain

metadata  
semantics  
conventions

processing  
algorithms

mapping  
visual encoding

## image

visual channel  
graphical marks



# Topics

Properties of Data

Properties of Images

Mapping Data to Images

**Data**

# Data Models / Conceptual Models

**Data models** are formal descriptions

Math: sets with operations on them

Example: integers with + and x operators

**Conceptual models** are mental constructions

Include semantics and support reasoning

**Examples** (data vs. conceptual)

1D floats vs. temperatures

3D vector of floats vs. spatial location



# Taxonomy of Data Types (?)

1D (sets and sequences)

Temporal

2D (maps)

3D (shapes)

nD (relational)

Trees (hierarchies)

Networks (graphs)

Are there others?

The eyes have it: A task by data type taxonomy for information visualization  
[Shneiderman 96]

# Nominal, Ordinal & Quantitative

# Nominal, Ordinal & Quantitative

N - Nominal (labels or categories)

- Fruits: apples, oranges, ...

# Nominal, Ordinal & Quantitative

N - Nominal (labels or categories)

- Fruits: apples, oranges, ...

O - Ordered

- Quality of meat: Grade A, AA, AAA

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Q - Interval (location of zero arbitrary)

- Dates: Jan, 19, 2006; Location: (LAT 33.98, LONG -118.45)
- Only differences (i.e. intervals) may be compared



# Nominal, Ordinal & Quantitative

N - Nominal (labels or categories)

- Fruits: apples, oranges, ...

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- Quality of meat: Grade A, AA, AAA

Q - Interval (location of zero arbitrary)

- Dates: Jan, 19, 2006; Location: (LAT 33.98, LONG -118.45)
- Only differences (i.e. intervals) may be compared

Q - Ratio (zero fixed)

- Physical measurement: Length, Mass, Temp, ...
- Counts and amounts

# Nominal, Ordinal & Quantitative

N - Nominal (labels or categories)

- Operations: =, ≠

O - Ordered

- Operations: =, ≠, <, >

Q - Interval (location of zero arbitrary)

- Operations: =, ≠, <, >, -
- Can measure distances or spans

Q - Ratio (zero fixed)

- Operations: =, ≠, <, >, -, %
- Can measure ratios or proportions

# From Data Model to N, O, Q

## Data Model

32.5, 54.0, -17.3, ...

Floating point numbers

## Conceptual Model

Temperature (°C)

## Data Type

Burned vs. Not-Burned (N)

Hot, Warm, Cold (O)

Temperature Value (Q)

Microsoft Excel - fischer.iris.2.xls

File Edit View Insert Format Tools Data Window Help Type a question for help

A1 ID

	A	B	C	D	E	F	G	H	I	J
1	ID	Case	Species_No	Species	Organ	Width	Length			
2	1	1	1	I. Setosa	Petal	2	14			
3	2	1	3	I. Verginica	Petal	24	56			
4	3	1	2	I. Versicolor	Petal	13	45			
5	4	1	1	I. Setosa	Sepal	33	50			
6	5	1	3	I. Verginica	Sepal	31	67			
7	6	1	2	I. Versicolor	Sepal	28	57			
8	7	2	1	I. Setosa	Petal	2	10			
9	8	2	3	I. Verginica	Petal	23	51			
10	9	2	2	I. Versicolor	Petal	16	47			
11	10	2	1	I. Setosa	Sepal	36	46			
12	11	2	3	I. Verginica	Sepal	31	69			
13	12	2	2	I. Versicolor	Sepal	33	63			
14	13	3	1	I. Setosa	Petal	2	16			
15	14	3	3	I. Verginica	Petal	20	52			
16	15	3	2	I. Versicolor	Petal	14	47			
17	16	3	1	I. Setosa	Sepal	31	48			
18	17	3	3	I. Verginica	Sepal	30	65			
19	18	3	2	I. Versicolor	Sepal	32	70			
20	19	4	1	I. Setosa	Petal	1	14			
21	20	4	3	I. Verginica	Petal	19	51			
22	21	4	2	I. Versicolor	Petal	12	40			
23	22	4	1	I. Setosa	Sepal	36	49			
24	23	4	3	I. Verginica	Sepal	27	58			
25	24	4	2	I. Versicolor	Sepal	26	58			
26	25	5	1	I. Setosa	Petal	2	13			
27	26	5	3	I. Verginica	Petal	17	45			
28	27	5	2	I. Versicolor	Petal	10	33			
29	28	5	1	I. Setosa	Sepal	32	44			
30	29	5	3	I. Verginica	Sepal	25	49			
31	30	5	2	I. Versicolor	Sepal	23	50			
32	31	6	1	I. Setosa	Petal	2	16			

fischer.iris

Ready

Sepal and petal lengths and widths for three species of iris [Fisher 1936].

Microsoft Excel - fischer.iris.2.colored.xls

File Edit View Insert Format Tools Data Window Help

Type a question for help

H270 fx

	A	B	C	D	E	F	G	H	I	J
1	ID	Case	Species_No	Species	Organ	Width	Length			
2	1	1	1	I. Setosa	Petal	2	14			
3	2	1	3	I. Verginica	Petal	24	56			
4	3	1	2	I. Versicolor	Petal	13	45			
5	4	1	1	I. Setosa	Sepal	33	50			
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10	9	2	2	I. Versicolor	Petal	16	47			
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28	27	5	2	I. Versicolor	Petal	10	33			
29	28	5	1	I. Setosa	Sepal	32	44			
30	29	5	3	I. Verginica	Sepal	25	49			
31	30	5	2	I. Versicolor	Sepal	23	50			
32	31	6	1	I. Setosa	Petal	2	16			

fischer.iris

Ready

N  
O  
Q



# Dimensions & Measures

**Dimensions** (~ independent variables)

Discrete variables describing data (N, O)

Categories, dates, binned quantities

**Measures** (~ dependent variables)

Data values that can be aggregated (Q)

Numbers to be analyzed

Aggregate as sum, count, avg, std. dev...

# Example: U.S. Census Data

# Example: U.S. Census Data

**People Count:** # of people in group

**Year:** 1850 - 2000 (every decade)

**Age:** 0 - 90+

**Sex:** Male, Female

**Marital Status:** Single, Married, Divorced, ...

# Example: U.S. Census

People Count

Year

Age

Sex

Marital Status

2,348 data points

	A	B	C	D	E
1	year	age	marst	sex	people
2	1850	0	0	1	1483789
3	1850	0	0	2	1450376
4	1850	5	0	1	1411067
5	1850	5	0	2	1359668
6	1850	10	0	1	1260099
7	1850	10	0	2	1216114
8	1850	15	0	1	1077133
9	1850	15	0	2	1110619
10	1850	20	0	1	1017281
11	1850	20	0	2	1003841
12	1850	25	0	1	862547
13	1850	25	0	2	799482
14	1850	30	0	1	730638
15	1850	30	0	2	639636
16	1850	35	0	1	588487
17	1850	35	0	2	505012
18	1850	40	0	1	475911
19	1850	40	0	2	428185
20	1850	45	0	1	384211
21	1850	45	0	2	341254
22	1850	50	0	1	321343
23	1850	50	0	2	286580
24	1850	55	0	1	194080
25	1850	55	0	2	187208
26	1850	60	0	1	174976
27	1850	60	0	2	162236
28	1850	65	0	1	106827
29	1850	65	0	2	105534
30	1850	70	0	1	73677
31	1850	70	0	2	71762
32	1850	75	0	1	40834
33	1850	75	0	2	40229
34	1850	80	0	1	23449
35	1850	80	0	2	22949
36	1850	85	0	1	8186
37	1850	85	0	2	10511
38	1850	90	0	1	5259
39	1850	90	0	2	6569
40	1860	0	0	1	2120846
41	1860	0	0	2	2092162

# Census: N, O, Q?

People Count

Q-Ratio

Year

Q-Interval (O)

Age

Q-Ratio (O)

Sex

N

Marital Status

N

# Census: Dimension or Measure?

**People Count**

Measure

**Year**

Dimension

**Age**

Depends!

**Sex**

Dimension

**Marital Status**

Dimension

# Data Transformation

# Relational Data Model

Represent data as a **table** (*relation*)

Each **row** (*tuple*) represents a record

Each record is a fixed-length tuple

Each **column** (*attribute*) represents a variable

Each attribute has a *name* and a *data type*

A table's **schema** is the set of names and types

A **database** is a collection of tables (relations)



# Relational Algebra [Codd '70]

Data Transformations (sql)

Projection (`select`) - selects columns

Selection (`where`) - filters rows

Sorting (`order by`)


Aggregation (`group by, sum, min, max, ...`)

Combine relations (`union, join, ...`)

# Roll-Up and Drill-Down

Want to examine marital status in each decade?

**Roll-up** the data along the desired dimensions



The diagram consists of two horizontal curly braces. The first brace is positioned above the words 'year, marst,' in the 'GROUP BY' clause and is labeled 'Dimensions' above it. The second brace is positioned above the 'sum(people)' expression in the 'SELECT' clause and is labeled 'Measure' above it.

```
SELECT year, marst, sum(people)
FROM census
GROUP BY year, marst;
```

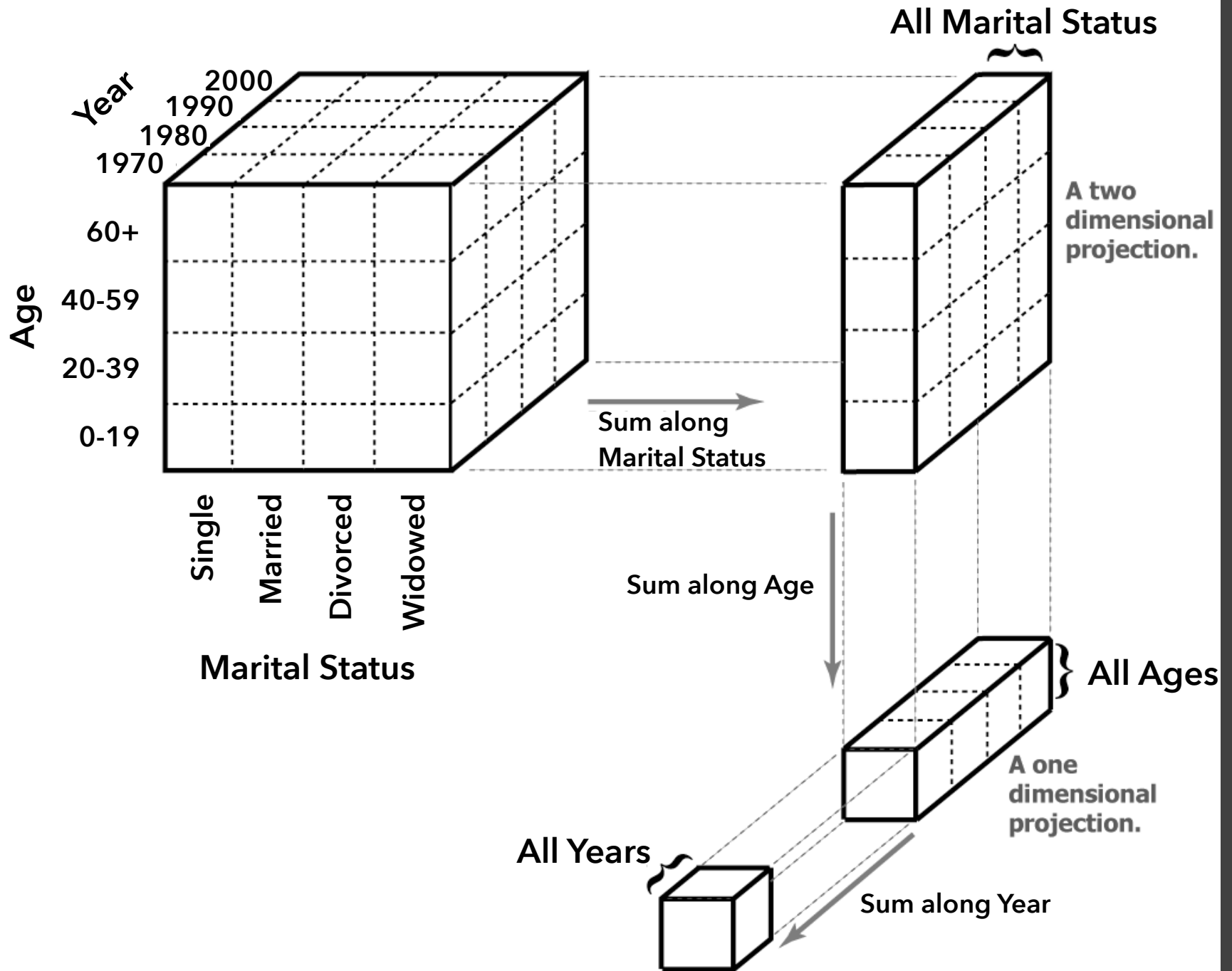
Dimensions

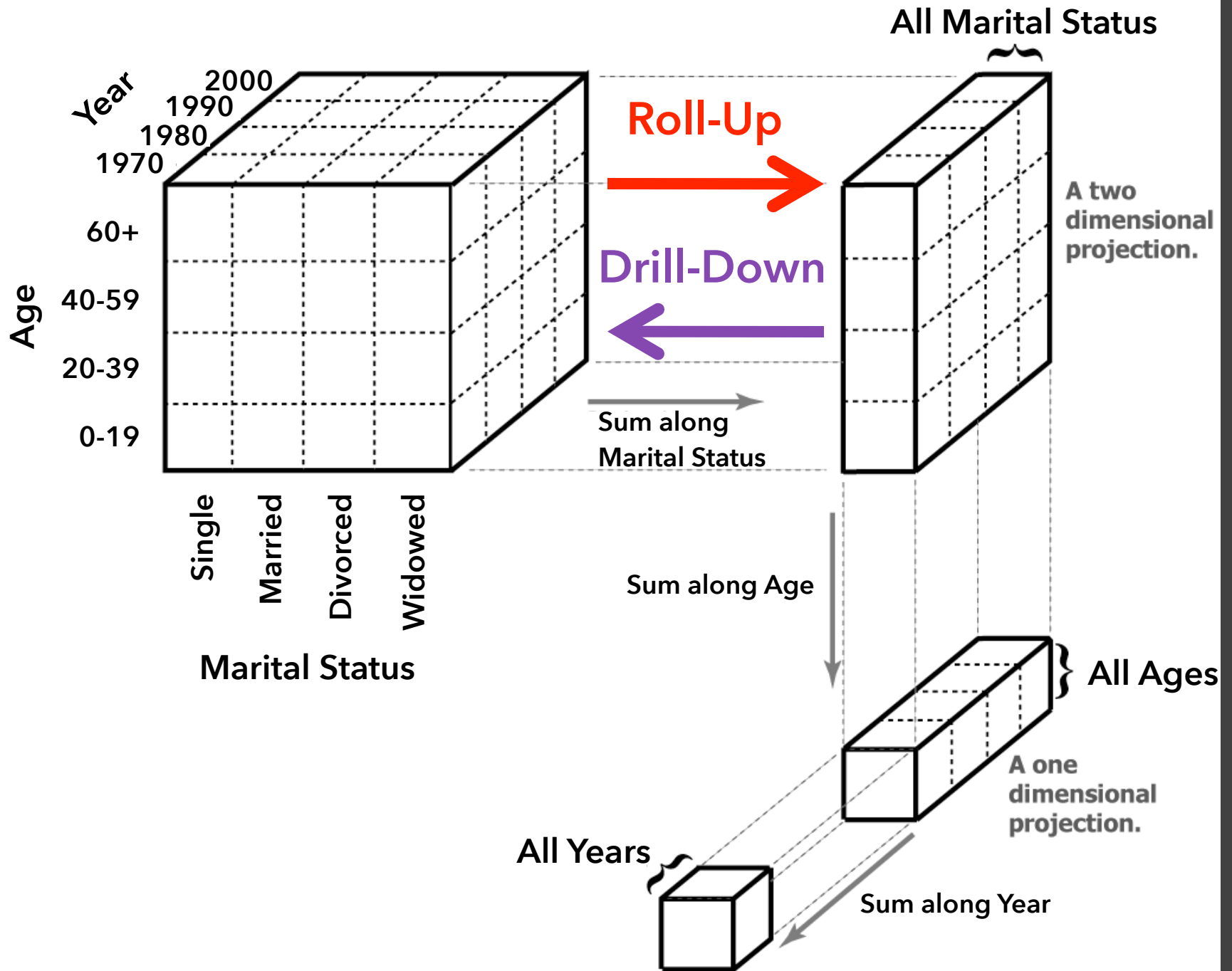
# Roll-Up and Drill-Down

Need more detailed information?

**Drill-down** into additional dimensions

```
SELECT year, age, marst, sum(people)
FROM census
GROUP BY year, age, marst;
```





YEAR	AGE	MARST	SEX	PEOPLE
1850	0	0	1	1,483,789
1850	5	0	1	1,411,067
1860	0	0	1	2,120,846
1860	5	0	1	1,804,467
...				

AGE	MARST	SEX	1850	1860	...
0	0	1	1,483,789	2,120,846	...
5	0	1	1,411,067	1,804,467	...
...					

Which format might we prefer?

**Administrivia**

# Assignment 1: Visualization Design

**Design a static visualization for a data set.**

College admissions can play a profound role in determining one's future life and career. We've collected admissions data (grouped by gender) for selected departments at a major university.

You must choose the message you want to convey. What question(s) do you want to answer? What insight do you want to communicate?



# Assignment 1: Visualization Design

Pick a **guiding question**, use it to title your vis.

Design a **static visualization** for that question.

You are free to **use any tools** (inc. pen & paper).

**Deliverables** (upload via Canvas; see A1 page)

Image of your visualization (PNG or JPG format)

Short description + design rationale ( $\leq 4$  paragraphs)

Due by **5:00 pm, Monday April 4.**

# Next Tuesday: Design Exercise

We will **review A1 submissions**

*So be sure to turn yours in on time!*

We will then have a **redesign exercise**

*Please bring **paper, pens, etc** for sketching*

Image



# Visual Language is a Sign System



Jacques Bertin

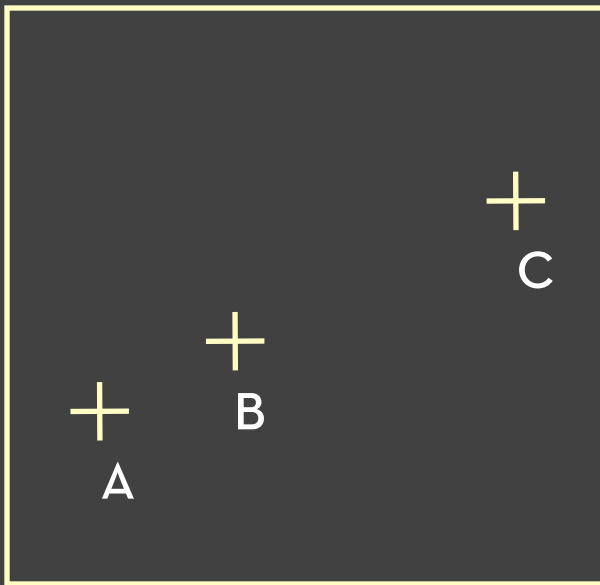
Images perceived as a set of signs

Sender encodes information in signs

Receiver decodes information from signs

Sémiologie Graphique, 1967

# Bertin's Semiology of Graphics



1. A, B, C are distinguishable
2. B is between A and C.
3. BC is twice as long as AB.

∴ Encode quantitative variables

*"Resemblance, order and proportion are the three signfields in graphics."* - Bertin

# LES VARIABLES DE L'IMAGE

	POINTS			LIGNES			ZONES	
XY 2 DIMENSIONS DU PLAN								
Z TAILLE								
VALEUR								

# LES VARIABLES DE SÉPARATION DES IMAGES

GRAIN								
COULEUR								
ORIENTATION								
FORME								

# Visual Encoding Variables

Position (x 2)

Size

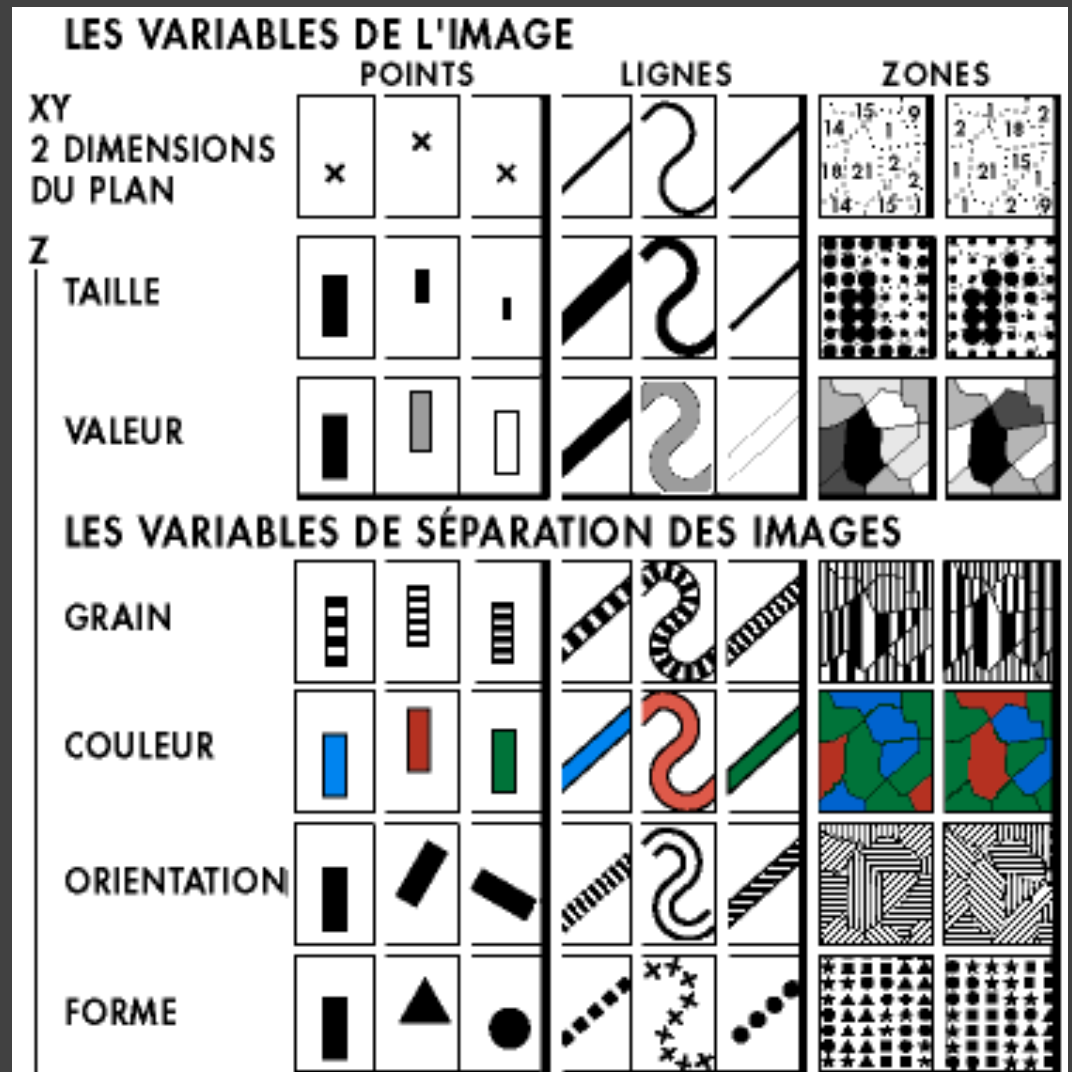
Value

Texture

Color

Orientation

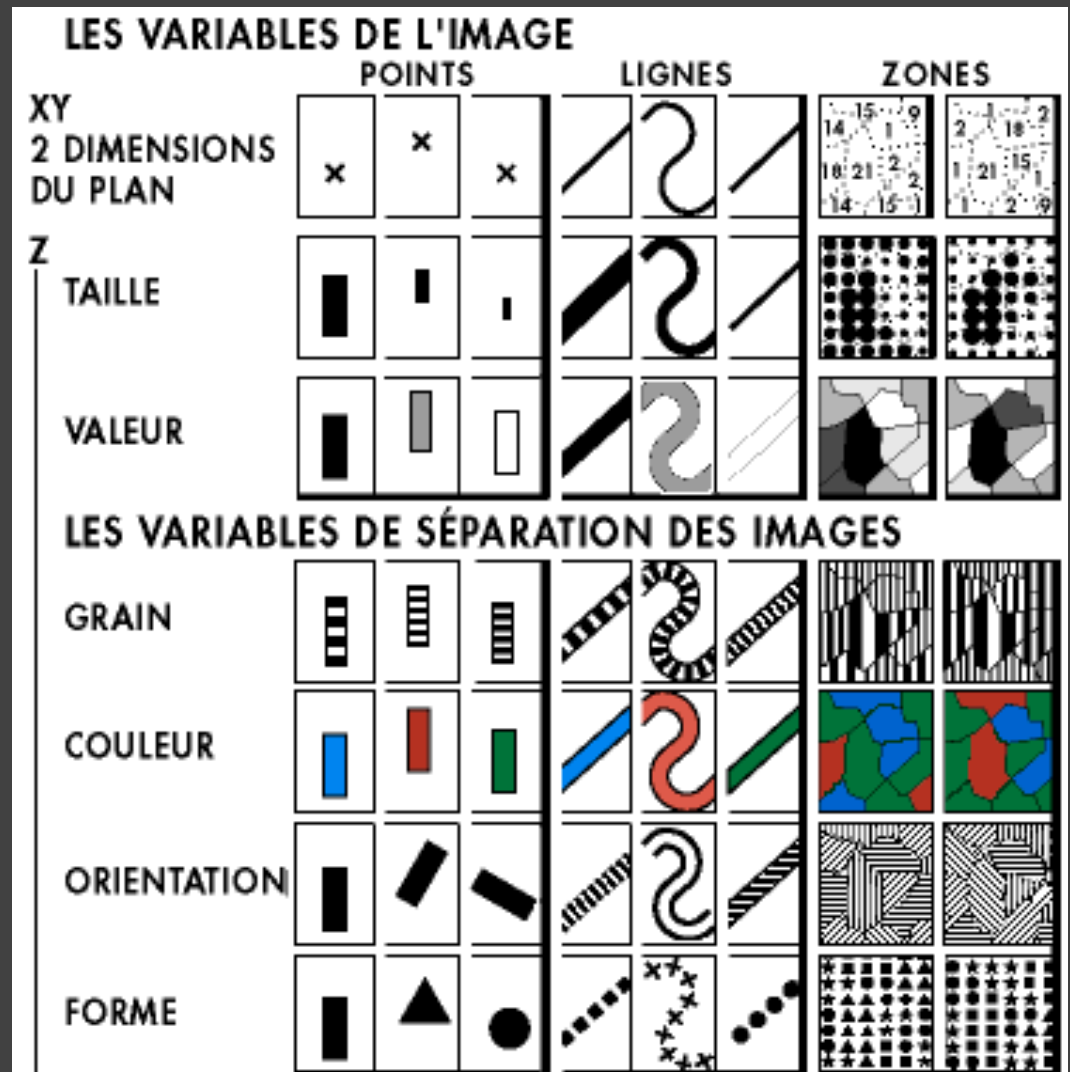
Shape





# Visual Encoding Variables

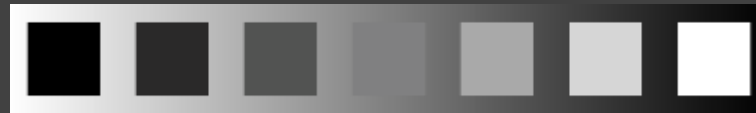
Position  
 Length  
 Area  
 Volume  
 Value  
 Texture  
 Color  
 Orientation  
 Shape  
 Transparency  
 Blur / Focus ...



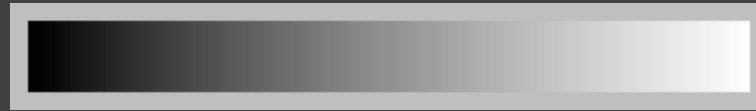
# Information in Hue and Value

Value is perceived as ordered

∴ Encode ordinal variables (O)



∴ Encode continuous variables (Q) [not as well]



Hue is normally perceived as unordered

∴ Encode nominal variables (N) using color



# Bertin's "Levels of Organization"

Position

N	O	Q
---	---	---

Nominal

Size

N	O	Q
---	---	---

Ordinal

Value

N	O	Q
---	---	---

Quantitative

Note:  $Q \subset O \subset N$

Texture

N	o	
---	---	--

Color

N		
---	--	--

Orientation

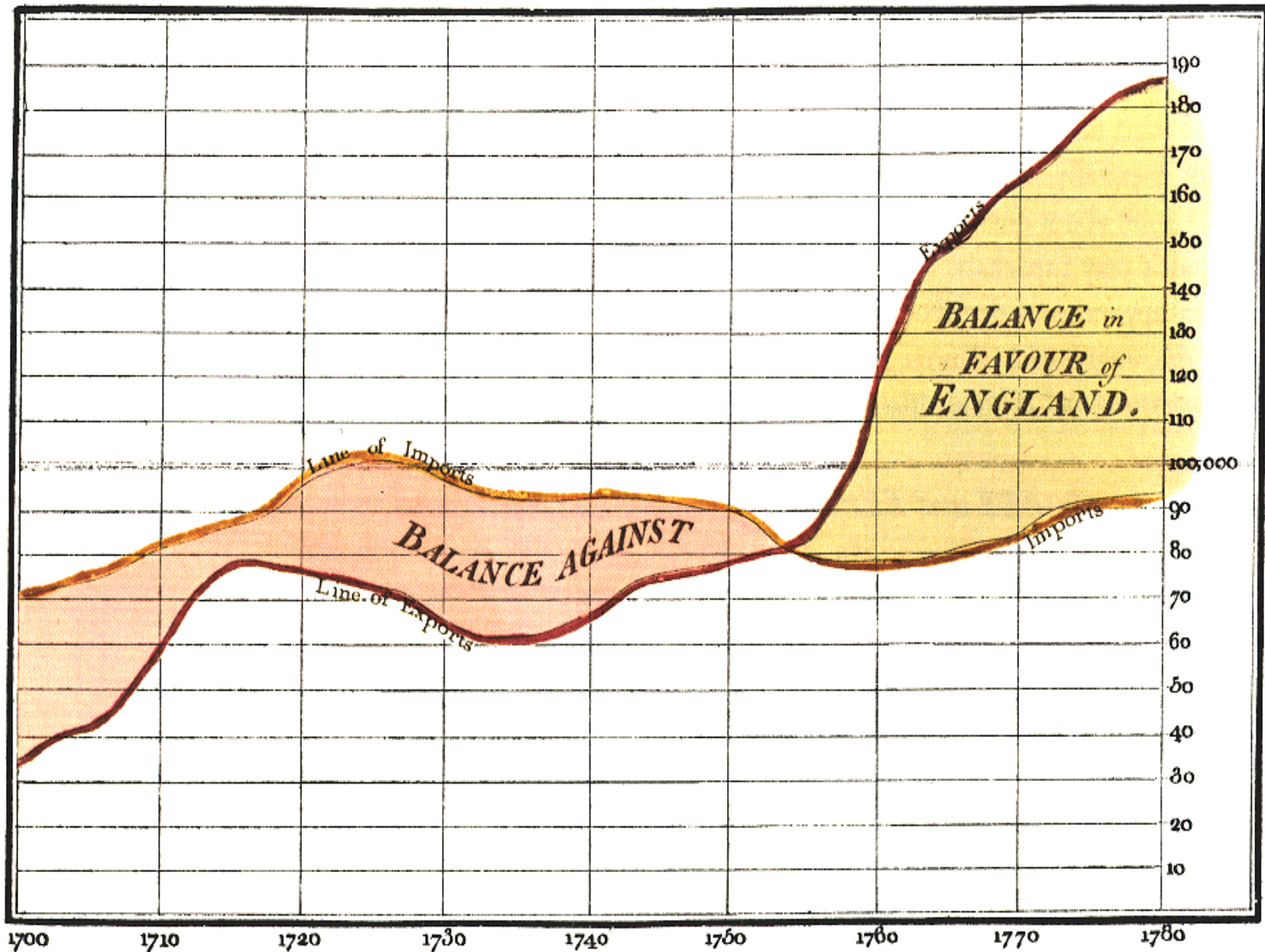
N		
---	--	--

Shape

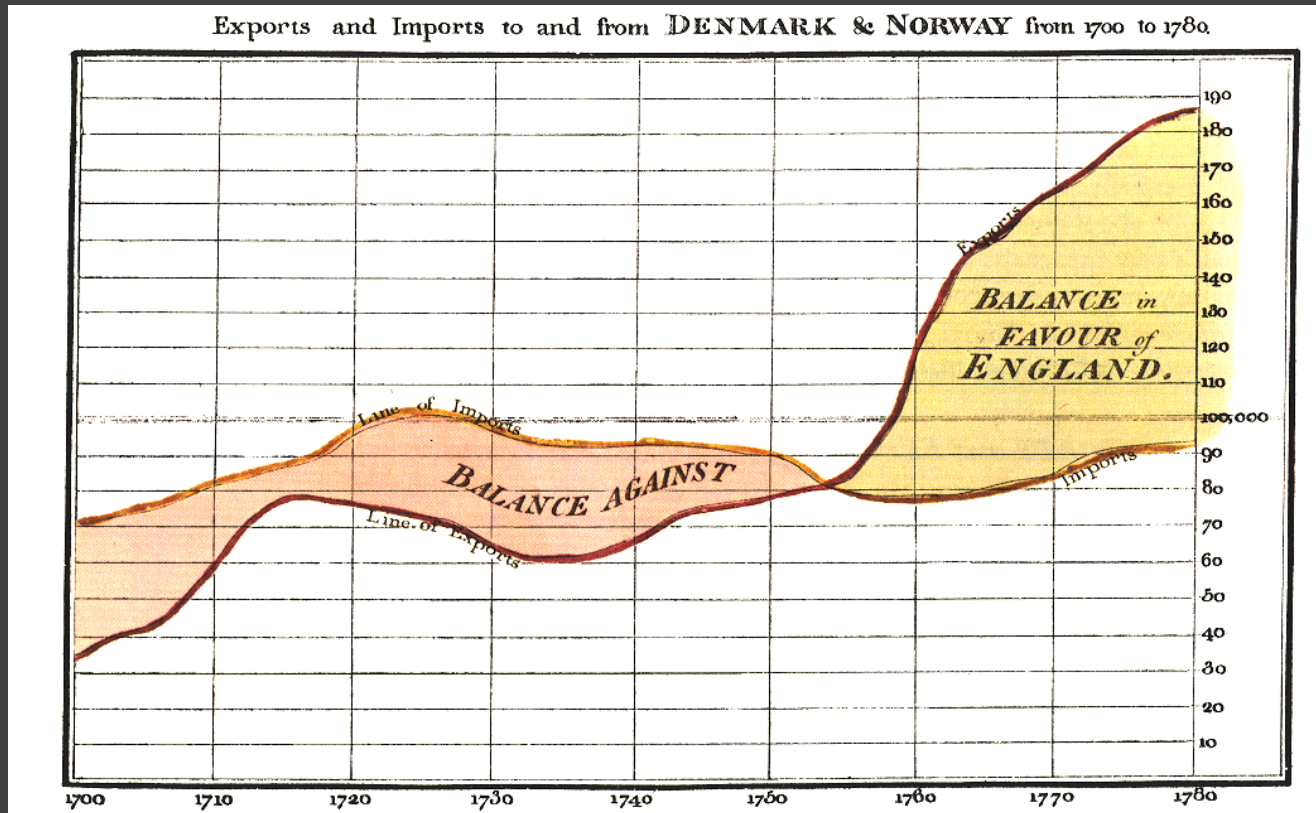
N		
---	--	--

# Deconstructions

Exports and Imports to and from DENMARK & NORWAY from 1700 to 1780.



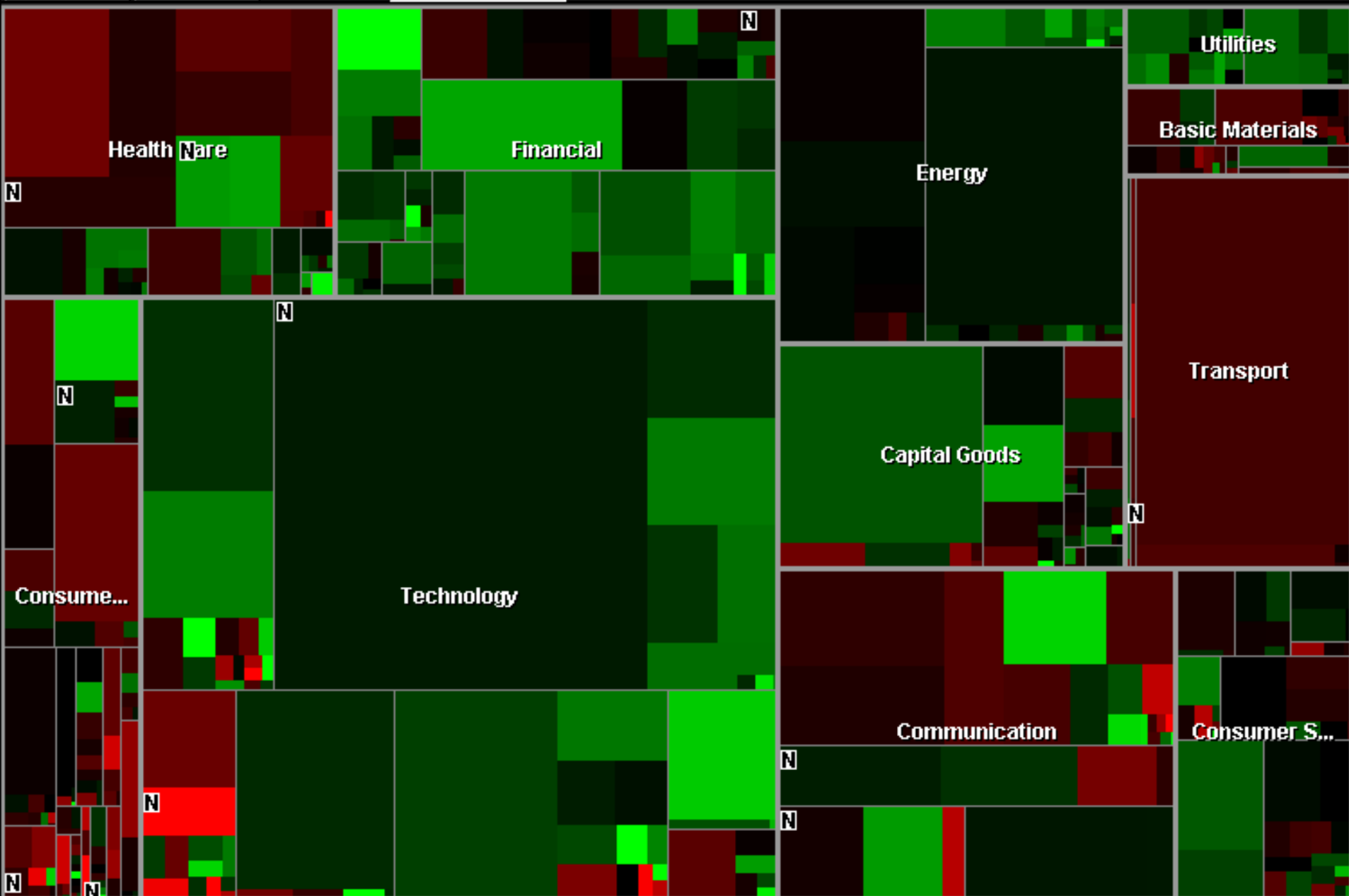
# William Playfair, 1786



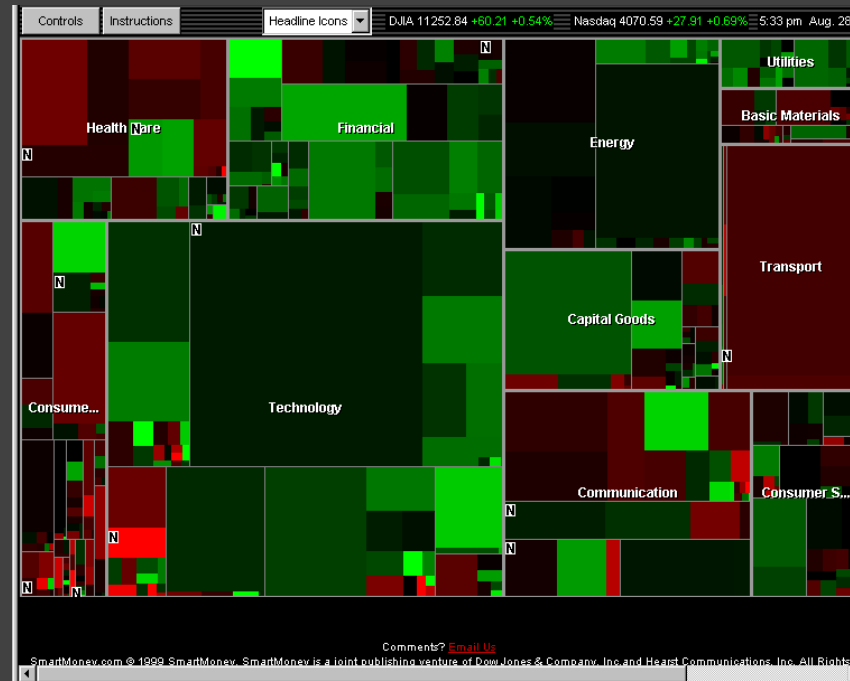
X-axis: year (Q)

Y-axis: currency (Q)

Color: imports/exports (N, O)



# Wattenberg's Map of the Market



Rectangle Area: market cap ( $Q$ )

Rectangle Position: market sector ( $N$ ), market cap ( $Q$ )

Color Hue: loss vs. gain ( $N$ ,  $O$ )

Color Value: magnitude of loss or gain ( $Q$ )



# Minard 1869: Napoleon's March

## Carte Figurative des pertes successives en hommes de l'Armée Française dans la campagne de Russie 1812-1813.

Dressée par M. Minard, Inspecteur Général des Ponts et Chaussées en retraite Paris, le 20 Novembre 1869.

Les nombres d'hommes présents sont représentés par les largeurs des zones colorées à raison d'un millimètre pour dix mille hommes; ils sont de plus écrits en travers des zones. Le rouge désigne les hommes qui entrent en Russie, le noir ceux qui en sortent. Les renseignements qui ont servi à dresser la carte ont été puisés dans les ouvrages de M. M. Chiers, de Légar, de Fezensac, de Chambray et le journal inédit de Jacob, pharmacien de l'Armée depuis le 28 Octobre.

Pour mieux faire juger à l'œil la diminution de l'armée, j'ai supposé que les corps du Prince Jérôme et du Maréchal Davoust qui avaient été détachés sur Minsk et Mohilow et qui s'en rejoignent vers Orscha et Witebsk, avaient toujours marché avec l'armée.

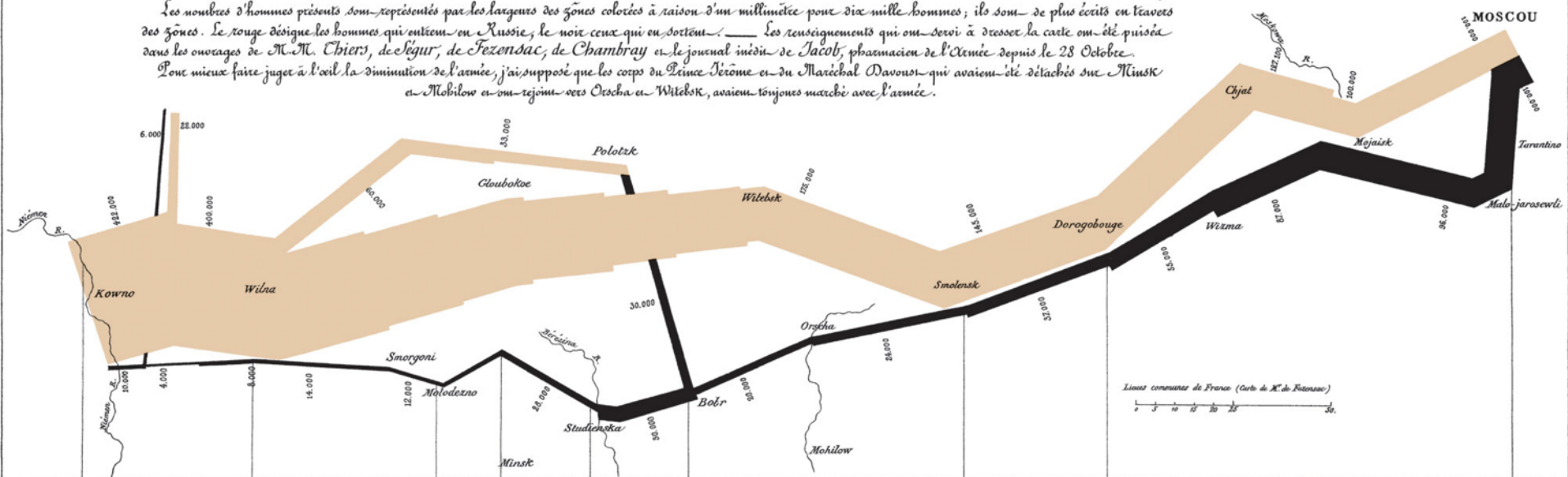
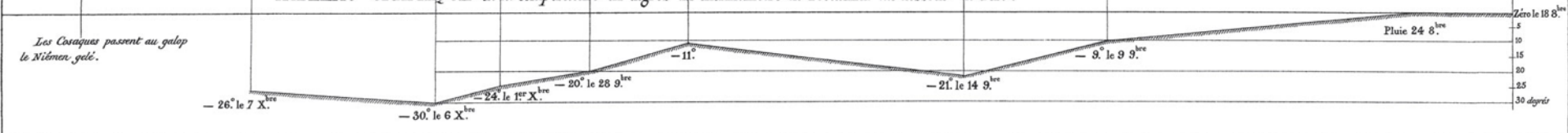
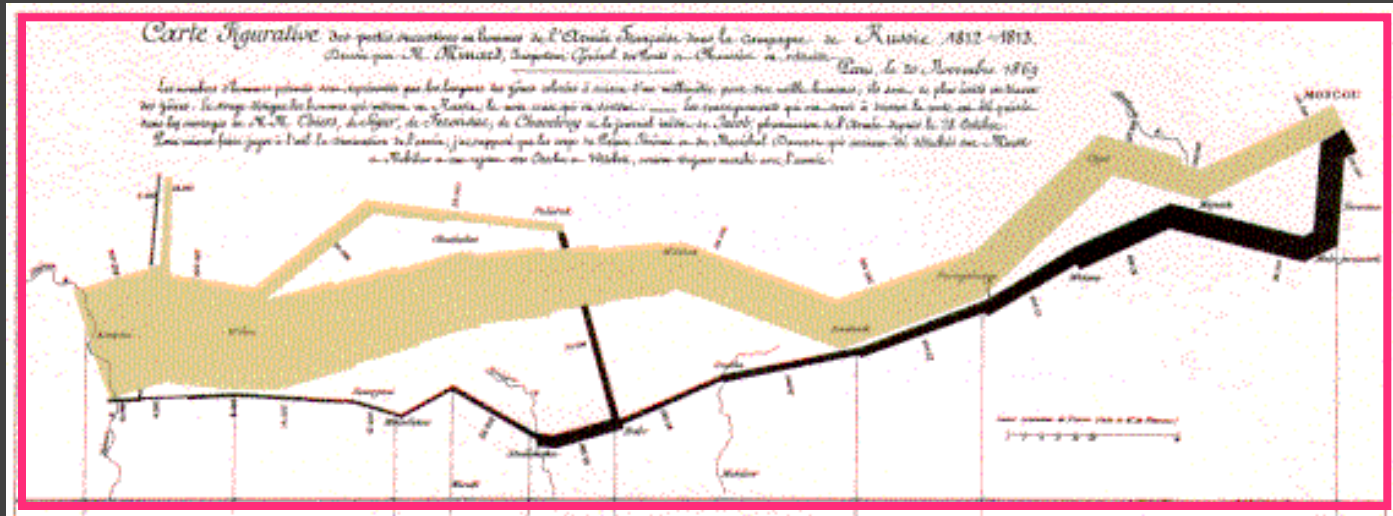


TABLEAU GRAPHIQUE de la température en degrés du thermomètre de Réaumur au dessous de zéro.

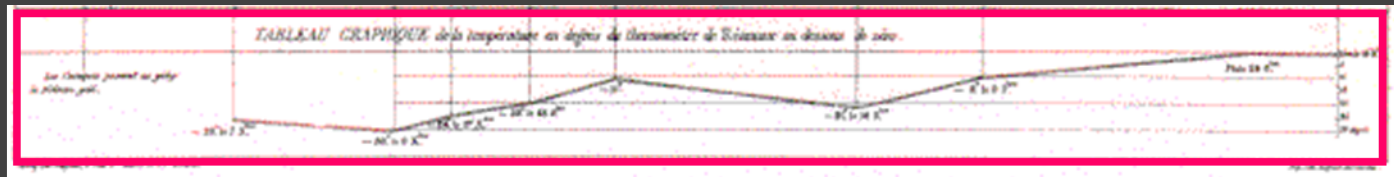


Les Cosaques passent au galop le Niémen gelé.

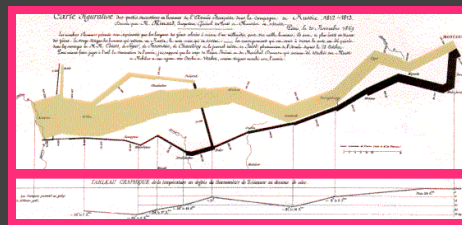
# Single-Axis Composition



+



=



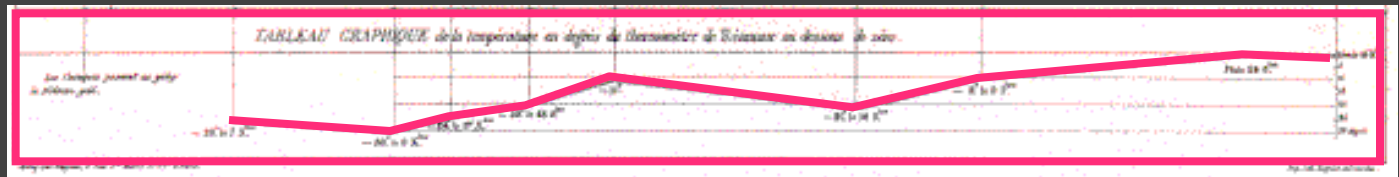
# Mark Composition

Y-axis: temperature (Q)

+

X-axis: longitude (Q) / time (O)

=



Temp over space/time (Q x Q)

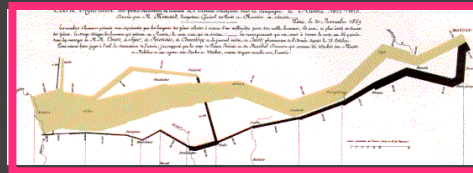
# Mark Composition

Y-axis: longitude (Q)

+ X-axis: latitude (Q)

+ Width: army size (Q)

=

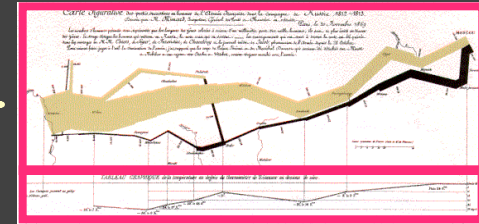
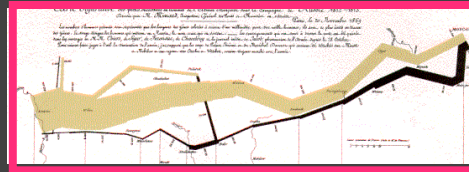


Army position (Q x Q) and army size (Q)

longitude (Q)

latitude (Q)

army size (Q)



temperature (Q)

latitude (Q) / time (O)



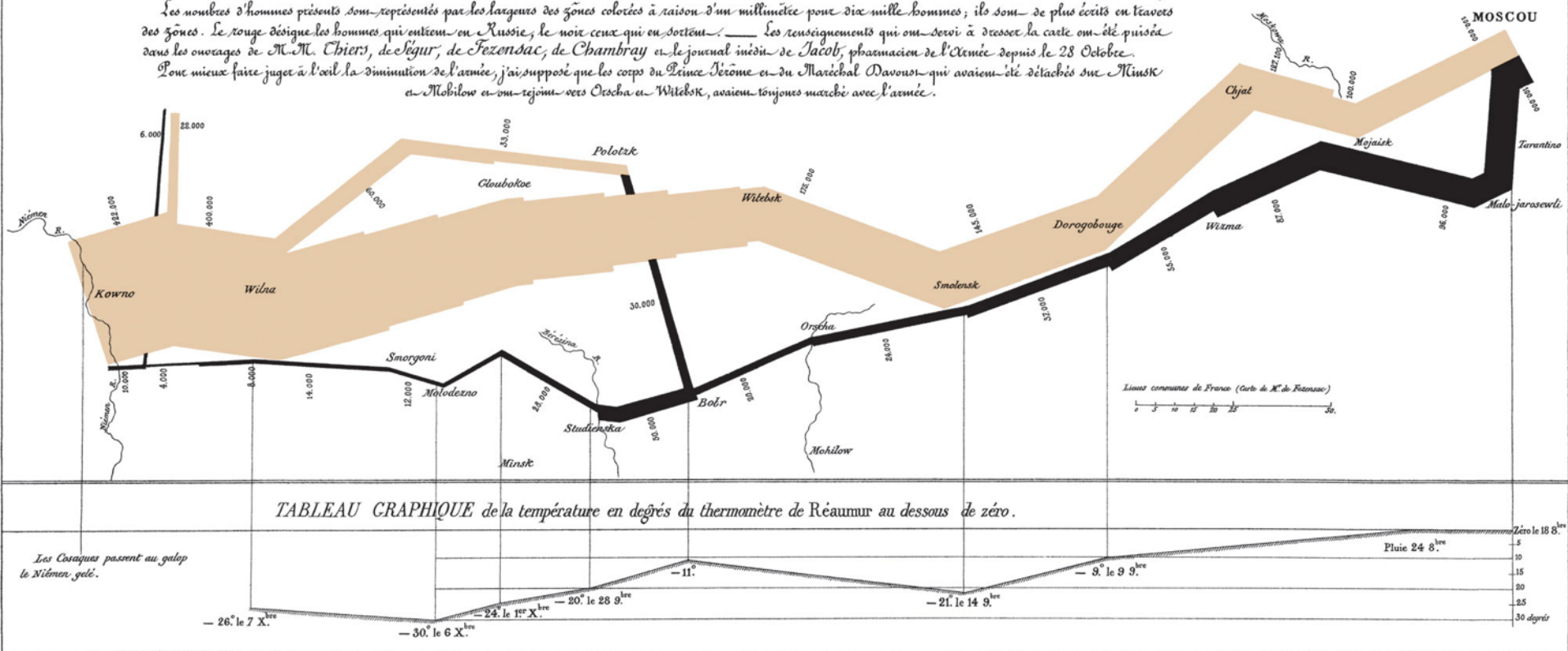
# Minard 1869: Napoleon's March

## Carte Figurative des pertes successives en hommes de l'Armée Française dans la campagne de Russie 1812-1813.

Dressée par M. Minard, Inspecteur Général des Ponts et Chaussées en retraite Paris, le 20 Novembre 1869.

Les nombres d'hommes présents sont représentés par les largeurs des zones colorées à raison d'un millimètre pour dix mille hommes; ils sont de plus écrits en travers des zones. Le rouge désigne les hommes qui entrent en Russie, le noir ceux qui en sortent. Les renseignements qui ont servi à dresser la carte ont été puisés dans les ouvrages de M. M. Chiers, de Léger, de Fezensac, de Chambray et le journal inédit de Jacob, pharmacien de l'Armée depuis le 28 Octobre.

Pour mieux faire juger à l'œil la diminution de l'armée, j'ai supposé que les corps du Prince Jérôme et du Maréchal Davoust qui avaient été détachés sur Minsk et Mohilow et qui rejoignent vers Orscha et Witebsk, avaient toujours marché avec l'armée.



Depicts at least 5 quantitative variables. Any others?

# Formalizing Design

# Choosing Visual Encodings

Assume  $k$  visual encodings and  $n$  data attributes. We would like to pick the “best” encoding among a combinatorial set of possibilities of size  $(n+1)^k$

## Principle of Consistency

The properties of the image (visual variables) should match the properties of the data.

## Principle of Importance Ordering

Encode the most important information in the most effective way.



# Design Criteria [Mackinlay 86]

## Expressiveness

*A set of facts is expressible in a visual language if the sentences (i.e. the visualizations) in the language express all the facts in the set of data, and only the facts in the data.*

## Effectiveness

*A visualization is more effective than another visualization if the information conveyed by one visualization is more readily perceived than the information in the other visualization.*

# Design Criteria [Mackinlay 86]

## Expressiveness

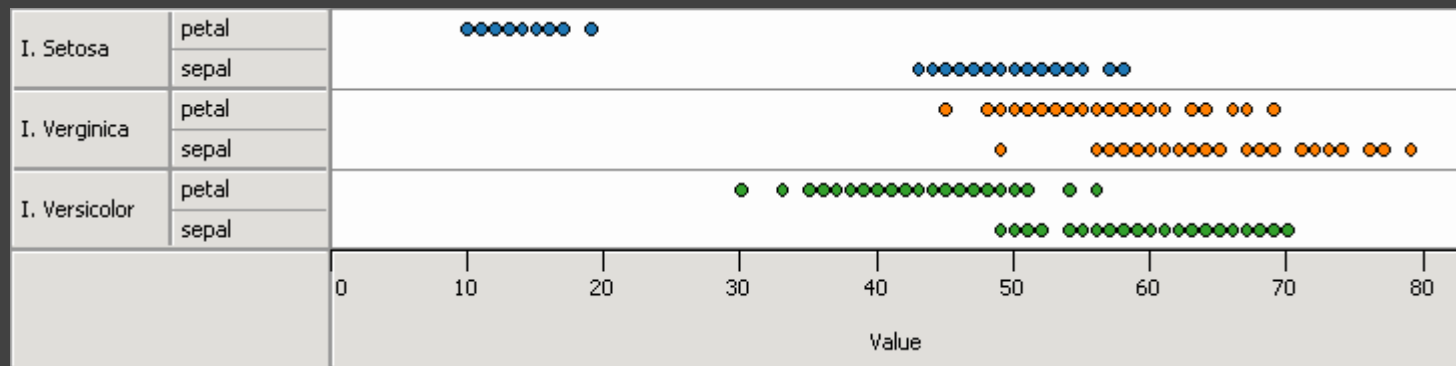
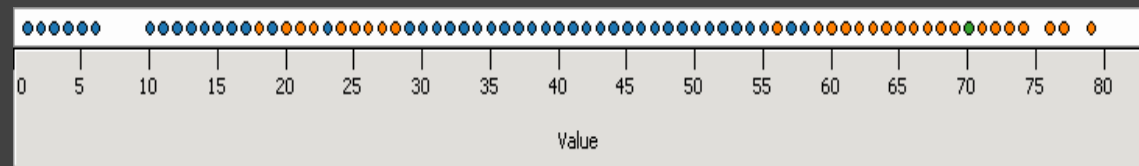
A set of facts is *expressible* in a visual language if the sentences (i.e. the visualizations) in the language express all the facts in the set of data, and only the facts in the data.

## Effectiveness

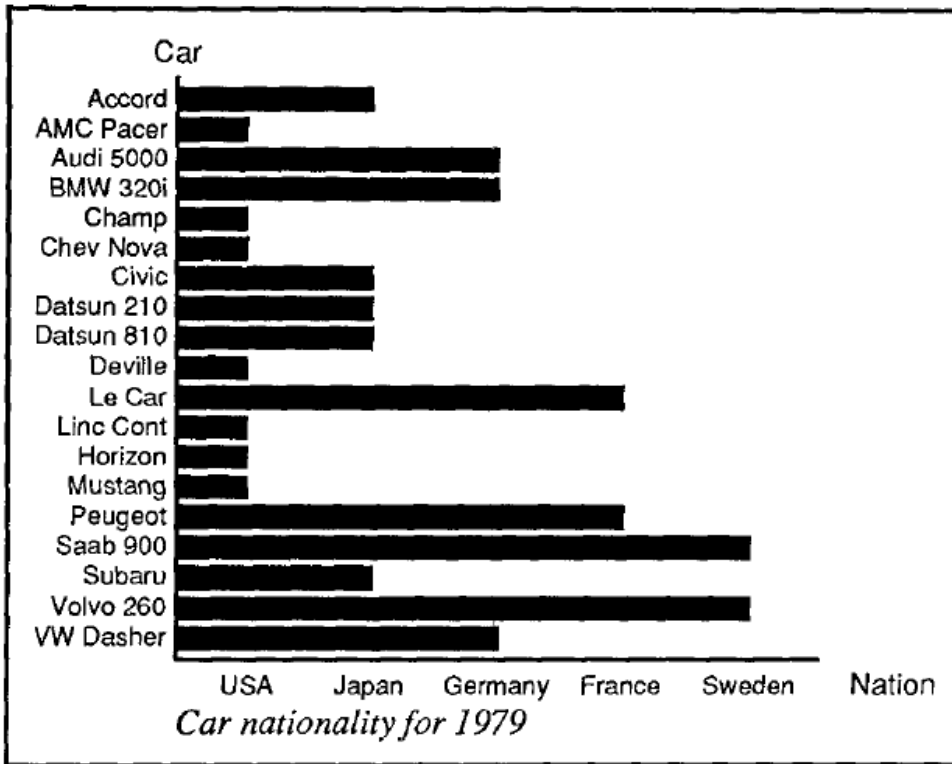
Visualization A is more effective than another visualization if the information conveyed by one is perceived more effectively than the other in the other visualization.

# Can not express the facts

A multivariate relation may be *inexpressive* in a single horizontal dot plot because multiple records are mapped to the same position.



# Expresses facts not in the data



apt

Fig. 11. Incorrect use of a bar chart for the *Nation* relation. The lengths of the bars suggest an ordering on the vertical axis, as if the USA cars were longer or better than the other cars, which is not true for the *Nation* relation.

A length is interpreted as a quantitative value.

# Design Criteria [Mackinlay 86]

## Expressiveness

A set of facts is *expressible* in a visual language if the sentences (i.e. the visualizations) in the language express all the facts in the set of data, and only the facts in the data.

## Effectiveness

Visualization A is more effective than another visualization if the information conveyed by one is perceived more effectively than the other in the other visualization.

# Design Criteria [Mackinlay 86]

## Expressiveness

A set of facts is *expressible* in a visual language if the sentences (i.e. the visualizations) in the language express all the facts in the set of data, and only the facts in the data.

## Effectiveness

A visualization is more *effective* than another visualization if the information conveyed by one visualization is more readily perceived than the information in the other visualization.

# Design Criteria [Tversky 02]

## Congruence

The structure and content of the external representation should correspond to the desired structure and content of the internal representation.

## Apprehension

The structure and content of the external representation should be readily and accurately perceived and comprehended.

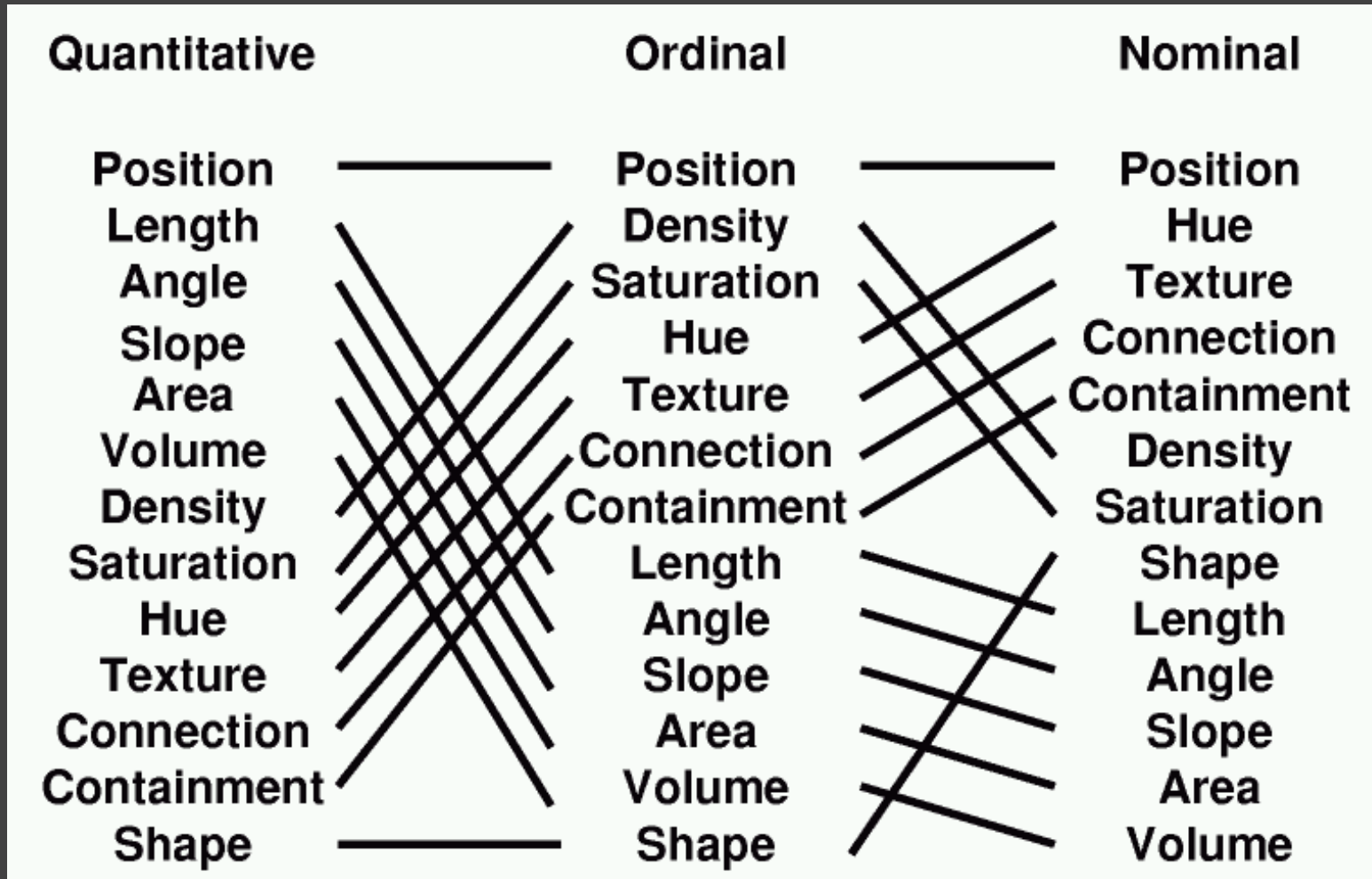
# Design Criteria *Translated*

**Tell the truth and nothing but the truth**  
(don't lie, and don't lie by omission)

**Use encodings that people decode better**  
(where better = faster and/or more accurate)



# Mackinlay's Ranking



Conjectured *effectiveness* of encodings by data type

# Mackinlay's Design Algorithm

**APT** - "A Presentation Tool", 1986

**User formally specifies data model and type**

Input: ordered list of data variables to show

**APT searches over design space**

Test expressiveness of each visual encoding

Generate encodings that pass test

Rank by perceptual effectiveness criteria

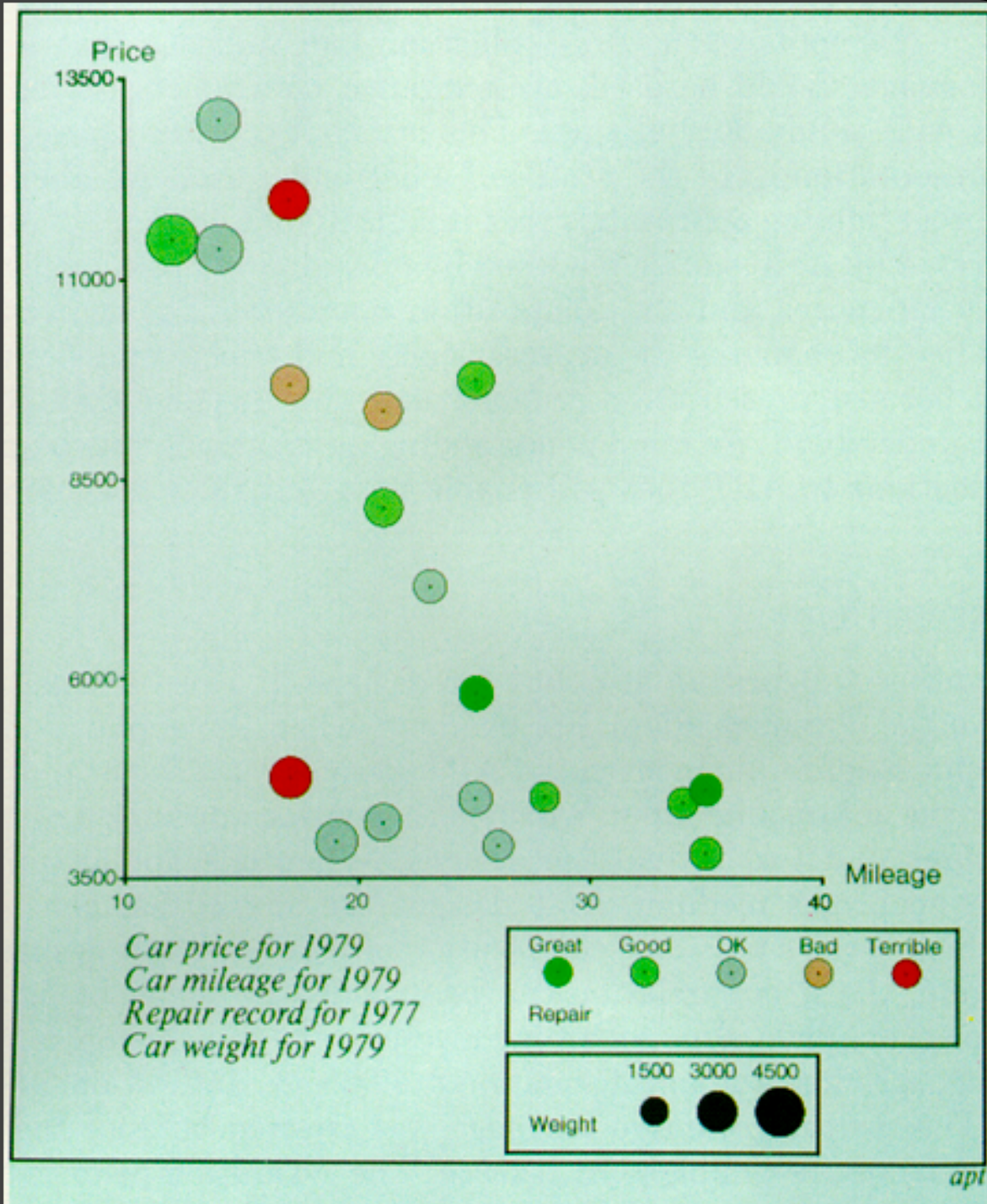
**Output the "most effective" visualization**

# APT

Automatically  
generate chart  
for car data

Input variables:

1. Price
2. Mileage
3. Repair
4. Weight



# Limitations of APT?

# Limitations of APT

**Does not cover many visualization techniques**

Networks, hierarchies, maps, diagrams

Also: 3D structure, animation, illustration, ...

**Does not consider interaction**

**Does not consider semantics / conventions**

**Assumes single visualization as output**

# Summary: Data & Image Models

## Formal specification

Data model: relational data; N,O,Q types

Image model: visual encoding channels

Encodings map data to visual variables

## Choose expressive and effective encodings

Rule-based tests of expressiveness

Perceptual effectiveness rankings

**Question:** how do we establish effectiveness criteria? *Subject of perception lectures...*

# Assignment 1: Visualization Design

Pick a **guiding question**, use it to title your vis.

Design a **static visualization** for that question.

You are free to **use any tools** (inc. pen & paper).

**Deliverables** (upload via Canvas; see A1 page)

Image of your visualization (PNG or JPG format)

Short description + design rationale ( $\leq 4$  paragraphs)

Due by **5:00 pm, Monday April 4.**